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Alarm management based on diagnosis

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Abstract: The transitions between operational modes (startup/shutdown) in chemical processes generate alarm floods and cause critical alarm saturation. We propose in this paper an approach of alarm management based on a diagnosis process. This diagnosis step relies on situation recognition to provide to the operators relevant information on the failures inducing the alarms flows. The situation recognition is based on chronicle recognition where we propose to use the hybrid causal model of the system and the expertise to generate the pattern event sequences from which the chronicles will be extracted using the Heuristic Chronicle Discovery Algorithm Modified HCDAM. An illustrative example in the field of petrochemical plants is presented in the article.

Keywords: Alarm management, Diagnosis, Chronicles, Transitional stages, Hybrid models

1. INTRODUCTION

The petrochemical industries losses have been estimated at 20 billion dollars only in the U.S. each year, and the AEM (Abnormal Events Management) has been classified as a problem that needs to be solved. Hence the alarm management is one of the aspects of great interest in the safety planning for the different plants. In the process state transitions such as startup and shutdown stages, the alarm flood increases and generates critical conditions in which the operator does not respond efficiently. A dynamic alarm management is then required (Beebe et al. (2013)). Currently, many fault detection and diagnosis techniques for multimode processes have been proposed; however, these techniques cannot indicate fundamental faults in the basic alarm system, Zhu et al. (2014); in the other hand the technical report Advance Alarm System Requirements EPRI (The Electric Power Research Institute) suggests a cause-consequence and event-based processing. Therefore, in this paper, a dynamic alarm management strategy is proposed in order to deal with alarm floods happening during transitions of chemical processes. This approach relies on situations recognition (i.e. chronicle recognition). As, the efficiency of alarm management approaches depends on the operator expertise and process knowledge, our final objective is to develop a diagnosis approach as a decision tool for operators. The paper is divided into 5 sections. Section 2 presents the Chronicle based alarm management proposal. The Section 3 presents the case study related with an illustrative application in the petrochemical sector. Section 4 expresses the formal framework for this analysis including the hybrid causal model and the description of the chronicle discovery algorithm. Finally, the construction of the chronicle database is given in the section 5.

2. CHRONICLE BASED ALARM MANAGEMENT

The Chronicle Based Alarm Management (CBAM) methodology proposed in this paper merges different techniques to take the hybrid aspect and the standard operational procedures of the concerned processes into account. These two features stand out of the literature (Jing et al. (2013), S. Xu (2014), Srinivasan et al. (2005), Bhagwat et al. (2003)). Another important aspect is the analysis of the Dynamic Alarm Management: most of the time the alarm is assumed to be a static indicator, in our proposal an alarm is an event with an occurrence date and the alarm flow is formally modeled by a chronicle (Vasquez et al. (2015)) as presented in section 4.2. Transposing this methodology to large-scale systems would benefit from a decentralized approach in which local chronicles would be learned and then integrated thanks to shared events. The main steps of this methodology are:

(1) From the standard operating procedures and from the evolution of the continuous variables, determine the set of event types in startup and shutdown stages.

(2) From the expertise and the event abstractions determine the date of occurrence of each event type to construct the representative event sequences.
cannot change the operational state, e.g. the tank (TK) sensors. The passive components are components which process is a HTG (Hydrostatic Tank Gauging) system and shutdown stages in the unit of water injection. This equipments. To start our analyze, we focus on the startup during the startup stage of the refinery with modified at helping the operator to recognize dangerous conditions riched by news units and elements. Our proposal aims the Cartagena Refinery in Colombia as recently been-detailed further in the article and the next section presents the case study.

