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# DyClee-C: a clustering algorithm for categorical data based diagnosis

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## Abstract

In data-based diagnostic applications, large amounts of data are often available but the data remains unlabelled because labelling would require too much time and imply prohibitive costs. The different situations, e.g. normal or faulty, must hence be learned from the data.

Clustering methods, also qualified as unsupervised classification methods, can then be used to create groups of samples according to some similarity criterion. The different groups can supposedly be associated to different situations. Numerous algorithms have been developed in recent years for clustering numeric data but these methods are not applicable to categorical data. However, in many application domains, categorical features are key to properly describe the different situations. This paper presents DyClee-C, an extension of the numeric feature based DyClee algorithm to categorical data. DyClee-C is applied to two data sets: a soybean data set to diagnose the disease soybean plants and a breast cancer data set to assess the current diagnosis in terms of recurrence events and prognose possible relapse.

## 1 Introduction

In the digital age, the amount of data that is recorded by organizations and companies is enormous. If this data is to have added value, it must be possible to extract relevant information automatically. This is why data mining methods appear to be crucial. Among them, clustering methods have an essential role to play. Indeed, data often remains unlabelled because labelling would require too much time and imply prohibitive costs. In diagnostic applications, the different situations, e.g. normal or faulty, must hence be learned from the data. Clustering methods, also qualified as unsupervised classification methods, can then be used to create groups of samples according to some similarity criterion. The different groups can supposedly be associated to different situations.

In the field of clustering, many unsupervised learning algorithms exist. Among the most well-known, we find K-Means [1], [2], DBSCAN [3] and hierarchical ascending classification (HAC) [4]. These algorithms use a numeric distance criterion such as the classical Euclidean distance or the Manhattan distance for high dimensional data sets to determine sample similarity and closest clusters. For this rea-

son, most algorithms are not applicable to categorical data, that is nominal or ordinal qualitative data. However, categorical features are key to properly describe the different situations in many application domains.

As a matter of fact, the metrics quoted above do not make possible to calculate a distance between two samples described by categorical features. Some algorithms have been developed to overcome this problem, such as K-modes [5], ROCK [6] or SQUEEZER [7]. All these algorithms use their own notion of similarity to create clusters.

In this paper, an extension of the DyClee numeric clustering algorithm is proposed [8], [9], [10]. The method, named DyClee-C, applies to categorical data. It must be considered as a building block of the mixed numeric/categorical DyClee version that is under construction. After the presentation of DyClee-C, DyClee-C is applied to two data sets: a soybean data set to diagnose the disease soybean plants and a breast cancer data set to assess the current diagnosis in terms of recurrence events and prognose possible relapse.

The paper is organized as follows. Section 2 presents the basic principles and the different steps of the DyClee algorithm. The categorical extension DyClee-C is introduced in section 3. The tests on the soybean and breast cancer data sets are presented in section 4. Finally, section 5 provides conclusions and perspectives of this work<sup>1</sup>.

## 2 DyClee algorithm

The Dynamic Clustering algorithm for tracking Evolving Environments (DyClee) is an unsupervised learning method. DyClee implements a distance and density based algorithm that features several properties like handling non convex, multi-density clustering with outlier rejection, and it achieves full dynamicity. All these properties are not generally found together in the same algorithm and DyClee hence pushes forward the state of the art in this respect. The first step qualified as *distance-based step* operates at the rate of the data stream and creates micro-clusters putting together data samples that are close in the sense of the L1-norm. Micro-clusters are stored in the form of summarized representations including statistical and temporal information. The second step qualified as *density-based step* uses a density-based approach applied to the micro-clusters to create the final clusters. A cluster is defined as a set of connected micro-clusters where every inside micro-cluster

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<sup>1</sup>This work is part of the CIFRE PhD project n°2017/0047 in collaboration with the company ACTIA. It is also related to the French Occitanie Region project Evolearn.

presents high density and every boundary micro-cluster exhibits either medium or high density. Figure 1 illustrates how the DyClee algorithm works.

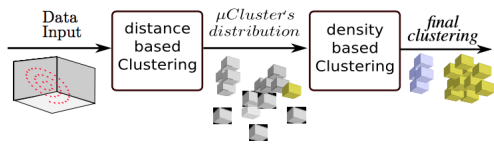


Figure 1: Overview of DyClee

DyClee only handles numeric data sets making use of the KD-Tree algorithm for grouping the micro-cluster at the beginning of the density-based step. However, the KD-tree does not process categorical data. A KD-Tree is a space-partitioning data structure for organizing points in a k-dimensional space [11]. KD-Trees are a useful data structure for several applications, such as nearest neighbor search. The work presented in this paper aims to propose a dynamic clustering approach able to manage categorical data and capture large data dimensions. For this purpose, an alternative to the KD-Tree is proposed and integrated with the DyClee method, thus leading to DyClee-C.

