

SOFI: Finding point group symmetries in atomic clusters as finding the set of degenerate solutions in a shape-matching problem

M. Gunde, N. Salles, L. Grisanti, L. Martin-Samos, Anne Hémeryck

▶ To cite this version:

M. Gunde, N. Salles, L. Grisanti, L. Martin-Samos, Anne Hémeryck. SOFI: Finding point group symmetries in atomic clusters as finding the set of degenerate solutions in a shape-matching problem. The Journal of Chemical Physics, 2024, 161 (6), 10.1063/5.0215689. hal-04677499

HAL Id: hal-04677499 https://laas.hal.science/hal-04677499

Submitted on 26 Aug 2024

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

SOFI: Finding point group symmetries in atomic clusters as finding the set of degenerate solutions in a shape-matching problem

M. Gunde,^{1, a)} N. Salles,² L. Grisanti,^{1, 2} L. Martin-Samos,² and A. Hemeryck³

¹⁾Institute Ruđer Bošković, Bijenička 54, 10000 Zagreb, Croatia

²⁾ CNR-IOM/Democritos National Simulation Center, Istituto Officina dei Materiali, c/o SISSA, via Bonomea 265, IT-34136 Trieste, Italy

³⁾LAAS-CNRS, Université de Toulouse, CNRS, 7 avenue du Colonel Roche, 31000 Toulouse, France

Point Group (PG) symmetries play a fundamental role in many aspects of theoretical chemistry and computational materials science. With the objective to automatize the search of PG symmetry operations of generic atomic clusters, we present a new algorithm called Symmetry Operation FInder (SOFI). SOFI addresses the problem of identifying PG symmetry by framing it as a degenerate shape-matching problem, where the multiple solutions correspond to distinct symmetry operations. The developed algorithm is compared against three other algorithms dedicated to PG identification, on a large set of atomic clusters. The results, along with some illustrative use cases, showcase the effectiveness of SOFI. The SOFI algorithm is released as part of the IRA library, accessible at https://github.com/mammasmias/IterativeRotationsAssignments.

I. INTRODUCTION

In the rise of quantum-chemistry and first-principle methods, the identification of Point Group (PG) symmetry has been a necessary step to effectively downsize the numerical problem and reduce the cost of simulations. Besides the computational accelerations made possible by exploiting the symmetry, the presence and identification of a PG symmetry in a molecule, or rather a cluster, or a defect, can be used to address the fundamental properties of its electronic ground, and excited states¹. Assigning symmetry label to each state (i.e. vibrational or electronic), is desirable to connect to group theory, which is the formal context where PG symmetries are described. If the symmetry is assigned to all relevant quantum (eigen)states, group theory can be applied to specific quantum-mechanical operators to understand which matrix elements are expected to vanish based on symmetry rules. This is extremely useful for example in molecular spectroscopy: depending on the operator governing the interaction term, the symmetry-based selection rules will provide information on which transitions will actually be $forbidden^{2,3}$.

As the identification of PG symmetry is not a new problem, the computational community has made numerous attempts to automatize it. Typically, quantum chemistry software and some molecular builders/editors include capabilities related to the symmetries of the system (i.e. automatic identification, symmetrization of structure). The algorithmic approaches to identify the PG may vary based on how the atomic structures are handled, and the way symmetry elements are utilised/exploited within the software framework. Despite the fundamental nature of PG symmetries and the broad use of related algorithms, there seem to be relatively few standalone libraries devoted to their identification. Moreover, it is often very difficult to trace which PG identification algorithm (and/or library) is integrated into the larger software environment, as the information is often poorly, or not at all documented. Many wellknown quantum chemistry packages already date back to several years ago, when the modularity in programming was not necessarily a priority, so each developing group has created an "ad-hoc" method plugged into the code, often poorly updated through the years. For example by inspecting NW chem source ${\rm code}^4$ one can find a collection of old Fortran routines apparently written in the 90s, used for identifying symmetries. Besides, proprietary codes do not necessarily share information about their algorithm choice, even if some initiatives are more transparent, for example the IQmol builder⁵, which uses, and references the SymMol⁶ algorithm in its documentation.

In the subsequent paragraph we highlight a handful of approaches for the identification of PG symmetry, which have been devised as standalone algorithms/libraries, with some of them presently integrated into larger quantum chemistry codes, and/or computational "toolboxes".

The PG symmetry of a structure can be identified in several ways. A relatively common strategy, used in several available approaches, is to first find the principal axis of symmetry, and then test for possible operations along other axes in relation to the principal axis. The principal axes could be identified straight-forwardly by relying on the properties of the principal moments and axes of the inertia tensor, as done in SymMol⁶, and Symmetrizer⁷ software. Relying on the inertia tensor can however be problematic, since its principal axes can be ambiguous in some specific cases (spheroidal shapes). Alternatively, certain properties of the atomic structure itself (atomic positions, midpoints between atoms, etc.) can be used to identify the axes of symmetry, such as employed in SYMMAPS⁸, and SYVA⁹ software. Another idea is to partition the atomic structure into sets of symmetryequivalent atoms, and search for symmetries within those

^{a)}Electronic mail: miha.gunde@gmail.com

sets. The partitioning can be done through the inspection of the distance matrix of the structure, such as in libmsym¹⁰, while the search for symmetries is conducted based on the properties of the inertia tensor of each equivalence set¹¹, and the PG of the entire structure is the subset of the symmetry operations common to all partitions. Some approaches based on arguments from graph theory also exist^{12,13}.

It is also common for PG-identification software to implement some other capabilities, such as precise symmetrization of structures^{7,9}, or similar, which can be thought of as extensions to the fundamental task of identifying the PG symmetry elements of a structure.

In the interest of our discussion and the algorithm we propose, we now briefly recall some fundamental notions of PG symmetry. If $\boldsymbol{\theta}$ is a specific symmetry operation, which is an element of the PG of an atomic structure A, the equation:

$$A' \leftarrow \boldsymbol{\theta} A,\tag{1}$$

represents the application of symmetry operation θ on structure A, which results in a symmetry-transformed structure A'. By definition of symmetry operations, Aand A' are equivalent up to a permutation of atomic indices P_A :

$$A' = P_A A,\tag{2}$$

where P_A is a permutation matrix, which is unique for a given operation θ . Then, the relation:

$$P_A A = \boldsymbol{\theta} A. \tag{3}$$

holds for any and every symmetry operation $\boldsymbol{\theta}$ of the structure A. Each element (symmetry operation) of the PG of structure A corresponds to a unique solution of Eq. (3), in the form of a pair $\{\boldsymbol{\theta}, P_A\}$.

It can be observed that the Eq. (3) is equivalent to the shape matching problem of two exactly congruent (equivalent) structures A and B, as:

$$P_B B = \mathbf{R} A + \mathbf{t},\tag{4}$$

where **R** is an orthonormal transformation matrix, and **t** is a translation vector. By comparing Eq. (3) to Eq. (4), we see that **R** is replaced by a symmetry operation $\boldsymbol{\theta}$, and the translation **t** vanishes. When solving the general shape matching problem of Eq. (4), only one solution (the optimal one) is sought, whereas in the case of PG identification in Eq. (3), the set of all degenerate solutions represents the set of all possible symmetry operations of structure A. Finding the PG of a structure can therefore be addressed as a "degenerate" shape matching problem.