3. CASE STUDY - HTG (HYDROSTATIC TANK GAUGING) SYSTEM

The Cartagena Refinery in Colombia as recently been-enriched by news units and elements. Our proposal aims at helping the operator to recognize dangerous conditions during the startup stage of the refinery with modified equipments. To start our analyze, we focus on the startup and shutdown stages in the unit of water injection. This process is a HTG (Hydrostatic Tank Gauging) system composed of passive components, active components and sensors. The passive components are components which cannot change the operational state, e.g. the tank (TK). In the other hand, the active components can change their states of operation by a procedural action, e.g. the two normally closed valves (V1 and V2) and the pump (Pu). The sensors, correspond to the instrumentation that measures the continuous variables, e.g. level sensor (LT), pressure sensor (PT), inflow sensor (FT1) and outflow sensor (FT2), see Fig. 1. The standard operating procedures give us the standard procedural actions for the startup and shutdown stages. For the correct execution of these procedures, the operators must execute the actions according to the correct evolution of the procedure. The abnormal situations are detected when the evolution of the procedural actions and the continuous variables evolution do not correspond to the standard operating procedure and wrong event type occurrences, happen. The fluctuations of the inlet flow of the tank, the response time of the pump that causes the outlet pressure and other conditions generate uncertain that can be determined by expertise. because to obtain a complex model which simulate all the process uncertain requires a lot of time and resources to build it.

4. FORMAL FRAMEWORK

This section presents the formal framework of the Chronicle Based Alarm Management (CBAM) methodology proposed.

4.1 Hybrid Causal Model

The hybrid system is represented by an extended transition system, whose discrete states represent the different modes of operation for which the continuous dynamics are characterized by a qualitative domain. Formally, a hybrid causal system is defined as a tuple Pons et al. (2015):

\[ \Gamma = (\vartheta, D, Tr, E, CSD, Init, COMP, DMC) \] (1)

Where

- \( \vartheta = \{v_i\} \) is a set of continuous process variables which are function of time \( t \).
- \( D \) is a set of discrete variables. \( D = Q \cup K \cup VQ \).
  - \( Q \) is a set of states \( q_i \) of the transition system which represent the system operation modes.
  - The set of auxiliary discrete variables \( K = \{K_i, i = 1,...,n_c\} \) represents the system configuration in each mode \( q_i \), where \( K_i \) indicates the discrete state of the active components.
  - \( VQ \) is a set of qualitative variables whose values are obtained from the behavior of each continuous variable \( v_i \).
- \( E = \Sigma \cup \Sigma^e \) is a finite set of observable (\( \Sigma_o \)) and unobservable (\( \Sigma_{uo} \)) event types, noted \( \sigma \), where:
  - \( \Sigma \) is the set of event type associated to the procedural actions in the startup or shutdown stages.
  - \( \Sigma^e \) is the set of event type associated to the behavior of the continuous process variables.
- \( Tr : Q \times \Sigma \rightarrow Q \) is the transition function. The transition from mode \( q_i \) to mode \( q_j \) with associated event \( \sigma \) is noted \( (q_i, \sigma, q_j) \).
- \( CSD \supseteq \bigcup CSD_i \), is the Causal System Description or the causal model used to represent the constraints underlying the continuous dynamics of the hybrid system.

Every \( CSD_i \) associated to a mode \( q_i \), is given by a graph \( (G_c = (\vartheta \cup K, I)) \). \( I \) is the set of influences where there is an edge \( e(v_i, v_j) \in I \) from \( v_i \in \vartheta \) to \( v_j \in \vartheta \) if the variable \( v_i \) influences variable \( v_j \). A dynamic continuous model \( DMC_{1e} \) is associated to every influence \( I_k \in I \), see Fig. 2. The model of the active component corresponds to a transfer function of first order with delay. The set of components is noted as \( COMP \).

- \( Init \) is the initial condition of the hybrid system.

4.2 Chronicle model

Let us consider time as a linearly ordered discrete set of instants. The occurrence of different events in time represents the system dynamics and a model can be determined to diagnose the correct evolution. An event is defined as a pair \( (e_i, t_i) \), where \( e_i \in E \) is an event.
Fig. 2. Dynamic Model of Control DMC

We define \( S \) as the set of all event types and a temporal sequence on \( E \) is an ordered set of events denoted \( S = \{(e_i, t_i)\}_j \) with \( j \in N_l \) where \( l \) is the size of the temporal sequence for the chronicle. We define two next sections present what is an event in our approach and how are defined the events types: we consider two sets of events; those generated by a qualitative abstraction over the process continuous behaviour and those identified from the knowledge of standard operating procedures.