### 3 Categorical extension DyClee-C

The extension to categorical data relies mainly on the removal of micro-clusters and on an alternative solution to KD-Tree for finding neighbors. Indeed, in DyClee, the hypercubes (i.e the micro-clusters) make it possible to represent a similar population. Centers of micro-clusters ( $\mu C$ ) can be calculated by averaging, for each attribute, all the samples present in the  $\mu C$ . In the case of categorical data, we decided to experiment an algorithm that does not make use of the micro-cluster concept. In consequence, the distance-based step of DyClee, during which the samples are assigned to the  $\mu C$ s, is removed and the density-based step directly deals with the samples. In DyClee, clusters are formed by searching in each group found by the KD-Tree, sub-regions of dense and semi-dense micro-clusters. In the DyClee-C extension, they are formed from the results of the Locality Sensitive Hashing (LSH) [12] algorithm, [13], [14]. This method is used in several applications such as clustering, searching for nearest neighbors in large dimensions and the detection of similar images.

The following sections detail the principles of the LSH algorithm, how the clusters are formed and they present several parameters of the method allowing to refine the clustering results.

#### 3.1 Locality Sensitive Hashing algorithm

The LSH algorithm is an appropriate alternative to the KD-Tree since, on the one hand, this algorithm is able to process numerical and categorical data, on the other hand this algorithm is a solution to the problem of the *curse of dimensionality* [15], [16], [17]. LSH makes it possible to reduce the dimensionality of large data sets. LSH refers to a family of hash functions that associate samples in *buckets*: similar samples (in the sense of a matching measure of similarity) are assigned to the same bucket while dissimilar samples are assigned to different bucket. Figure 2 illustrates this method: classic hash functions assign each sample to a different bucket while the hash functions belonging to the

family of hash functions of the LSH assign close samples to the same bucket.

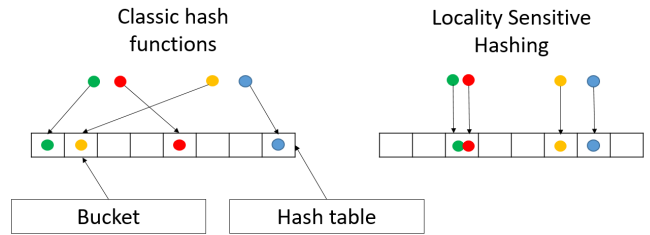


Figure 2: Assignment of samples with hash functions with the LSH

The intuition behind this family of hash functions is that the probability that two samples share the same bucket is related to the distance that separates these two samples. The greater the distance, the lower the probability that the two samples share the same bucket [12]. Definition 3.1 gives the conditions for two samples to share the same bucket.

**Definition 3.1.** A family of hash functions is called  $(d_1, d_2, p_1, p_2)$  - sensitive for all  $x$  and  $y \in S$ , where  $S$  is a set of samples if the two following conditions are fulfilled:

- $d(x,y) \leq d_1 \Rightarrow \Pr_{h \in \mathcal{H}}[h(x) = h(y)] \geq p_1$
- $d(x,y) \geq d_2 \Rightarrow \Pr_{h \in \mathcal{H}}[h(x) = h(y)] \leq p_2$

where  $d(\cdot, \cdot)$  is the distance between two samples with values between 0 and 1,  $h(\cdot)$  is the result of the hash function  $h$  applied to a sample.  $p_1$  and  $p_2$  are probability thresholds for two samples to share the same bucket, with values between 0 and 1.

To find sample's neighbors, all samples that share the same basket as some sample at least once on the  $t$  hash tables are considered neighbors. This technique is used to find groups in DyClee-C. Figure 3 illustrates the search for nearest neighbors for a sample. The neighbors of the sample  $q$  (noted  $q$  for *query point*) are all samples that share the same bucket as the  $q$  point at least once. Here, the neighbors of  $q$  are the red and yellow dots.

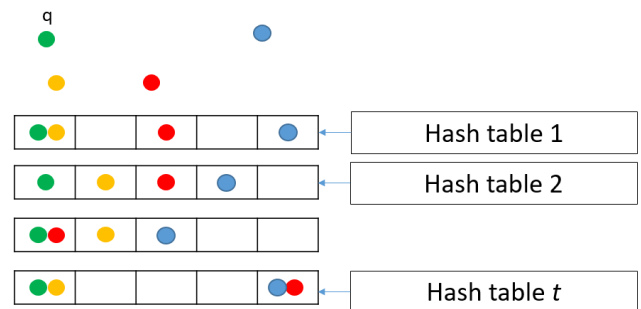


Figure 3: Searching neighbors with the LSH algorithm

#### 3.2 Identification of clusters with DyClee-C

In DyClee, clusters are created from groups of micro-clusters found by the KD-Tree. Let  $M = \{\mu C_1, \dots, \mu C_z,$

...,  $\mu C_k$  }, the set of micro-clusters found with  $\mu C_z$  the  $z$ -th micro-cluster and  $k$  the number of micro-clusters.  $D = \{D_1, \dots, D_z, \dots, D_k\}$  is the set of densities corresponding to micro-clusters with  $D_z$  the density of the  $z$ -th micro-cluster.  $G = \{G_1, \dots, G_z, \dots, G_l\}$  is the set of micro-cluster groups detected by the KD-Tree,  $G_z$  is the  $z$ -th micro-cluster group and  $l$  is the number of micro-cluster groups. Note that the number of micro-clusters  $k$  is generally much bigger than the number of groups of micro-clusters  $l$ . For each group, the densest micro-cluster subregions are searched. A cluster is created if a micro-cluster is dense and if its neighbors are dense or semi-dense inside a group. If a micro-cluster is outlier, all the samples in this micro-cluster are considered noise.