In practice, the "degeneracy" of these solutions is never exact, due to numerical limitations, or distortions in the atomic positions within the structure. An interpretation of "degeneracy" is thus needed, in terms of a threshold, such that all solutions within a given threshold are considered equivalent, degenerate. By the tuning of such

In this work, we present the Symmetry Operation FInder (SOFI) algorithm, and its implementation as a standalone library, aimed at solving the general problem of PG symmetry identification, in a way that is independent of specific properties of the atomic structure. SOFI finds the PG symmetry operations in the form of 3×3 matrices, and the corresponding permutations of atomic indices. The working principle of SOFI is fundamentally based on ideas and arguments of the shape-matching algorithm IRA^{14,15}. In contrast to other algorithms from the literature mentioned earlier, SOFI does not attempt to identify any special axes of symmetry, but is instead focused directly on generating the possible symmetry operations along any axis. SOFI takes as input an atomic structure, and returns the list of symmetry operation matrices, written in the specific form of the original reference frame, in which the structure was input/written. As such, the matrices can directly be used without any post processing. From this point of view, SOFI is a solver for symmetry elements, that does not modify the input structure in any way. In order to determine the PG of a structure, a separate routine is called, taking as input the list of symmetry operation matrices. Within this routine, each symmetry operation is first associated to the axis it acts on, and labelled according to the Schoenflies notation³. The PG is then deduced by inspection of the symmetry elements, following a standard flowchart. The search for non-exact symmetries in SOFI can be tuned via a threshold parameter, whose value is directly linked to the distortions in the atomic positions of the structure. Moreover, in case of an incomplete list of elements of a PG, basic arguments of group theory can be used to find the missing elements. An incomplete list of symmetry elements can be an indicator of broken symmetries in the system, which might happen when the atomic positions get distorted in a particular way. Due to the modularity of the algorithm implementation, external conditions acting on symmetry elements can easily be implemented through custom functions. As an example of such function, the action of an external arbitrary-direction magnetic field on the PG of a structure¹⁶ is included in the code. SOFI is written in Fortran, with a C-bound Application Programming Interface (API), making it a directly interoperable library. It can be used on its own, or easily inserted into other software.

Section II describes the details of our SOFI algorithm, and the Section III gives the implementation details. In the Section IV, SOFI algorithm is compared to three other algorithms for PG symmetry identification, namely SYVA⁹, SymMol⁶, and libmsym¹⁰. The discussion in Section V provides some possibly valuable insight into technical details of the algorithm, and the limits and tuning of its maximal "resolving" power. The Section VI gives some exemplary use cases of the SOFI algorithm, and its output. Further examples can be found in the online documentation.

II. THE ALGORITHM

We approach the problem of finding PG symmetries by solving the degenerate shape-matching problem of Eq. (3), but firstly we need to address the question of the origin point.

A fixed point is a point in space which remains unchanged under transformation by an arbitrary set of orthonormal matrices. When an atomic structure is transformed by symmetry operations belonging to some PG, we can observe one or more such fixed points. The points that remain fixed under transformation by all symmetry elements of the PG are the origin points of the entire PG, while points that are fixed only for a subset of the symmetry elements are origin points of the subgroups associated to that PG. For example, the Oh PG has six C4v subgroups oriented in three different directions, each with a different origin point, while in the case of C-groups, all points along the primary rotation axis are fixed. However, the only point of a generic structure, which is guaranteed to always remain fixed under transformation by any orthonormal matrix or symmetry element, is the geometric center (center of geometry, arithmetic mean, centroid). Therefore, picking the geometric center of a structure as the origin point, guarantees that the algorithm will parse the full PG of the structure. Indeed, most of the available algorithms assume this choice by default. However, alternative origin points are possible. For example when searching for symmetry operations about a given atom, the origin point should be the position of that specific atom (or some other specific point of choice). SOFI is agnostic to the choice of origin, which means it will find symmetry operations about the given point. This also means the origin has to be chosen from the outside (by the user, or another application).

After the origin point has been selected and the structure shifted accordingly, the atomic structure enters the main search loop of the SOFI algorithm. The key idea of SOFI is to parse the space of orthonormal transformations, at each step construct a trial transformation, evaluate Eq. (3) with the trial transformation, and keep track of all favourable solutions. Thus, the algorithm needs two main components, as follows.

The first component is a function which will evaluate Eq. (3). The idea employed in SOFI is to transform Eq. (3) into a distance $d(P_A A, \theta A)$, which should be equal to zero when P_A and θ correspond to a solution of Eq. (3), and greater than zero otherwise. In order to compute the distance $d(P_A A, \theta A)$, we employ the Hausdorff distance function^{14,15,17} with the generic form:

$$d_H(A,B) = \max_{a \in A} \min_{b \in B} d(a,b) \tag{5}$$

where A and B are structures with atomic vectors $a \in A$, $b \in B$, and d(a, b) is a Cartesian distance. The Hausdorff distance is invariant to permutations, and variant to other rigid transformations of either structure (rotation, reflection, translation). The evaluation of Eq. (3) is thus done by computing Eq. (6).

$$d(P_A A, \boldsymbol{\theta} A) = d_H(A, \boldsymbol{\theta} A) \tag{6}$$

If $\boldsymbol{\theta}$ is a solution of Eq. (3), then $d_H(A, \boldsymbol{\theta}A) = 0$. In order to compute d_H in SOFI, we use the CShDA algorithm, introduced in Ref.¹⁴. CShDA imposes a one-to-one assignment constraint on the atoms, and returns the permutation P_A and distance d_H .

The second component of the algorithm is a way of parsing the space of orthonormal transformations (3×3) orthonormal matrices θ). This parsing should be computationally efficient, but still broad enough to identify all possible solutions of Eq. (3). In SOFI, we define the parsing of transformation space in a similar way as in IRA¹⁴, in which the orthonormal transformations (bases) are constructed directly from atomic vectors present in the structure. It follows from Eq. (3), that for each atom $i \in A$ with the atomic position a_i , there exists a unique atom $j \in A$ with the atomic position a_j , such that:

$$a_i = \boldsymbol{\theta} a_j. \tag{7}$$

The Eq. (7) can be seen as operation of change of basis, from the basis β defined by a_i , to basis γ defined by a_j , written:

$$\boldsymbol{\beta}a_i = \boldsymbol{\gamma}a_j, \tag{8}$$

from which we see that

$$\boldsymbol{\theta} = \boldsymbol{\beta}^T \boldsymbol{\gamma}. \tag{9}$$

Therefore, the operation $\boldsymbol{\theta}$ is completely defined by two orthonormal bases, namely $\boldsymbol{\beta}$ and $\boldsymbol{\gamma}$, which are defined by atomic positions a_i and a_j , respectively.

However, an orthonormal basis set in 3D cannot be uniquely defined from a single 3D vector. This problem is resolved by adding another atomic vector $a_{i'}$ to the definition of the basis, as follows. The first basis vector \hat{e}_1 is the normalised atomic vector a_i , the second basis vector \hat{e}_2 is the component of the atomic vector $a_{i'}$ orthonormal to \hat{e}_1 , and the third basis vector is a cross product $\hat{e}_3 = \hat{e}_1 \times \hat{e}_2$. In this way, the basis β is defined by positions of atoms *i* and *i'*, and the basis γ by positions of atoms *j* and *j'*. Due to this, SOFI is restricted to structures containing at least 3 non-collinear atoms. The same procedure for constructing an orthonormal basis is used in IRA¹⁴.

According to the preceding considerations, in order to identify any symmetry operation $\boldsymbol{\theta}$, we need to find the quadruplet of atoms $\{i, i', j, j'\}$, which construct $\boldsymbol{\theta}$ by Eq. (9), such that Eq. (3) is satisfied. In order to find all possible solutions of Eq. (3), we need in turn to list all unique matrices $\boldsymbol{\theta}$ that can be constructed by such quadruplets of atoms, while also satisfying $d_H(A, \boldsymbol{\theta} A) =$ 0 by Eq. (5). The most naive algorithm to find all symmetry operations $\boldsymbol{\theta}$ is then to brute-force search over all combinations of quadruplets of atoms in A, which give $d_H = 0$. Such algorithm is constructed by four nested DO loops over all atoms, meaning an $\mathcal{O}(N^4)$ complexity, where N is the number of atoms in the structure. We can however quickly observe that such approach contains a huge degree of redundancy, which can be greatly reduced, or even avoided, by applying the following considerations.