Definition 1: A chronicle is defined as a triplet \( C = (\xi, T, G) \) such that:

- \( \xi \subseteq E \). \( \xi \) is called the topology of the chronicle.
- \( T \) is the set of temporal constraints of the chronicle.
- \( G = (V, A) \) is a directed graph where:
  - \( V \) represent the event types of \( \xi \)
  - \( A \) represents the time constraints between event dates. (Subias et al. (2014))

If the event \( e_1 \) occurs \( t \) time units after \( e_2 \), then it exists a directed link \( A \) from \( e_1 \) to \( e_2 \) associated with a time constraint. Considering the two events \( (e_i, t_i) \) and \( (e_j, t_j) \), we define the time interval as the pair \( \tau_{ij} = [t_i, t_j] \), \( \tau_{ij} \in T \) corresponding to the lower and upper bounds on the temporal distance between the two event dates \( t_i \) and \( t_j \).

The two next sections present what is an event in our approach and how are defined the events types: we consider two sets of events; those generated by a qualitative abstraction over the process continuous behaviour and those identified from the knowledge of standard operating procedures.

4.3 Event generation by qualitative abstraction of continuous behavior

In each mode of operation, variables evolve according to the corresponding dynamics. This evolution is represented with qualitative values. The domain \( D(V) \) of a qualitative variable \( V \) is obtained through the function \( f_{qual} : D(V) \rightarrow D(V) \) that maps the continuous values of variable \( v_i \) to ranges defined by limit values (High noted \( H_i \) and Low noted \( L_i \)).

The behavior of these qualitative variables is represented in Fig. 3 by the automaton \( G_{V_i} = (V_Q, \Sigma^c, \gamma) \) where \( V_Q \) is the set of the possible qualitative states (\( V^L : Low, V^M : Medium, V^H : High \)) of the continuous variable \( v_i \). \( \Sigma^c \) is the finite set of events associated to the transitions and \( \gamma : V_Q \times \Sigma^c \rightarrow V_Q \) is the transition function. The corresponding event generator is defined by the abstraction function \( f_{V_Q \rightarrow \sigma} \):

\[
\begin{align*}
V^Q &\rightarrow \sigma: V_Q \times \gamma(V_Q, \Sigma^c) \rightarrow \Sigma^c \\
\forall V_i \in V_Q, (V_i^n, V_i^m) &\rightarrow \begin{cases} \\
(\text{low}(v_i)) \text{ if } V_i^L \rightarrow V_i^M, & V_i^L \text{ if } L_i < v_i < H_i \\
(\text{high}(v_i)) \text{ if } V_i^H \rightarrow V_i^M, & V_i^H \text{ if } v_i \geq H_i \\
(\text{low}(v_i)) \text{ if } V_i^L \rightarrow V_i^M, & V_i^L \text{ if } v_i \leq L_i \\
\end{cases}
\end{align*}
\]

4.4 Event identification from procedural action

In the system HTG of the case of study, the set of event types \( \Sigma \) that represent the procedure actions is:

\[
\Sigma = \{V_1_{o,c}, V_2_{o,c}, Pu_{f-n}, V_1_{a,c}, V_2_{a,c}, Pu_{n-f}, M/A\}
\]