DyClee offers two approaches to find clusters: the global approach and the local approach.

In the **global approach**, a micro-cluster  $\mu C_z$  is said to be dense if  $D_z$  is greater than or equal to the two global density thresholds which are the median and average density of all micro-clusters  $D$ . A micro-cluster  $\mu C_z$  is semi-dense if  $D_z$  is greater than or equal to one of the two global density thresholds. Finally, a micro-cluster  $\mu C_z$  is said to be outlier if  $D_z$  is less than or equal to the two global density thresholds. These conditions are represented by the inequalities (1), (2), (3), where  $median(D_1, \dots, D_k)$  and  $average(D_1, \dots, D_k)$  correspond respectively to the median and average density of micro-clusters in  $M$ .

$$\begin{aligned} \mu C_z \text{dense} &\Leftrightarrow D_z \geq median(D_1, \dots, D_k) \\ &\wedge D_z \geq average(D_1, \dots, D_k) \end{aligned} \quad (1)$$

$$\begin{aligned} \mu C_z \text{semi-dense} &\Leftrightarrow D_z \geq median(D_1, \dots, D_k) \\ &\vee D_z \geq average(D_1, \dots, D_k) \end{aligned} \quad (2)$$

$$\begin{aligned} \mu C_z \text{outlier} &\Leftrightarrow D_z < median(D_1, \dots, D_k) \\ &\wedge D_z < average(D_1, \dots, D_k) \end{aligned} \quad (3)$$

In the case of DyClee-C, as explained previously, the concept of micro-cluster no longer exists. The notion of density of a micro-cluster  $D_z$  is replaced by the number of neighbors of each categorical sample. The neighbor of a sample is spotted by a *connection*. Let  $O = \{O_1, \dots, O_z, \dots, O_n\}$ , the set of samples with  $O_z$ , the  $z$ -th sample of  $O$  and  $n$  the number of samples.  $C = \{C_{O_1}, \dots, C_{O_z}, \dots, C_{O_n}\}$  is the set of connections of all samples with  $C_{O_z}$ , the number of connections of  $O_z$ .  $C_G = \{C_{G_1}, \dots, C_{G_z}, \dots, C_{G_l}\}$  is the set of samples connections for all groups of samples found by the LSH algorithm, with  $C_{G_z}$  the number of connections of samples in the group  $z$  and  $l$  the number of groups of categorical samples found.

As part of the categorical global approach, a sample  $O_z$  is dense if  $C_{O_z}$  is greater than or equal to the global density thresholds which are then the median and average of the number of connections of each sample.  $O_z$  is semi-dense if  $C_{O_z}$  is greater than or equal to the global density thresholds. Finally,  $O_z$  is outlier if  $C_{O_z}$  is less than the global density thresholds. These conditions are represented by the inequalities (4), (5), (6), where  $median(C_{O_1}, \dots, C_{O_k})$  and  $average(C_{O_1}, \dots, C_{O_k})$  correspond respectively to the median and mean of the set of connections of  $C$ .

$$\begin{aligned} O_z \text{dense} &\Leftrightarrow C_{O_z} \geq median(C_{O_1}, \dots, C_{O_k}) \\ &\wedge C_{O_z} \geq average(C_{O_1}, \dots, C_{O_k}) \end{aligned} \quad (4)$$

$$\begin{aligned} O_z \text{semi-dense} &\Leftrightarrow C_{O_z} \geq median(C_{O_1}, \dots, C_{O_k}) \\ &\vee C_{O_z} \geq average(C_{O_1}, \dots, C_{O_k}) \end{aligned} \quad (5)$$

$$\begin{aligned} O_z \text{outlier} &\Leftrightarrow C_{O_z} < median(C_{O_1}, \dots, C_{O_k}) \\ &\wedge C_{O_z} < average(C_{O_1}, \dots, C_{O_k}) \end{aligned} \quad (6)$$

Algorithm 1 implements the creation of clusters with the global approach of DyClee-C. From line 1 to 3, the density thresholds  $median(C_{O_1}, \dots, C_{O_k})$  and  $average(C_{O_1}, \dots, C_{O_k})$  are calculated from the set of connections of all the samples of  $C$ . When a dense sample is detected, his neighbors are searched for and analyzed. If these are dense neighbors of neighbors are sought. If the sample is semi-dense, the sample is added to the cluster but his neighbors are not sought. This approach allows for a cluster with a dense center and semi-dense cluster edges. A cluster is created when no new neighbor is detected. The operation continues with a new sample. Algorithm stops when all the samples have been analyzed (lines 4 to 24).