A. Reduce complexity I: fix one basis

The Eq. (7) holds true for a given $\boldsymbol{\theta}$, for all atoms *i* simultaneously. Therefore, instead of looping over all *i*, i', j, and j', we can simply select any two different atoms *i* and *i'*, and loop over only *j* and *j'*. The atoms *i* and *i'* construct the basis $\boldsymbol{\beta}$, which is kept fixed throughout the search, while the basis $\boldsymbol{\gamma}$ constructed by atoms *j* and *j'* keeps changing, effectively constructing different trial $\boldsymbol{\theta}$ operations. The argument also holds for all possible operations $\boldsymbol{\theta}$, since each true symmetry operation $\boldsymbol{\theta}$ is associated to a single permutation P_A . Thus the complexity of the search algorithm is reduced to $\mathcal{O}(N^2)$.

B. Reduce complexity II: preserve distances and atomic types

A PG symmetry operation θ is a unitary transformation, meaning it preserves distances. Thus, an atom after the transformation cannot have a position which is at a different distance from the origin than it was before the transformation. Moreover, upon transformation by θ , the position of atom *i* is effectively replaced by the atom i, which must have the same properties as atom i. Hence atom i should possess the same atomic type, and be positioned at the same distance from the origin, as atom i. This can be translated into a simple constraint for the choice of atom j – and also j' – namely the norms of atomic vectors (distances from the origin) must be equal, $||a_i|| = ||a_i||$ and $||a_{i'}|| = ||a_{i'}||$; and the atomic types of the pairs $\{i, j\}$ and $\{i', j'\}$ must be identical (see lines 4,5 and 7,8 of Alg. 1). Thus the complexity of the search algorithm is further reduced, to $\mathcal{O}(N_i N_{i'})$, where N_i and $N_{i'}$ are the number of atoms within the same radial distance and atomic type as atom i, and atom i', respectively.

C. Reduce complexity III: pick atoms close to origin

The numbers N_i and $N_{i'}$ are further reduced by choosing *i* and *i'* which are as close as possible to the origin (avoiding the atoms at the origin, for numerical reasons), and are of the atomic type which has the least number of equivalent atoms in that radial shell. For close-packed structures (clusters), the worst-case scenario is a structure of a single atomic type, where N_i and $N_{i'}$ are 12 (hexagonal close-packed single-crystal structure), which means 144 possible constructions of $\boldsymbol{\theta}$ by the SOFI algorithm. For some types of structures however, these numbers can be a lot higher, the extreme case being fullerene-type structures where all the N atoms are at the same distance from the origin, $N_i = N_{i'} = N$. For those structures, the use of SOFI as described and implemented in the present paper is not efficient.

D. A word about (roto-)reflections

Notice that when the bases β and γ are generated with the procedure defined earlier, the matrix θ resulting from Eq. (9) is always such that its determinant is positive, $det(\theta) = 1$. This means our search algorithm always produces trial transformations which correspond strictly to rotations. In order to mitigate this behaviour, we systematically flip each of the three vectors for each basis γ that is generated (see line 11 of Alg. 1). As such, the resulting trial transformations include proper rotations, reflections, and roto-reflections. This slightly raises the complexity of the algorithm by a factor of 4 (one for the original γ , and additional three for each flipped axis).

E. Inexact symmetries

A structure can exhibit inexact symmetries due to disorder or inaccuracies in atomic positions, which can be purely numerical, or due to physical reasons. In any case, this disorder can cause some symmetry elements to become inexact, *i.e.* the distance $d_H(A, \theta A)$ does not reach zero, but only a local minimum. For this reason we introduce the threshold sym_thr into SOFI, which modifies the condition for a transformation $\boldsymbol{\theta}$ to be recognised as symmetry operation of a structure A into $d_H(A, \theta A) < \text{sym_thr}$, which is interpreted as the maximal deviation (in units of distance) between an atom of the non-transformed structure, and its associated atom of the transformed structure, must be below the threshold. The value of sym_thr is an input parameter to SOFI. For the same reason of possible disorder in the atomic structure, the transformations $\boldsymbol{\theta}$ which are constructed from atomic vectors by Eq. (9), can potentially become inexact (in the sense of non-zero d_H). In order to obtain as precise transformation matrices $\boldsymbol{\theta}$ as possible, we introduce the concept of matrix refinement, see Sec. III and Alg. 3.

It can still happen that SOFI's parsing procedure will not identify all the symmetry operations of a structure due to such atomic disorder. In that case, arguments of fundamental group theory can be used to generate the missing symmetry operations. The most important argument is the property of group closure, which states that if $\theta_i \in G$ and $\theta_j \in G$ then also the product $\theta_i * \theta_j \in G$, where G is the point group. Therefore, after the main parsing procedure of SOFI is performed, the list of found symmetry operations can be looped through itself, and all possible products of the operations generated, then tested for the symmetry condition on the structure, and finally included in the set accordingly. Thus if any symmetry operation has been missed by the main search algorithm for any reason, it will be found and added by this (optional) procedure.

The value given to the threshold sym_thr is directly linked to the level of disorder in atomic positions on the structure. Its extremal value can ultimately be related to the distance between nearest atoms in the structure, in the sense that if the value sym_thr is close to, or larger than that, the algorithm will accept operations that effectively exchange the positions of atoms, as valid symmetry operations. In order to avoid that, the rule of thumb is that sym_thr can sensibly be set to any values up to about half the distance between nearest atoms, anything beyond that should be carefully tested, and will most probably produce results that will be hard to interpret.

III. IMPLEMENTATION

The main loop of the SOFI search procedure is schematised in Alg. 1, which follows the considerations from Sec. II. Each iteration of the main loop consists of constructing a new orthonormal basis γ , and with it a new trial operation θ' . Each trial θ' is passed to the routine try_sofi (schematised in Alg. 2). This routine first determines if the matrix is already a known symmetry operation, and if not, computes the first $d_H(A, \theta' A)$ via the CShDA algorithm. If the first d_H is small enough, the trial θ' is considered as potential symmetry operation, and passed to the refine routine (schematised in Alg. 3). The refine routine returns a refined trial θ' and the associated $d_H(A, \theta' A)$. If this distance d_H is below the threshold sym_thr, the trial θ' is stored as a new symmetry operation of A. At the end of the main loop, the list of symmetry operations $\boldsymbol{\theta}$ of structure A is known.

A trial matrix transformation θ' , whose action on a structure A is sufficiently close to some true symmetry operation $\boldsymbol{\theta}$, can be identified, and *refined* to correspond to the true symmetry θ , see Alg. 3. The matrix θ' is said to be sufficiently close to $\boldsymbol{\theta}$, when the distance $d_H(A, \boldsymbol{\theta}'A)$ is below a given parameter value, but not zero (this value in SOFI corresponds to 5 * sym_thr, see line 4 of Alg. 2). In this case, the permutation of atoms P_A that is returned when computing $d_H(A, \theta' A)$ with CShDA, is not exact, but can be said to be partially correct, meaning that there are at least some atoms for which the assignments are correct. This partially correct assignment can be applied to the structure A, and used as input to the well-known SVD-based algorithm described in Ref.¹⁸. which returns an optimal rotation given a fixed permutation of atoms. The small rotation ν which is found by SVD is added to the original transformation, $\theta'' = \nu \theta'$, and applied to the structure, $\theta''A$. At this point, the distance $d_H(A, \theta''A)$ and the corresponding assignments