The underlying DES (Discrete event system) of the HTG system represents the sequence of observable procedure actions for a startup stage (indicated by the red or green arrows on Fig. 4) corresponding to the evolution of the operation modes (i.e. \( q_0, q_1, q_2, q_3 \) and \( q_7 \)). To each operation mode \( q_i \) is associated a causal system description to identify the influences between the variables \( L, P_o \) and \( Q_o(V_2) \) see Fig. 5. These influences allow to determine the event types \( \Sigma^c \) occurrence.
indicating that the level of the liquid into the tank $TK$ has passed the limit of low level. Between 1 and 4 time units after $h$, the liquid into the tank must arrive to the high limit of the level and the event type $i$: $h^L_{(L)}$ must occur. At this time point, the ordered sequence of event types that has occurred is $a, h, i$. The high limit of the level into the tank is the condition for continuing the procedure actions $Open$ $V2$ and $Turn$ $ON$ $P_u$ ($b$: $V2_{on}$ and $c$: $Pu_{f-n}$). If the operator opens the valve $V2$ first, the system passes in the mode of operation $q_4$, but if the pump $P_u$ is turned ON first, the system passes in $q_5$. The duration between the occurrences of event types $b$ and $c$ must be of 1 time unit, leaving the system in the mode of operation $q_7$. At this time point, the ordered sequence of event types that has occurred must be $a, h, i, b, c$ or $a, h, i, c, b$. In the scenario $1_a$: $(a, h, i, c, b)$, the outlet pressure $(Po)$ of the pump $P_u$ increases first of that the outlet flow $(Q_{AV2})$. Then, between 1 and 6 time units after $b$, the pressure $Po$ has passed its limit of low pressure and the event type $l$: $t^r_{(Po)}$ must occur. The outlet flow after 1 unit time has passed its limit of low flow and the event type $p$: $t^r_{(Q_{AV2})}$ must occur. The high limit of pressure $(m$: $h^L_{(Po)}$) occurs between 1 and 6 time units after $p$ and the high limit of outlet flow occurs 1 time unit after $m$. In the scenario $1_b$: $(a, h, i, b, c)$, the event type $p$ occurs between 3 and 4 time units and after $c$. At 1 time unit after $p$, $l$ must occur. After $l$, the event type $q$ must occurs between 3 and 4 time units and the event type $m$ must occur 1 time unit after $q$. At this time point, the ordered sequence of event types that has occurred must be $a, h, i, c, b, l, p, m, q$ or $a, h, i, b, c, p, l, q, m$. In this situation, the unobservable event type $MA$ occurs and the control loops are closed, carrying the system to a steady state. We assume that the control loops are closed whereas $q$ occurs in the scenario $1_a$ or $m$ in the scenario $1_b$. Then, the event type $k$ indicates that the level of liquid in the tank $TK$ decreases from the high limit of level, between 1 and 4 time units after that the control loops are closed. In the same way, the outlet pressure and outlet flow decrease from its high limits $(o$ and $s)$ between 1 and 4 time units after that $k$ occurs. The time units between $s$ and $o$ must be 1. When the event types $o$ and $s$ occur, we assume that the startup stage, finish correctly and the ordered sequences of event types must be $a, h, i, c, b, l, p, m, q, k, o, s$ or $a, h, i, b, c, p, l, q, m, k, s, o$.

For this scenario, we chose the representative event sequences $(Sp_1, Sp_2$ and $Sp_3)$ that represent the extreme behaviors with all the possible sequence order of event types.

$Sp_1 = \langle (a, 6), (b, 7), (i, 8), (c, 9), (h, 10), (l, 11), (p, 12), (m, 13), (q, 14), (k, 15), (a, 16), (s, 17) \rangle$

$Sp_2 = \langle (a, 1), (h, 3), (i, 6), (b, 7), (c, 8), (p, 12), (l, 13), (q, 17), (m, 18), (k, 22), (s, 26), (o, 27) \rangle$

$Sp_3 = \langle (a, 1), (h, 5), (i, 7), (b, 8), (c, 9), (p, 12), (l, 13), (q, 16), (m, 17), (k, 21), (s, 24), (o, 25) \rangle$

The simulation of a normal startup is presented in Fig. 6 where we can see the evolution of the variables $L$ in color blue, $Po$ in color green and $Q_u(V2)$ in color red. This simulation represents only one possible situation in this scenario related with the pattern sequence $Sp_1$.
Fig. 6. Simulation of a normal startup