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#### Algorithm 1 DyClee-C global approach

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**Require:** Set of samples  $O$ , set of connexions of samples  $C$

- 1:  $O_z \rightarrow$  Dense such that  $C_{O_z} \geq median(C_{O_1}, \dots, C_{O_k})$   
 $\wedge C_{O_z} \geq average(C_{O_1}, \dots, C_{O_k})$
- 2:  $O_z \rightarrow$  Semi-dense such that  $C_{O_z} \geq median(C_{O_1}, \dots, C_{O_k}) \vee C_{O_z} \geq average(C_{O_1}, \dots, C_{O_k})$
- 3:  $Clusters = []$
- 4: **while**  $O$  not empty **do**
- 5:    $toAnalyze = []$
- 6:    $cluster = []$
- 7:    $toAnalyze \leftarrow O.pop()$
- 8:   **while**  $toAnalyze$  not empty **do**
- 9:     **for**  $i \in toAnalyze$  **do**
- 10:      **if**  $i \rightarrow$  Dense **then**
- 11:        $Neighbors \leftarrow LSH.query(i)$
- 12:       **for**  $neighbor \in Neighbors$  **do**
- 13:          **if** ( $neighbor$  is Dense  $\wedge neighbor \notin cluster$ ) **then**
- 14:            $cluster.add(neighbor)$
- 15:            $toAnalyze.add(neighbor)$
- 16:          **else if** ( $neighbor$  is Semi-dense  $\wedge neighbor \notin cluster$ ) **then**
- 17:            $cluster.add(neighbor)$
- 18:          **end if**
- 19:       **end for**
- 20:      **end if**
- 21:    **end for**
- 22:    **end while**
- 23:     $Clusters.add(cluster)$
- 24:     $O \leftarrow$  samples that are not in  $Clusters$
- 25: **end while**

---

To illustrate the global approach, two groups found by the *LSH*, are shown in Figure 4. The first categorical group is made up of eight samples  $G_1 =$

$\{1, 2, 3, 4, 5, 6, 7, 8\}$  and the second is composed of six samples  $G_2 = \{9, 10, 11, 12, 13, 14\}$ . The set  $C = \{5, 3, 1, 3, 2, 1, 2, 1, 2, 5, 2, 3, 3, 1\}$  corresponds to the connections of all samples. The overall density thresholds, i.e. the median and the mean of the connections present in  $C$ , are respectively equal to  $median(C_{O_1}, \dots, C_{O_k}) = 2$  and  $average(C_{O_1}, \dots, C_{O_k}) = 2.43$ . A cluster is composed of dense samples in the center and semi-dense samples at the cluster boundaries.

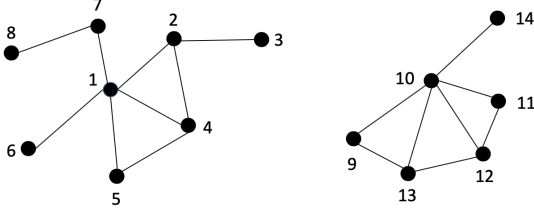


Figure 4: Example of groups of categorical samples detected by the LSH algorithm

For the group  $C_{G_1}$ , the dense samples are  $Dense_{C_{G_1}} = \{1, 2, 4\}$  and the semi-dense samples are  $Semi-dense_{C_{G_1}} = \{5, 7\}$ . Samples 1, 2, and 4 are dense because their number of  $C_{O_1}$ ,  $C_{O_2}$ , and  $C_{O_4}$  connections are greater than or equal to the overall density thresholds. Samples 5 and 7 are semi-dense because their number of connections  $C_{O_5}$  and  $C_{O_7}$  is greater than or equal to one of the global density thresholds. Samples 3, 6, and 8 are outliers because their number of  $C_{O_3}$ ,  $C_{O_6}$ , and  $C_{O_8}$  connections are less than the overall density thresholds. The same reasoning is applied for the second group. The resulting clusters are  $Cl_1 = \{1, 2, 4, 5, 7\}$  and  $Cl_2 = \{9, 10, 11, 12, 13\}$ . The clusters found by applying the global approach are shown in Figure 5.

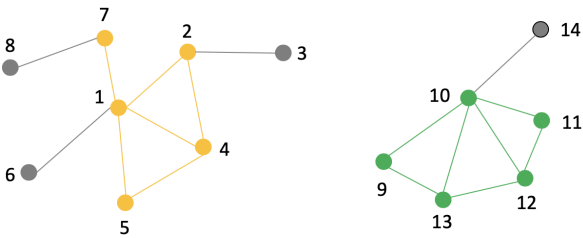


Figure 5: Clusters found by applying the global approach

In the **local approach** of DyClee, the density of a  $D_z$  micro-cluster is no longer compared to the median and mean density of all  $\mu C_z$  micro-clusters, but to the median density and average of the micro-clusters of the group in which  $\mu C_z$  belongs. Let  $D_G = \{D_{G_1}, \dots, D_{G_z}, \dots, D_{G_l}\}$ , all the densities of the groups found by the KD-Tree,  $D_{G_z}$ , the densities of the micro-clusters present in the group  $G_z$  and  $l$  the number of groups of micro-clusters.  $\mu C_z$  is dense if  $D_z$  is greater than or equal to the local density thresholds, i.e. the median and mean density of the micro-clusters