Algorithm 1: The main search loop of SOFI,										
including the considerations from Sec. II A-II D.										
The called routine try_sofi is schematised in										
Alg. 2.										
Input: structure A, threshold sym_thr.										
Output: List of symmetry operations $\boldsymbol{\theta}$.										
1 Select i and i' close to origin; !! Sec IIC										
2 $\beta \leftarrow \text{OrthonormalBasis}(i, i');$!! Sec IIA										
3 for $j \in 1, N$ do										
4 if $(abs(a_i - a_j) > sym_thr) cycle; !! Sec IIB$										
5 $\mathbf{if}(typ(i) \neq typ(j))$ cycle;										
6 for $j' \in 1, N$ do										
7 $\mathbf{if}(abs(a_{i'} - a_{j'}) > \text{sym_thr}) \mathbf{cycle};$										
8 if $(typ(i') \neq typ(j'))$ cycle;										
9 $\gamma \leftarrow \text{OrthonormalBasis}(j, j');$										
10 for $m \in 0, 3$ do										
11 flip axis m of γ ; !! Sec IID										
12 $\theta' = \beta^T \gamma$; call try_sofi $(A, \theta', \text{sym_thr})$;										
13 end										
14 end										
15 end										

	Algorithm 2: The schema of routine try_sofi.
	The called routine refine is schematised in
	Alg. 3.
	Input: structure A , 3×3 matrix θ' , threshold
	sym_thr.
	Output: Updated list of symmetry operations $\boldsymbol{\theta}$.
1	Compare θ' to current list of all θ ;
2	if $(\theta' \in \text{list})$ return;
3	Compute $d = d_H(A, \theta' A)$ via CShDA algorithm;
4	if $(d > 5.0 * \text{sym_thr})$ return;
5	call refine $(A, \theta', d_H);$
6	$\mathbf{if}(\ d_H \leq \mathtt{sym_thr}\) \mathbf{add}\ \boldsymbol{\theta}'\ \mathbf{to}\ \mathbf{list};$

 P_A'' are recomputed. If P_A'' contains permutations, the cycle of SVD-CShDA is repeated. Once the new assignment does not contain any further permutation, the procedure is stopped, the refined matrix is $\theta'' = \nu \theta'$, and if $d_H(A, \theta''A) \leq \text{sym_thr}$, then the refined matrix θ'' is a true symmetry operation θ . The process is schematised in Algorithm 3.

_	
	Algorithm 3: The schema of routine refine.
	Input: structure A, trial matrix θ' .
	Output: refined matrix θ' , distance d_H .
1	$oldsymbol{ heta}^{\prime\prime} \leftarrow oldsymbol{ heta}^{\prime};$
2	$P_A, d_H \leftarrow CShDA(A, \theta''A);$
3	for $n \in 1, \max_$ iter do
4	$\nu \leftarrow SVDrotation(A, \theta''A);$
5	$oldsymbol{ heta}'' \leftarrow u oldsymbol{ heta}'';$
6	$P_A, d_H \leftarrow CShDA(A, \theta''A);$
7	if (no permutation in P_A): exit loop;
8	end
9	$\mathbf{return} \ \boldsymbol{\theta}' \leftarrow \boldsymbol{\theta}'', \ d_H$
_	

The self-sufficient iteration scheme of Algorithm 3 is similar to the algorithm Iterative Closest Point (ICP)¹⁹, which is very well known in the computer vision community. ICP has some known pitfalls, and several proposed solutions to them²⁰. The most notable being getting stuck in local minima, or oscillating between two equivalent solutions. It should be stated that these pitfalls can in principle occur in our matrix refinement approach as well, however, they occur in situations when $d_H(A, \theta' A)$ is far from zero, and above any meaningful threshold, thus the trial transformation θ' in such situations is far from a suitable candidate for our purposes, and it is not of concern. Moreover, the number of iterations in Algorithm 3 has a hard limit at max_iter=3.

In order to determine the PG from a list of symmetry operations in the form of 3×3 matrices, as returned by SOFI, we have implemented a decision process based on a flowchart available in physical chemistry textbooks³. The decision tree is based on the identification and classification of specific symmetry elements. For our purpose, the simplest way of carrying it out is to employ the Schoenflies notation for the symmetry elements, in the form of $Op \ n^{\wedge}p$, where Op is the name of the operation (C for rotation, S for rotoreflection, I for inversion, and E for identity), n is the order of rotation, and p the multiple of rotation, for example S 12^{5} corresponds to a rotoreflection with an angle of $\frac{5}{12}2\pi$. The analysis of a 3 × 3 matrix, and assignment of its Schoenflies label is done as described in the Appendix A. Once the list of symmetry operations is converted to the Schoenflies notation, and grouped together by the axis they act on, the decision tree to determine the PG is applied.

The SOFI software library is organized as a series of independent routines. For performing a default (full) search for PG of a structure, there is a wrapper routine which includes calls to all the needed routines. This includes shifting the structure to its geometric center before entering SOFI, and using the closure property of the groups to fully identify all symmetry operations (see Sec. II E). A workflow for more specialized tasks can be constructed as-desired from the routines included in the library.

The source code repository also includes an API to the main SOFI routines, which is bound to the C-namespace via the iso_c_binding intrinsic Fortran module. The API is compiled into a dynamic library (file .so), and thus the interface routines can easily be linked and called from either Fortran or C, or imported into Python. Example programs for each of these languages are included in the repository. An appropriate Python module is also proposed, which acts as an interface to the C-bound routines in the dynamic library, through the ctypes Python module.

IV. COMPARISON TO OTHER ALGORITHMS

The SOFI algorithm has been compared to the SYVA⁹, SymMol⁶, and libmsym¹⁰ software. The full details and results of the tests are available in the Supplementary Materials, and the associated Zenodo repository²¹ which contains all the structures, software, and scripts used in the test, and all results in plain text format. The goal of this comparison is to showcase the behaviour of SOFI in comparison to other established software.

All of the atomic structures included in our comparison test were obtained from the Cambridge Cluster Database $(CCD)^{22}$. They include atomic cluster structures, where we have excluded any structures with number of atoms less than 3. The total number of structures included in the test is thus 3858, with the number of atoms varying between 3 and 380. There is only one set of structures with more than one atomic type, which has two atomic types.

The comparison tests were carried out by computing the PG of each input structure, at different values of the symmetry threshold. Changing the value of this threshold can result in the respective algorithm detecting a different number of possible symmetry operations, and hence a different assignment of the PG. The SYVA and SymMol algorithms have a single adjustable parameter for the tolerance, which, to our understanding, is more or less equivalent to the symmetry threshold sym_thr used in SOFI. That is, it specifies the maximal allowed displacement of any atom of the symmetry-transformed structure, with respect to the original structure. Therefore, it is possible to directly compare the results of SYVA, SymMol, and SOFI algorithms at the same value of tolerance. On the other hand, the libmsym algorithm does not have a single-valued parameter for the tolerance, but rather a set of parameters which act upon different segments of the algorithm, and it is therefore not straight-forward to compare the results. Any computation where a respective algorithm outputs an explicit message of error or failure, or the software crashes with no output, is recorded as a failure.

The values for the tolerance used in SYVA, SymMol, and SOFI were tol = 0.001 and tol = 0.05, while for libmsym we used three sets of parameters which are also used in the Avogadro software²³, where they are labelled as "default", "medium", and "loose".

To the best of our knowledge in the CCD database, the source/algorithm which was used for obtaining the listed PGs is not clearly specified. This is an issue since the claimed PG cannot be actually tested or revised. In other words, the PG assignment by CCD cannot be assumed to have a benchmarking value.