Fig. 7. Simulation of a startup with a failure in V2

Scenario 2, Abnormal startup This abnormal situation is related to a failure in the valve V2. In this scenario the sequences of event types are the same that the event sequences of a normal startup, until that is detected that the outlet flow in the system does not increase. When the level of liquid in the tank TK arrived to its high limit, the ordered sequence of event types that has occurred must be \( a, h, i, c, b \) or \( a, h, i, b, c \). In scenario2a : \((a, h, i, c, b)\) the event type \( l \) occurs after 1 time units of \( b \). In scenario2b : \((a, h, i, b, c)\) the event type \( l \) occurs after 2 time units of \( c \). The event type \( m \) occurs between 1 and 2 time units after \( l \), then the ordered sequences of event types must be \( a, h, i, c, b, l, m \) or \( a, h, i, b, c, l, m \). For this scenario, we chose the representative event sequences (\( Sp_4, Sp_5 \) and \( Sp_6 \)) that show the extreme behaviors with all the possible sequence order of event types.

\[
Sp_4 = \{(a, 6), (h, 7), (i, 8), (c, 9), (b, 10), (l, 11), (m, 12)\} \\
Sp_5 = \{(a, 1), (h, 3), (i, 6), (b, 7), (c, 8), (l, 10), (m, 12)\} \\
Sp_6 = \{(a, 1), (h, 3), (i, 7), (b, 8), (c, 9), (l, 11), (m, 13)\}
\]

The simulation of this abnormal startup is presented in Fig. 7 where we can see the evolution of the variables \( L \) in the color blue and \( P_o \) in color green. The variable \( Q_o(V2) \) (in red in Fig 6) does not appear because the valve V2 failed. The limits \( PAL, PAH \) and \( PAHH \) correspond to the alarms of low, high and high high pressure. This simulation represents only one possible situation in this scenario related with the pattern sequence \( Sp_4 \).

4.6 Heuristic Chronicle Discovery Algorithm Modified HCDAM

The chronicle exploration process corresponds in discovering all the chronicles, whose instances occur in a given temporal sequence of event types. In many cases the same situation does not implies temporal sequences perfectly identical. The HCDAM learns the chronicles, whose instances occur in all temporal sequences represented exhibiting the same situation (Subias et al. (2014)). Given a set of temporal sequences and a minimum frequency threshold, it finds all minimal frequent chronicles presented in all temporal sequences. The chronicle learning algorithm has the following two phases:

1. It builds a constraint database from a set of the temporal sequences \( \mathcal{S} \) where it stores for each pair of event types its temporal constraints in a constraint graph structure.
2. It generates a set of candidate chronicles initializing with a set of chronicles that were proved to be frequent and it uses the constraint database to explore the chronicle space.

The base of the chronicles stores for each pair of event types its temporal constraints in a constraint graph structure. In this graph, time constraints are nodes of an acyclic graph whose arcs represent the relationship is parent of. Which is defined as:

**Definition 2:** The node \( e_i[t^−,t^+] \) is parent of another \( e_j[t^−,t^+] \) if, only if \( [t^−,t^+] \subset [t^−,t^+] \) and not exist \( e_j[t^−,t^+] \) such that \( [t^−,t^+] \subset [t^−,t^+] \subset [t^−,t^+] \).

**Definition 3:** The graph of constraints is defined as the tuple \( GC = (\varepsilon, \tau, G_c) \) containing time constraints, which are nodes in an oriented acyclic graph whose arcs represent the inclusion relations of the constraints. \( \varepsilon \subseteq \mathcal{E} \) with \( \forall e_i \in \mathcal{E}, e_i \leq e_i+1 \): A finite set of event types is called the typology of the constraint graph. \( T = [\tau_1, \tau_2, \ldots, \tau_p] \) is the set of time constraints of the chronicle. \( G_c = (T, A_c) \) is a directed graph whose nodes represent the time constraints valid for a given frequency and the arcs \( A_c \) represent the relationships is parent of. As this analysis is for several sequences, only the pairs of event types which are present in all sequences, are processed. This leads us to the first stage of the constraint graph construction that is the filtering operation. **Definition 4:** The filtering operation is a preliminary treatment on sequences and it can be summarized in two possible actions: 1. Filtering the event types not present in all sequences \( \mathcal{S} \). If \( \exists S_i \in \mathcal{S} \) such as \( \exists e_i \notin \mathcal{S}_i \), then \( e_i \) will be removed of all other sequences.
2. Filtering on a given set of event types \( \varepsilon = \{e_i, e_j, \ldots \} \) if we are interested only those event types during processing. This option will be useful when we want to learn the patterns of a subset of event types.