of the group  $D_{G_z}$  in which  $\mu C_z$  is included.  $\mu C_z$  is semi-dense if  $D_z$  is greater than or equal to one of the local density thresholds. Finally,  $\mu C_z$  is outlier if  $D_z$  is strictly less than the local density thresholds. These conditions are represented by the inequalities (7), (8), (9), where  $median(D_{G_z})$  and  $average(D_{G_z})$  correspond respectively to the median and mean density of micro-clusters belonging to the group  $G_z$ .

$$\begin{aligned} \mu D_z \text{ dense} &\Leftrightarrow D_z \geq median(D_{G_z}) \\ &\wedge D_z \geq average(D_{G_z}) \end{aligned} \quad (7)$$

$$\begin{aligned} \mu D_z \text{ semi-dense} &\Leftrightarrow D_z \geq median(D_{G_z}) \\ &\vee D_z \geq average(D_{G_z}) \end{aligned} \quad (8)$$

$$\begin{aligned} \mu D_z \text{ outlier} &\Leftrightarrow D_z < median(D_{G_z}) \\ &\wedge D_z < average(D_{G_z}) \end{aligned} \quad (9)$$

In DyClee-C, the principle of creating clusters by local approach is unchanged but instead of comparing a sample's connections to the median and the average of the connections of all samples  $O$ ,  $C_{O_z}$  is compared to the connection thresholds calculated from the median and the average of the connections of samples in the  $C_{G_z}$  group. The conditions for a sample to be dense, semi-dense and outlier are given by inequalities (10), (11) and (12). The pseudo code associated with the local approach is given by Algorithm 2.

$$\begin{aligned} O_z \text{ dense} &\Leftrightarrow C_{O_z} \geq median(C_{G_z}) \\ &\wedge C_{O_z} \geq average(C_{G_z}) \end{aligned} \quad (10)$$

$$\begin{aligned} O_z \text{ semi-dense} &\Leftrightarrow C_{O_z} \geq median(C_{G_z}) \\ &\vee C_{O_z} \geq average(C_{G_z}) \end{aligned} \quad (11)$$

$$\begin{aligned} O_z \text{ outlier} &\Leftrightarrow C_{O_z} < median(C_{G_z}) \\ &\wedge C_{O_z} < average(C_{G_z}) \end{aligned} \quad (12)$$

To illustrate this approach, the example of Figure 6 is used. The density thresholds change in relation to the overall approach. Each group has its own density thresholds. Group 1 composed of  $G_1 = \{1, 2, 3, 4, 5, 5, 6, 7, 8\}$  has for  $median(D_{G_1}) = 2$  and  $average(D_{G_1}) = 2.25$  and group 2 composed of  $G_2 = \{9, 10, 11, 12, 12, 13, 14\}$  has for  $median(D_{G_2}) = 2.5$  and  $average(D_{G_2}) = 2.75$ . The  $Cl_1$  cluster remains unchanged from the overall approach. Concerning the  $Cl_2$  cluster, samples 9 and 11 are added to sample 14 and are also considered outliers because  $C_{O_9}$  and  $C_{O_{11}}$  are less than  $median(D_{G_2})$  and  $average(D_{G_2})$ . The  $Cl_2$  cluster is therefore composed of  $Cl_2 = \{10, 12, 13\}$ . Figure 6 illustrates the clusters found by applying the local approach.

The methods for generating clusters in DyClee-C have been detailed in the previous section. Several parameters allow the user to improve clustering results by adding some knowledge to the data. These parameters are detailed below.

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**Algorithm 2** DyClee-C local approach
 

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**Require:** Set of samples  $O$ , set of connexions of samples  $C$ , Set of groups of samples  $C_G$

- 1:  $O_z \rightarrow$  Dense such that  $C_{Oz} \geq \text{median}(C_{Gz}) \wedge C_{Oz} \geq \text{average}(C_{Gz})$
- 2:  $O_z \rightarrow$  Semi – dense such that  $C_{Oz} \geq \text{median}(C_{Gz}) \vee C_{Oz} \geq \text{average}(C_{Gz})$
- 3:  $Clusters = []$
- 4: **while**  $O$  not empty **do**
- 5:    $toAnalyze = []$
- 6:    $cluster = []$
- 7:    $toAnalyze \leftarrow O.pop()$
- 8:   **while**  $toAnalyze$  not empty **do**
- 9:     **for**  $i \in toAnalyze$  **do**
- 10:      **if**  $i \rightarrow$  Dense **then**
- 11:        $Neighbors \leftarrow LSH.query(i)$
- 12:       **for**  $neighbor \in Neighbors$  **do**
- 13:         **if** ( $neighbor$  is Dense  $\wedge$   $neighbor \notin cluster$ ) **then**
- 14:           $cluster.add(neighbor)$
- 15:           $toAnalyze.add(neighbor)$
- 16:         **else if** ( $neighbor$  is Semi – dense  $\wedge$   $neighbor \notin cluster$ ) **then**
- 17:           $cluster.add(neighbor)$
- 18:         **end if**
- 19:       **end for**
- 20:     **end if**
- 21:   **end for**
- 22:   **end while**
- 23:    $Clusters.add(cluster)$
- 24:    $O \leftarrow$  samples that are not in  $Clusters$
- 25: **end while**