The Fig. 1 gives a correlation plot of the PGs as assigned by the different algorithms included in the test, excluding CCD. This plot has been made by combining the results of each algorithm in the test, using the value of tolerance for which that algorithm produced the least failures. These are explicitly SYVA(tol = 0.001),

SymMol(tol = 0.05), libmsym(tol = "default"), and SOFI(tol = 0.05). A point on the diagonal of the plot represents PG assignments of SOFI equal to any of the other algorithms, while an off-diagonal point represents different assignment of PGs, for the same structure. The distance of a point from the diagonal could be seen as proportional to the extent of the difference in the assignment, in terms of number of symmetry operations of a group. Similar plots of this type are available in the Supplementary Materials, resolved per each algorithm and tolerance value included in the test.

We show in the Supplementary Materials, that SOFI is fully capable of computing the PG symmetry in atomic clusters. Contrary to other algorithms in the test, there are zero cases of failure in SOFI, among all the structures and tolerance values included in the test. In all cases of disagreement between SOFI and another algorithm, SOFI is capable of finding a PG of the same order, or higher, when computed with an appropriate tolerance value.

The small differences in SYVA, SymMol, and SOFI most probably arise due to the different ways in which algorithms find the symmetry operations, or their axes. A small difference in the axis on which a symmetry element acts, can lead to a small difference in the atomic positions of the symmetry-transformed structure, which leads to a different value of distance to the original structure. When such small discrepancies lead to distance values that are comparable to the value of symmetry threshold used, they can be sufficient to cause an algorithm to detect PGs of a different (lower) order. These small variations can be observed in our tests, where in some cases SOFI detects less symmetry operations than SYVA and SymMol, however upon slight increase in the threshold, the higher-order PGs are always retrieved.

A more in-depth analysis of all the results would require a detailed inspection of the participating algorithms, and a case-to-case analysis of each result, which is well beyond the scope of the present article. Besides, our tests did not investigate the impact of the symmetry threshold in a systematic way, which makes drawing any general conclusions from this comparison test nontrivial.

The Dzugutov-mod clusters dataset was used to give some indicative timing of the algorithms. It contains 248 structures with number of atoms from 3 to 250, all of the same atomic type. The structures where an algorithm was not able to determine a PG were excluded from this measurement, since they take a disproportionate amount of time. The SYVA algorithm took 155.8 s to determine 248 PGs, SymMol took 2.1 s to determine 245 PGs, libmsym took 0.8 s to determine 245 PGs, and SOFI took 1.2 s for 248 PGs. All the timing measurements were done on single Intel Core i7-10700K processor.



FIG. 1. Compact summary of the comparison test results: The horizontal axis represents PGs as assigned by SOFI, and the vertical axis PGs assigned by any other algorithms in the test (SYVA, SymMol, libmsym). Labels of PGs are sorted by the cardinality of the groups. The points below the diagonal represent cases where SOFI assigned a PG with higher order, and values above the diagonal represent cases where SOFI assigned a PG with lower order. The color of each point represents the number of structures where that particular combination of PG assignment happened.

V. DISCUSSION

Due to the SVD-based "matrix refinement" procedure introduced in SOFI (Sec. III, Alg. 3), the axis of a symmetry element is ultimately set such that the root-meansquare distance between the original, and the symmetrytransformed structure $d_{rmsd}(A, \theta A)$ is minimized. However it should be noted that, in general, the value of θ which minimizes a distance function D, in the sense of Eq. (10),

$$\arg\min_{\boldsymbol{\theta}} \left\{ D(\boldsymbol{\theta} A, A) \right\} \tag{10}$$

can be slightly different for different distance functions D, such as the root-mean-square d_{rmsd} , and Hausdorff distance d_H , the latter of which is used to evaluate the operations θ in SOFI by Eq. (6). This is a small inconsistency in the SOFI algorithm, and it means the value of Eq. (6) can actually *increase* slightly after the matrix refinement procedure. We have found in our tests that this is the reason for SOFI to set the axis of some symmetry operation slightly different than the other algorithms, and that leads to rare cases when SOFI needs a slightly higher value of symmetry threshold, to obtain the same PG as SYVA or SymMol. In the set of structures used in our comparison test, the usefulness of the matrix refine-

ment procedure might not be apparent, however when SOFI is used on structures with more disorder in the atomic positions, the refinement procedure is key to the recognition of proper symmetry operations.

The slowest part of the SOFI algorithm is the evaluation of the distance $d_H(A, \theta' A)$ from Eq. (5), calculated by the CShDA algorithm, which is done for each trial θ' . It would make sense to spend some computational effort in trying to lower as much as possible the number of times CShDA is computed. This can be done by recognising when a trial θ' is very similar to some already known symmetry operation θ , meaning the trial θ' can be skipped, and thus avoid computing CShDA. In order to evaluate the similarity between two orthonormal matrices, we use a simple distance function $d(\theta^a, \theta^b)$, which is a sum of the distances between the matrix elements:

$$d(\boldsymbol{\theta}^{a}, \boldsymbol{\theta}^{b}) = \sqrt{\sum_{i,j} (\boldsymbol{\theta}^{a}_{ij} - \boldsymbol{\theta}^{b}_{ij})^{2}}$$
(11)

which can be seen as a measure of the order of rotation needed to transform θ^a into θ^b . By default, SOFI considers two orthonormal matrices, namely θ' and θ , as equal when the order of rotation needed to transform one into the other is more than 200, that is an operation C200 in the Schoenflies notation, or rotation by angle $0.005 \cdot 2\pi$. This sets the maximal limit to the resolving power of SOFI, meaning that any symmetry operation of order higher than 200 can not be recognised. This default behaviour can be changed by tuning of some internal parameters, and recompiling the code. The procedure to do that is detailed in the online documentation, available through the front page of the GitHub repository.

With this modification to SOFI, a relatively big speedup is achieved for structures with a large number of atoms close to the origin (number N_i in Sec. II C), where the redundancy of the search space of matrices $\boldsymbol{\theta}$ is large. The very extreme example of such structure being the perfect fullerene-type structures, where all atoms are at the same distance.

The search space of highly symmetric tetrahedral, octahedral, and icosahedral PGs in particular -T, O, and I variants – can be largely redundant. In SOFI, this redundancy can be reduced by an early-termination condition, which is triggered when both of the following criteria are met: i) either σ or I operations are found, and ii) there are two or more unique C_n axes with $n \ge 3$. The two criteria are sufficient to terminate the search procedure, and directly identify the corresponding PG by the standard procedure. In principle, this condition can be ambiguous, since a group can be a subgroup of another (for instance, all T variants are subgroups of Oh). However the ambiguity is lifted by performing the combinations of symmetry elements identified at the current step of the algorithm, which are at that point extremely unlikely to be cyclic, and will thus generate the missing operations. The overhead of computing the early-termination condition is largely negligible.

The redundancy of the search space however cannot be reduced by the mentioned arguments when the number of symmetry operations is low, as for instance in C1, Cs, and Ci PGs. The absolute worst-case performance for the SOFI algorithm as presented in this article is thus a structure with many atoms N, all of a single atomic type, where relatively many of them are close to the origin (N_i in Sec. II C), and a low-order PG.

VI. EXEMPLARY USES

A. Generating PG by combination of group elements

In SOFI, the assignment of PG name is done by a separate routine, which acts only on the list of operations $\boldsymbol{\theta}$. Thus, we can design a small program which reads a number of input operations, generates all possible combinations $\boldsymbol{\theta}' = \boldsymbol{\theta}^i * \boldsymbol{\theta}^j$ in a self-consistent manner, and assigns the PG name to the final list of operations. In the present example, we use this program to confirm that the D2h and D3d groups are indeed among the subgroups of D6h. In group theory a high-symmetry PG may lose certain elements to give rise to a new PG, which is a subgroup of the former. Such descent of symmetry can be useful in certain applications. The small program of this example is included in the examples directory of the git repository: examples/SOFI/ex_D6h_subgroup.