5. CONSTRUCTION OF THE CHRONICLE DATABASE

An industrial or complex process \( \mathcal{P} \) is composed of different areas \( \mathcal{P} = \{A_{r1}, A_{r2}, \ldots A_{rn}\} \) where each area \( A_{rk} \) has different operational modes such as startup, shutdown, etc. The set of the chronicles \( \{C_{ij}\} \) for each area \( A_{rk} \) is presented in the matrix below, where the rows represent the operating modes (i.e. \( O_1 : StartUp, O_2 : ShutDown, etc \)) and the columns the normal and abnormal situations.

\[
CA_{rk} = \begin{bmatrix}
O_1 & O_2 & O_3 & \ldots & O_n \\
C_{ij}^{11} & C_{ij}^{12} & \ldots & C_{ij}^{1n} \\
C_{ij}^{21} & C_{ij}^{22} & \ldots & C_{ij}^{2n} \\
\vdots & \vdots & \ddots & \vdots \\
C_{ij}^{n1} & C_{ij}^{n2} & \ldots & C_{ij}^{nn}
\end{bmatrix}
\] (7)

This chronicle database, is to be submitted to a chronicle recognition system that identifies in an observable flow of events all the possible matching with the set of chronicles from which the situation (normal or faulty) can be
assessed. In the following subsection are presented two chronicles \((C_{101} \text{ and } C_{111})\) of the set of chronicles of the HTG (Hydrostatic Tank Gauging) system i.e of the area \(A_{1}\) of the whole system. \(C_{101}\) is a chronicle describing the normal start up stage of the HTG and \(C_{111}\) is associated to failure behavior of type \(f_1\) during a startup stage.

5.1 Using HCDAM

We present two chronicles \((C_{101} \text{ and } C_{111})\) of the set of chronicles of the HTG (Hydrostatic Tank Gauging) system i.e of the area \(A_{1}\) of the whole system. \(C_{101}\) is a chronicle describing the normal start up stage of the HTG and \(C_{111}\) is associated to failure behavior of type \(f_1\) during a startup stage.

Scenario 1, Normal startup: The chronicle \(C_{101}\) that resulted using the algorithm HCDAM is presented in Fig. 8. The pattern event sequences used are the \(Sp_{1}, Sp_{2}\) and \(Sp_{3}\) generated in section IV.

Scenario 2, Abnormal startup: The chronicle \(C_{111}\) that resulted using the algorithm HCDAM is presented in Fig. 9. The representative event sequences used are the \(Sp_{4}, Sp_{5}\) and \(Sp_{6}\) generated in section IV. Similar to the language theory, in the chronicles the alphabet corresponds to \(E\). The timed language \(L^{T}(\xi, T)\) of each chronicle \(C\) will be referenced in the strings \(w\) that can be generated according to the typology of the chronicle and the concatenation of the elements in the strings will be restricted by the set of temporal constraints \(T\).

6. CONCLUSION

A preliminary method for alarm management based on a diagnosis process has been proposed. The proposal is based on a hybrid causal model of the system and a chronicle based approach for diagnosis. An illustrative example of an hydrostatic tank gauging has been considered to introduce the main concepts of the approach. The algorithm HCDAM is a tool for the automatic generation of the chronicles from representative event sequences. Transposing this methodology to large-scale systems would benefit from a decentralized approach in which local chronicles would be learned and then integrated thanks to shared events.

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