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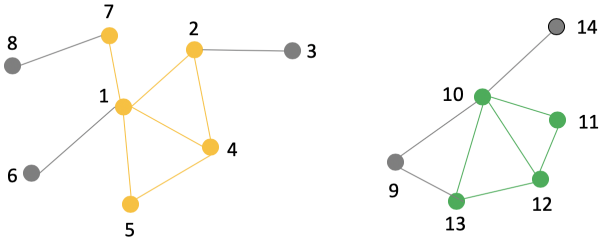


Figure 6: Clusters found by applying the local approach

### 3.3 Settings of Dyclee-C

The final clusters are found using one of the two approaches described in the previous section. These results can be refined with optional parameters. In this section, three parameters are described. The first is called *Unclassified\_accepted*, the second is called *minimum\_samples* and the last parameter presented is called *n\_clusters*. These parameters are tuned in function of the problem encountered and evaluated with cluster validity methods [18] like those they are presented in section 4.

In DyClee, clusters are composed of dense (center) and semi-dense (edge of the cluster) micro-clusters. Outliers are considered unrepresentative and their samples are rejected (considered noise). Depending on the context, it may be interesting not to consider outliers but, on the contrary,

to assign all the data to a cluster. When the parameter *Unclassified\_accepted* is activated, all the samples must be assigned to a cluster, i.e. there is no outlier rejection.

The second parameter is called *minimum\_samples* and allows you to set the minimum number of samples that a cluster must contain to be considered as a final cluster. Indeed, depending on the application, small clusters may not be representative. In the case where a nominal situation has to be analysed, small clusters can represent abnormal situations. These clusters are no longer considered as final clusters and the samples assigned to them are marked as noise. The equation (13) allows you to set the size that clusters must have to be considered as final clusters.

$$|Cl_z| > \frac{\sum_{i=0}^l |Cl_i|}{|Cl|} \quad (13)$$

with  $|Cl_z|$  the size of the cluster  $z$  to be evaluated and  $|Cl|$  is the number of cluster groups.

The use of the parameter is illustrated in Figure 7 with three clusters  $Cl = \{Cl_1, Cl_2, Cl_3\}$ . Cluster 1 is given by  $Cl_1 = \{1, 2, 3, 4, 5, 6, 7, 8\}$ , cluster 2 by  $Cl_2 = \{9, 10, 11, 12, 13, 14\}$  and the third by  $Cl_3 = \{15, 16, 17\}$ . To be considered as final clusters, all  $Cl$  clusters must have a size greater than the threshold defined in the equation (14):

$$Threshold = \frac{|Cl_1| + |Cl_2| + |Cl_3|}{|Cl|} = \frac{8 + 6 + 3}{3} = 5,67 \quad (14)$$

The  $Cl_1$  and  $Cl_2$  clusters are larger than 5.67 (respectively 8 and 6) and are therefore considered final clusters. On the other hand, since the  $Cl_3$  cluster has a size equal to 3, the samples that compose it (15, 16 and 17) are considered as noise (in the Figure 7 in grey).

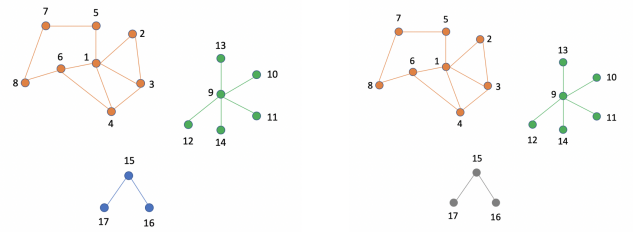


Figure 7: Left: parameter *minimum\_samples* disabled. Right: parameter *minimum\_samples* enabled

The last parameter is called *n\_clusters* and allows you to consider the most important  $n$  clusters as final clusters. Samples belonging to the remaining clusters are assigned to the final  $n$  clusters. Let be  $A = \{A_1, \dots, A_i, \dots, A_m\}$ , all the categorical attributes of the set of samples  $O$ , with  $m$  the number of attributes.  $c = \{c_1, \dots, c_z, \dots, c_l\}$  is the set of cluster centers  $Cl$  with  $c_z$  the cluster center  $Cl_z$ . A  $c_z$  center is defined by  $c_z = \{c_{z1}, \dots, c_{zi}, \dots, c_{zm}\}$  with  $c_{zi}$ , the  $i$ -th component of the  $z$  center. The terms of an attribute  $A_i$  are noted  $Mod(A_i) = \{m_{i1}, \dots, m_{ij}, \dots, m_{ip}\}$  with  $m_{ij}$ , the  $j$ -th term of the attribute  $A_i$  and  $p$ , the number of terms of

the attribute  $A_i$ . The frequency of a modality  $m_{ij}$  is noted  $fr(m_{ij})$ . The  $i$  component of the  $c_z$  center is defined as the most frequent modality of the  $A_i$  attribute (see equation (15)).