The upper part of Table I lists the symmetry operations $\boldsymbol{\theta}$ of some atomic structure with the D6h PG (the precise structure is not important for this example). If we take only the four operations of labels 5 and 7, and generate all possible unique combinations $\boldsymbol{\theta}' = \boldsymbol{\theta}^i * \boldsymbol{\theta}^j$, we obtain the list of operations in the middle part of Table I. It is straightforward to verify that the obtained list of operations corresponds to D2h PG, and that all the resulting operations are in fact part of D6h, and therefore D2h is a subgroup of D6h.

Similarly, by generating all possible combinations of the four operations labelled 6 and 7 on the upper part of Table I, we obtain the list shown in the lower part of Table I, which constitutes the D3d PG, and is a subgroup of D6h. It can be verified that if we take all unique operations from the middle and lower parts of Tables I, which is 16 operations, and input them to the combinations program, we obtain back the list of 24 operations of D6h from the upper section of Table I.

B. Obtaining symmetry-equivalent configurations

The power of knowing the set of local symmetries $\boldsymbol{\theta}$ is demonstrated on the example system of heptamer island on Pt(111) surface, taken from the OptBench database²⁴, shown on Fig. 2.

A particular, known displacement of the atoms from the initial structure is shown on Fig. 3 in six symmetryequivalent variants in each panel, with the displacement

	Label	Operations $\boldsymbol{\theta}$	Axis
	0	E, I	
	1	$\sigma, C_2, C_3, C_6, S_3, S_6$	0.989 - 0.094 - 0.109
	2	σ, C_2	-0.052 -0.939 0.339
3h	3	σ, C_2	$\textbf{-}0.134 \ \textbf{-}0.330 \ \textbf{-}0.934$
ĕ	4	σ, C_2	-0.022 0.648 -0.761
	5	σ, C_2	-0.112 -0.978 -0.173
	6	σ, C_2	-0.142 -0.756 -0.639
	7	σ, C_2	0.090 - 0.183 0.979
	0	E, I	
Ъ	1	σ, C_2	-0.112 -0.978 -0.173
õ	2	σ, C_2	0.090 - 0.183 0.979
	3	σ, C_2	0.989 - 0.094 - 0.109
	0	E, I	
	1	$C_3, \overline{C_3}, S_6, \overline{S_6}$	0.989 - 0.094 - 0.109
33	2	σ, C_2	0.090 - 0.183 0.979
Н	3	σ, C_2	-0.142 -0.756 -0.639
	4	σ, C_2	-0.052 -0.939 0.339

TABLE I. Upper part: list of operations $\boldsymbol{\theta}$ of some structure with the D6h PG, grouped together by the axis they act on. The transposes of applicable operations $(\overline{C_3}, \overline{C_6}, \overline{S_3}, \overline{S_6})$ on axis 1 are omitted for clarity.

Middle part: the resulting operations of all possible combinations of four operations on axes 5 and 7 from the upper part. The PG with these operations is D2h, and all the operations are also included in D6h.

Lower part: the resulting operations of all possible combinations of four operations on axes 6 and 7 from the upper part. The PG with these operations is D3d, and all the elements are also included in D6h.



FIG. 2. Initial state configuration of the heptamer island on Pt(111) surface. Left: side view. Right: top view of the surface layer, with bonds drawn between the atoms of the island. Marked in green are the atoms of the local configuration that is used as input for SOFI.

vectors marked in cyan, each labelled Δ_j , for $j \in [1, 6]$. The displacement of the atoms by specifically these vectors actually corresponds to equivalent configurations at the saddle point of the potential energy surface (PES) of the system, the details of which are not important for the purpose of this example. By knowing only one of these displacements, say Δ_1 shown on the top left panel of Fig. 3, the other five can be generated by only using the information of local symmetry of the heptamer island, which can be computed by SOFI.



FIG. 3. First panel (top left) shows Δ_1 in cyan, which is on other panels transformed by the set $\{\boldsymbol{\theta}_j, P_j\}$, and represents saddle points of the PES equivalent by local symmetry. The top row contains the rotations of Δ_1 about the axis through the origin atom (out of plane axis), and the bottom row contains reflections of Δ_1 over three mirror planes.

In the present example, this was done by first selecting the first-neighbour local configuration around the atom at the center of the heptamer, shown in green on Fig. 2, where the set of atomic indices contained in the local configuration is labelled [s], and the atom at the center of the heptamer is taken as the origin point. This local configuration was then input to SOFI as an independent atomic structure, which returns the set of six symmetry operation matrices and the corresponding permutations $\{\boldsymbol{\theta}_i, P_i\}$, in relation to the desired origin. The symmetry operations are three rotations about the vertical axis through the origin atom, and three mirror reflections. The displacement $\Delta_1[s]$ on the subset of atoms [s] can then be transformed by applying each matrix $\boldsymbol{\theta}_{j}$, followed by permutation of the vector elements P_i , to obtain the other five displacements $\Delta_i[s]$,

$$\Delta_j[s] = P_j(\boldsymbol{\theta}_j \Delta_1[s]) \tag{12}$$

which correspond to the displacement vectors of Fig. 3, and bring the system to the symmetry-equivalent saddle point configurations.

The example shown in this section illustrates a procedure which exploits the list of symmetry operations, and applies them on some property of the atomic structure to obtain the symmetry-equivalent representations of that property, in this case a displacement. By analogy, such procedure can be done to any vectorial property of a structure, for which symmetry-equivalent representations exist. The symmetrization of an atomic structure is an example of such procedure (with some modifications), acting on the atomic positions.

VII. CONCLUSION

We have developed the SOFI algorithm for finding PG symmetry operations of non-periodic atomic structures, based on the IRA shape matching algorithm¹⁴. The working principle of SOFI is to cast the problem of finding PGs as a shape-matching problem of a single structure with itself, and find all the degenerate solutions. The set of these solutions corresponds to the symmetry operations of the atomic structure.

Contrary to some other algorithms, SOFI is not limited to the number of atoms that a structure can contain. It is also agnostic to the choice of the origin point, which allows the identification of symmetry operations about any chosen point/atom, not only the geometric center.

We have tested SOFI on a large set of atomic structures where symmetry identification can be challenging, such as single-element clusters and close-packed structures. The former are critical because of the large number of possible permutations of atomic indices, and the latter due to the rather homogeneous spatial distribution of atoms, which prevents simple identification of any principal axes. Both these cases are of relevance for numerical applications, for instance in processing substructures obtained from other condensed phase (periodic) simulations, whenever a local symmetry assignment is required for clusters or slabs, and hence where an automatic assignment of symmetry is highly desirable. Due to the way SOFI parses through the space of possible operations, it can be advantageous in such critical cases.

We have compared the results of our SOFI algorithm to three other algorithms for PG identification from the literature, namely SYVA, SymMol, and libmsym, at two different values of the symmetry threshold. The results are given in a statistical manner that shows the general behaviour of SOFI, as compared to other algorithms. SOFI was able to successfully identify PGs across all sets, with a large degree of agreement with other algorithms. In most cases of disagreement between algorithms, SOFI has found a higher number of symmetry elements within the specified symmetry threshold, and thus a higher order point group. In all cases where SOFI found a lower order PG than another algorithm, we have been able to retrieve the higher order PG by tuning of the symmetry thresholds parameter of SOFI.

We also present two examples of how SOFI can be utilised, other than simple identification of PGs; in the first example as a tool to generate combinations of several matrices until group completeness; and in the second example as tool to aid automatic generation of structures, and their properties (in this case a displacement vector), that transform according to the local PG symmetry about a specific atom, *i.e.* any covariant property.

One of the core ideas of SOFI is to provide a modular, and interoperable set of computational routines, which could be used for retrieving the point group symmetry properties of a structure, as standalone, or within another application. The inclusion of SOFI into the IRA library makes it a convenient, and accessible tool for purposes related to the precise analysis of atomic structures.