$$c_{zi} = \max(fr(m_{i1}), \dots, fr(m_{ij}), \dots, fr(m_{ip})). \quad (15)$$

When the  $n\_clusters$  parameter is active, the distance between samples not in the final  $n$  clusters is calculated and samples are assigned to the nearest center. Figure 8 takes the example of Figure 7. In this example, the two most important clusters are considered as final clusters ( $Cl_1$  and  $Cl_2$ ). Samples 15, 16 and 17 of  $Cl_3$  are reassigned to the nearest clusters. Samples 15 and 17 are therefore assigned to the  $Cl_1$  cluster and sample 16 to the  $Cl_2$  cluster.

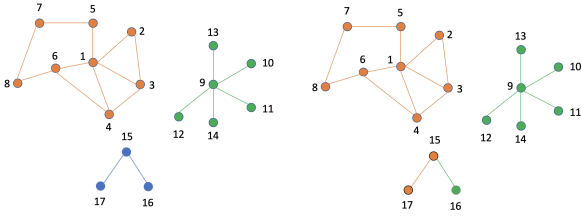


Figure 8: Left: parameter  $n\_clusters$  disabled. Right: parameter  $n\_clusters$  enabled with  $n = 2$

The section 4 presents the different tests performed on the DyClee-C.

## 4 Evaluation

DyClee-C was tested on well-known UCI Machine Learning data sets in the clustering domain like *Zoo*, *Congressional Voting Records*, *Soybean* and *Breast Cancer*. The two latter data sets have been selected to be reported in this paper because they correspond to a diagnosis problem. As they have a large number of dimensions, it allows to test how DyClee-C handles data sets with many categorical attributes. DyClee-C was compared to the K-modes clustering algorithm [5]. Note that an initialization method for the centers of clusters that is not present in the Huang paper is also tested. Indeed, this new method was introduced by [19] 11 years after the original paper. Training phases have been realized on a part of the data sets to find correct combinations of parameters. To evaluate clusters, three validity measures are used: the *purity*, *recall* and the *precision*. Purity is the ratio between the sum of the number of elements correctly assigned in each class  $i$  (noted  $TP_i$ ) and the number of samples in the data set. This measure is described in the equation (16) where  $TP_i$  is the real positive rate of the  $i^{th}$  class,  $k$  is the number of classes and  $N$  is the number of samples in the data set.

$$Purity = \frac{\sum_{i=0}^k TP_i}{N} \quad (16)$$

The recall corresponds to the ratio between the number of elements correctly assigned to the  $i^{th}$  class and the number of elements belonging to the  $i^{th}$  class (noted  $TP_i + FN_i$ ). This measure is described in the equation (17) with  $R_i$ , the

recall of the  $i^{th}$  class,  $TP_i$ , the real positive rate in the  $i^{th}$  class and  $FN_i$  class, the false negative rate in the  $i^{th}$  class. A false negative is a result where the model incorrectly predicts the negative class.

$$R_i = \frac{TP_i}{TP_i + FN_i} \quad (17)$$

The last measure is the precision which corresponds to the ratio between the number of elements correctly assigned to the  $i^{th}$  class and the number of elements assigned to the  $i^{th}$  class (noted  $TP_i + FP_i$ ). This measure is described in the equation (18), with  $P_i$ , the accuracy of the  $i^{th}$ ,  $TP_i$  class, the true positive rate for the  $i^{th}$  and  $FP_i$  class, the false positive rate for the  $i^{th}$  class. A false positive is a result where the model incorrectly predicts the positive class.

$$P_i = \frac{TP_i}{TP_i + FP_i} \quad (18)$$

### 4.1 Soybean data set

The first data set is the "Soybean" [20]. This data set consists of 47 soybean plants with 35 categorical attributes and 4 classes. Attributes correspond to the characteristics of the plant (size of the seed, leaves,...). The classes correspond to diseases specific to soybean plants. Two tests with two different settings were performed on this data set. The first one was done with the parameter *Unclassed\_accepted* enabled. The parameter of K-Modes corresponding to the number of clusters is  $k\_clusters = 4$ . Original classes of the "Soybean" data set, results of DyClee-C and K-Modes algorithms with both initializations [5], [19] are shown in Table 1.

	$C_1$	$C_2$	$C_3$	$C_4$
Soybean	17	10	10	10
DyClee-C	26	10	10	1
K-Modes (Huang)	16	14	10	7
K-Modes (Cao)	<b>17</b>	<b>10</b>	<b>10</b>	<b>10</b>

Table 1: Clusters found by DyClee-C and K-Modes for the Soybean data set

Results in Table 1 show that classes  $C_2$  and  $C_3$  were perfectly detected by both algorithms tested. However, the  $C_1$  and  $C_4$  clusters were poorly formed by DyClee-C while K-Modes found the right classes. The reason behind the DyClee-C misclassification is that DyClee-C do not compute the distance between every samples. Indeed, the Locality Sensitive Hashing consider as nearest neighbors samples that share the same bucket at least once (section 3.1). As K-Modes method measures the dissimilarity between the whole data set, the Huang's algorithm is more precise. Moreover, K-Modes method needs the number of clusters as a parameter. As an unsupervised clustering algorithm, this kind of information is normally not known in advance. Purity, recall and precision measures for DyClee-C and K-Modes algorithms are shown in Table 2.

	Purity	Recall	Precision
DyClee-C	70%	77%	85%
K-Modes (Huang)	78%	55%	52%
K-Modes (Cao)	<b>100%</b>	<b>100%</b>	<b>100%</b>

Table 2: Purity, recall and precision scores of DyClee-C and K-Modes algorithm for the Soybean data set

As K-Modes method found correct classes, purity, recall and precision measures corresponding are equal to 100%. The second test highlights outliers and their influence on DyClee-C's results. Parameters enabled for this test are *Unclassed\_accepted* and *minimum\_samples*. The latter makes it possible to eliminate samples belonging to clusters with a size smaller than the average cluster size.

	$C_1$	$C_2$	$C_3$	$C_4$
Soybean	10	9	9	6
Result	10	9	9	6

Table 3: Clusters found by DyClee-C for the Soybean data set with outliers removed

Table 3 represents the classes of the "Soybean" data set and the clusters found by DyClee-C when the outliers detected by the parameter *minimum\_samples* are not taken into account. The results show that in this configuration, all classes were found by DyClee-C. The three validity measures associated to this result are equal to 100%.

## 4.2 Breast Cancer data set

The second data set is the "Breast Cancer" [21]. This data set consists of 286 instances and 9 categorical attributes and 2 classes. An instance corresponds to a patient and each attribute is an information about the patient and his pathology (age, which breast has the tumor, the degree of the malignancy,...). Some attributes have missing values and are represented by a "?" in the data set. These special values are considered as a modality for the test. Classes are instances which have a no recurrence events and recurrence events. Parameters enabled of DyClee-C for this test are *Unclassed\_accepted* and  $n\_clusters = 2$ . The parameter of K-Modes corresponding to the number of clusters is  $k\_clusters = 2$ . Original classes of the "Breast Cancer" data set, results of DyClee-C and K-Modes (with both initializations) are shown in Table 4.

	$C_1$	$C_2$
Breast Cancer	201	85
DyClee-C	<b>207</b>	<b>79</b>
K-Modes (Huang)	149	137
K-Modes (Cao)	183	103

Table 4: Clusters found by DyClee-C and K-Modes for the Breast Cancer data set

DyClee-C have detected better groups than the K-Modes algorithm. Few samples have been misclassified by DyClee-C while they are more samples in the wrong class with the K-Modes algorithm. Purity, recall and precision measures for DyClee-C and K-Modes algorithms are shown in Table 5.

	Purity	Recall	Precision
DyClee-C	<b>72%</b>	<b>63%</b>	<b>63%</b>
K-Modes (Huang)	70%	45%	45%
K-Modes (Cao)	70%	53%	52%

Table 5: Purity, recall and precision scores of DyClee-C and K-Modes algorithm for the Breast Cancer data set

While purity score is slightly higher for DyClee-C than K-Modes, the method presented in this paper is clearly better for recall and precision score than the Huang's algorithm.

## 5 Conclusions and perspectives

In this article, an extension of DyClee, a dynamic clustering algorithm for digital data, is presented. This extension, called DyClee-C, allows you to apply the basic concepts of DyClee to categorical data. The KD-Tree has been replaced by the LSH algorithm, which makes it possible to form groups of categorical samples with large dimensions. The two approaches, global and local density, to generate clusters have been modified to capture categorical data. The concept of micro-cluster density is replaced by the number of neighbours of a sample, i.e. connections. Thus, a sample with a certain number of connections is more dense than a sample with few connections. Three parameters have been adapted in order to refine the clusters obtained. The first one allows you to have no noise, the second one only keeps clusters with a size larger than the average cluster size and the last one allows you to consider the most important  $n$  clusters as final clusters.

For the tests, DyClee-C has been compared to the K-Modes algorithm on two well-known data sets. The *Breast Cancer* data set shows that DyClee-C is able to detect classes even if the samples have missing modalities. The *Soybean* data sets illustrates the capacity of DyClee-C to detect outliers. The obtained results are promising and show that clustering can be used for diagnosis purposes even for data bases with categorical features. However, as classes were known in advance, results are biased. Indeed, an unsupervised classification algorithm is applied to a dataset which labels are not known. Subsequently, further tests and comparisons with other algorithms are to be carried out.

In the future, we plan to develop a mixed version of DyClee to manage both numerical and categorical data.

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