SUPPLEMENTARY MATERIALS

The supplementary material contains all results of the comparison tests done in this work. The results are reported in tables and images, where the tables report the result (PG) of each algorithm included in the test for each structure, and the images serve as an overall comparison between the algorithms.

ACKNOWLEDGMENTS

The authors are active members of the Multiscale And Multi-Model ApproacheS for Materials In Applied Science consortium (MAMMASMIAS consortium), and acknowledge the efforts of the consortium in fostering scientific collaboration. The work was partly funded by the Croatian Science Foundation (HrZZ), via the project IP-2020-02-7262 (HYMO4EXNOMOMA). All images of atomic structures in this article were generated with Ovito²⁵ software.

AUTHOR DECLARATIONS

Conflict of interest

The authors have no conflicts to disclose.

Author contributions

M. Gunde: Conceptualization, Data curation, Software, Writing - original draft, Writing - review & editing, Supervision, Visualization; N. Salles: Conceptualization, Writing - review & editing, Supervision, Visualization, Writing - review & editing, Supervision, Visualization, Writing - review & editing, Supervision, Visualization, Writing - review & editing, Supervision, Visualization; A. Hemeryck: Conceptualization, Writing - review & editing, Supervision, Visualization; Supervision, Visualization; Supervision, Visualization; Supervision, Visualization; Supervision, Visualization; A. Hemeryck: Conceptualization;

DATA AND SOURCE CODE AVAILABILITY

SOFI is released as part of the IRA library, which is under double licensing, GPL v3 and Apache v2. The source code and example programs are available at https://github.com/mammasmias/ IterativeRotationsAssignments. Link to the online documentation is available from the main GitHub page, which includes some tutorials, and detailed descriptions of the source code, the C-bound API, and the python interface. All data used in the comparison tests is openly available from the CCD^{22} . All datasets and scripts used in the comparison test, and plain-text results are available from Zenodo²¹.

Appendix A: Some properties of PG symmetry matrices

The matrices $\boldsymbol{\theta}$ corresponding to PG symmetry operations are orthonormal ($\boldsymbol{\theta}^{-1} = \boldsymbol{\theta}^T$), non-symmetric matrices with real elements, and correspond to either pure rotations (symbol C), pure reflections (symbol σ), or combinations of both (rotoreflections, symbol S).

The matrices θ_R corresponding to pure rotations (symbol C) have a positive determinant, $det(\theta_R) = 1$, the value of trace is $Tr(\theta_R) = 1 + 2\cos(\alpha)$, and their eigenvalues are $\lambda_1 = 1$, and $\lambda_{2,3} = \exp(\pm i\alpha)$ where α is the angle of rotation about the axis given by the eigenvector corresponding to λ_1 . A pure rotation matrix can be constructed from knowing the angle and axis of rotation, for example by the well-known Euler-Rodrigues rotation formula.

Matrices $\boldsymbol{\theta}_F$ which represent pure reflection (symbol σ) are characterised by the negative determinant, $det(\boldsymbol{\theta}_F) = -1$, the value of trace $Tr(\boldsymbol{\theta}_F) = 1$, and their eigenvalues are $\lambda_1 = -1$, and $\lambda_{2,3} = 1$. The normal vector of the plane of reflection is given by the eigenvector of $\boldsymbol{\theta}_F$ corresponding to λ_1 . A reflection matrix can be constructed from knowing the normal vector of the plane of reflection $|x\rangle$ by $\boldsymbol{\theta}_F = E - 2 |x\rangle \langle x|$, where E is the identity matrix, and $|.\rangle \langle .|$ indicates the outer product.

Matrices θ_{RF} corresponding to rotoreflections (symbol S) are characterised by the negative determinant, $det(\theta_{RF}) = -1$, the value of trace $Tr(\theta_{RF}) = -1 + 2\cos(\alpha)$, and their eigenvalues are $\lambda_1 = -1$, and $\lambda_{2,3} = \exp(\pm i\alpha)$, where α is the angle of rotation about the axis given by the eigenvector of λ_1 , which is at the same time also the normal vector of the plane of reflection. Matrices corresponding to rotoreflections can be constructed from combination of pure rotation and pure reflection matrices, $\theta_{RF} = \theta_F \theta_R$, where θ_F and θ_R have the same vector as the axis of rotation, and the normal of the plane of reflection.

The angle α in radians is transformed to integers n and p, such that $\alpha/2\pi = p/n$. For instance, the rotation for 5/12th of a circle (angle 150°), would be n = 12 and p = 5.

It can be observed that the use of σ symbol for pure reflections over some axis is redundant, since an equivalent notation is a rotoreflection S with angle $\alpha = 0$. We thus label pure reflections as "S 0".

The properties listed above are synthesised in the Table II.

The slight exceptions to the above are the identity E = diag(1, 1, 1) and the point-inversion I = diag(-1, -1, -1), which have the same matrix form regardless of the orientation of the reference frame. Never||identity E | inversion I | rotation C | rotoreflection S

$det(\boldsymbol{\theta})$	1	-1	1	-1
$\lambda_{1,2,3}$	1, 1, 1	-1, -1, -1	1, $\exp(\pm i\alpha)$	$-1, \exp(\pm i\alpha)$
$Tr(\boldsymbol{\theta})$	3	-3	$1 + 2\cos(\alpha)$	$-1+2\cos(\alpha)$

TABLE II. The axis of rotation (plane of reflection) is given by the eigenvector corresponding to λ_1 .

the less, the identity matrix can be seen as rotation about any axis for an angle $\alpha = 0$ (operation C 0), and the point-inversion can be seen as rotor effection about any axis for an angle $\alpha = \pi$ (operation S 2¹).

Due to the numerical procedure of matrix diagonalization, where any \pm direction is an equivalent solution for the eigenvectors (thus the axis), the relative orientation of the operation (sign of the angle α) cannot be trusted. For this reason, we follow the convention for orienting the axis such that its components are: z > 0, if z = 0then x > 0, and if x = 0 then y > 0. The sign of α is then deduced with respect to this axis.

- ¹G. Herrero-Saboya, L. Martin-Samos, N. Richard, and A. Hemeryck, "Common defects in diamond lattices as instances of the general t \bigotimes ($e + t_2$) jahn-teller effect," Phys. Rev. Mater. **6**, 034601 (2022).
- ²F. A. Cotton, *Chemical applications of group theory* (John Wiley & Sons., 1990.).
- ³P. Atkins and F. R., "Molecular quantum mechanics," (Oxford university Press, 2005) Chap. 5.
- ⁴E. Apra, E. J. Bylaska, W. A. de Jong, N. Govind, K. Kowalski, T. P. Straatsma, M. Valiev, H. J. J. van Dam, Y. Alexeev, J. Anchell, V. Anisimov, F. W. Aquino, R. Atta-Fynn, J. Autschbach, N. P. Bauman, J. C. Becca, D. E. Bernholdt, K. Bhaskaran-Nair, S. Bogatko, P. Borowski, J. Boschen, J. Brabec, A. Bruner, E. Cauët, Y. Chen, G. N. Chuev, C. J. Cramer, J. Daily, M. J. O. Deegan, J. Dunning, T. H., M. Dupuis, K. G. Dyall, G. I. Fann, S. A. Fischer, A. Fonari, H. Früchtl, L. Gagliardi, J. Garza, N. Gawande, S. Ghosh, K. Glaesemann, A. W. Goetz, J. Hammond, V. Helms, E. D. Hermes, K. Hirao, S. Hirata, M. Jacquelin, L. Jensen, B. G. Johnson, H. Jónsson, R. A. Kendall, M. Klemm, R. Kobayashi, V. Konkov, S. Krishnamoorthy, M. Krishnan, Z. Lin, R. D. Lins, R. J. Littlefield, A. J. Logsdail, K. Lopata, W. Ma, A. V. Marenich, J. Martin del Campo, D. Mejia-Rodriguez, J. E. Moore, J. M. Mullin, T. Nakajima, D. R. Nascimento, J. A. Nichols, P. J. Nichols, J. Nieplocha, A. Otero-de-la Roza, B. Palmer, A. Panyala, T. Pirojsirikul, B. Peng, R. Peverati, J. Pittner, L. Pollack, R. M. Richard, P. Sadayappan, G. C. Schatz, W. A. Shelton, D. W. Silverstein, D. M. A. Smith, T. A. Soares, D. Song, M. Swart, H. L. Taylor, G. S. Thomas, V. Tipparaju, D. G. Truhlar, K. Tsemekhman, T. Van Voorhis, Vázquez-Mayagoitia, P. Verma, O. Villa, A. Vishnu, K. D. Vogiatzis, D. Wang, J. H. Weare, M. J. Williamson, T. L. Windus, K. Woliński, A. T. Wong, Q. Wu, C. Yang, Q. Yu, M. Zacharias, Z. Zhang, Y. Zhao, and R. J. Harrison, "NWChem: Past, present, and future," The Journal of Chemical Physics **152**, 184102 (2020), https://pubs.aip.org/aip/jcp/articlepdf/doi/10.1063/5.0004997/16684361/184102 1 online.pdf.
- ⁶T. Pilati and A. Forni, "SYMMOL: a program to find the maximum symmetry group in an atom cluster, given a prefixed tolerance," J. Appl. Crystallogr. **31**, 503–504 (1998).
- ⁷R. J. Largent, W. F. Polik, and J. R. Schmidt, "Symmetrizer: Algorithmic determination of point groups in nearly symmetric molecules," J. Comput. Chem. **33**, 1637–1642 (2012), https://onlinelibrary.wiley.com/doi/pdf/10.1002/jcc.22995.

- ⁸K. Nedwed, K. Gatterer, and H. P. Fritzer, "Symapps 1.0: A software packet for group theoretical applications to molecular symmetry," Comput. Chem. 18, 371–376 (1994).
- ⁹L. Gyevi-Nagy and G. Tasi, "Syva: A program to analyze symmetry of molecules based on vector algebra," Comput. Phys. Commun. **215**, 156–164 (2017).
- ¹⁰M. Johansson and V. Veryazov, "Automatic procedure for generating symmetry adapted wavefunctions," J. Cheminformatics 9, 8 (2017).
- ¹¹O. Beruski and L. N. Vidal, "Algorithms for computer detection of symmetry elements in molecular systems," J. Comput. Chem. **35**, 290–299 (2014), https://onlinelibrary.wiley.com/doi/pdf/10.1002/jcc.23493.
- ¹²J. Ivanov and G. Schüürmann, "Simple algorithms for determining the molecular symmetry," J. Chem. Inf. Comp. Sci. **39**, 728– 737 (1999), https://doi.org/10.1021/ci990322q.
- ¹³N. M. Vandewiele, R. Van de Vijver, K. M. Van Geem, M.-F. Reyniers, and G. B. Marin, "Symmetry calculation for molecules and transition states," J. Comput. Chem. **36**, 181–192 (2015), https://onlinelibrary.wiley.com/doi/pdf/10.1002/jcc.23788.
- ¹⁴M. Gunde, N. Salles, A. Hémeryck, and L. Martin-Samos, "Ira: A shape matching approach for recognition and comparison of generic atomic patterns," J. Chem. Inf. Model. **61**, 5446–5457 (2021), pMID: 34704748, https://doi.org/10.1021/acs.jcim.1c00567.
- ¹⁵M. Gunde, "Development of ira: a shape matching algorithm, its implementation, and utility in a general off-lattice kmc kernel (phd thesis)," (2021).
- ¹⁶A. Pausch, M. Gebele, and W. Klopper, "Molecular point groups and symmetry in external magnetic fields," J. Chem. Phys. **155**, 201101 (2021), https://doi.org/10.1063/5.0069859.

- ¹⁷T. Eiter and H. Mannila, "Distance measures for point sets and their computation," Acta Inform. **34**, 109–133 (1997).
- ¹⁸K. S. Arun, T. S. Huang, and S. D. Blostein, "Least-squares fitting of two 3-d point sets," IEEE T. Pattern Anal. **PAMI-9**, 698-700 (1987).
- ¹⁹P. J. Besl and N. D. McKay, "A method for registration of 3-d shapes," IEEE T. Pattern Anal. 14, 239–256 (1992).
- ²⁰H. Pottmann, Q.-X. Huang, Y.-L. Yang, and S.-M. Hu, "Geometry and convergence analysis of algorithms for registration of 3d shapes," Int. J. Comput. Vision **67**, 277–296 (2006).
- ²¹M. Gunde, N. Salles, L. Grisanti, L. MARTIN-SAMOS, and A. Hemeryck, "SOFI: Finding point group symmetries in atomic clusters as finding the set of degenerate solutions in a shapematching problem," (2024).
- ²²D. J. Wales, J. P. K. Doye, A. Dullweber, M. P. Hodges, F. Y. N. F. Calvo, J. Hernández-Rojas, and T. F. Middleton, "The cambridge cluster database," https://wwwwales.ch.cam.ac.uk/CCD.html.
- ²³M. D. Hanwell, D. E. Curtis, D. C. Lonie, T. Vandermeersch, E. Zurek, and G. R. Hutchison, "Avogadro: an advanced semantic chemical editor, visualization, and analysis platform," Journal of Cheminformatics 4, 17 (2012).
- ²⁴S. T. Chill, J. Stevenson, V. Ruehle, C. Shang, P. Xiao, J. D. Farrell, D. J. Wales, and G. Henkelman, "Benchmarks for characterization of minima, transition states, and pathways in atomic, molecular, and condensed matter systems," J. Chem. Theory Comput. **10**, 5476–5482 (2014), pMID: 26583230, https://doi.org/10.1021/ct5008718.
- ²⁵A. Stukowski, "Visualization and analysis of atomistic simulation data with ovito-the open visualization tool," Model. Simul. Mater. Sc. 18, 015012 (2009).

Supplementary Materials for: "SOFI: Finding point group symmetries in atomic clusters as finding the set of degenerate solutions in a shape-matching problem"

M. Gunde^a, N. Salles^b, L. Grisanti^{a,b}, L. Martin-Samos^b, A. Hemeryck^c

^a Institute Ruđer Bošković, Bijenička 54, 10000 Zagreb, Croatia

^b CNR-IOM/Democritos National Simulation Center, Istituto Officina dei Materiali, c/o SISSA, via Bonomea 265,

IT-34136 Trieste, Italy

^c LAAS-CNRS, Université de Toulouse, CNRS, 7 avenue du Colonel Roche, 31000 Toulouse, France

1 Algorithms and datasets used in the comparison test

All the structures, software source codes, scripts, and plain-text format of all results from the test can be downloaded from Zenodo [1].

The SOFI algorithm presented in the main article has been compared to the SYVA [2], SymMol [3], and libmsym [4] software. SYVA has been downloaded from ¹. SymMol software has been extracted from IQmol3 respository, commit 32cbf13 at ², and libmsym v0.2.3 from ³.

In order to make the tests run smoother, we had to make some small modifications to some of the source code, mostly regarding their output. The SYVA code was used completely as-is, it is limited to max 250 atoms, and we were not able to modify that limit. The SymMol code is by default limited to maximum 100 atoms, but we were able to simply modify this to our needs. Its source was also modified in one instance of integer initialisation, which was causing a crash due to segmentation fault. The output of SymMol uses the label "C3i", and "T23" for the groups "S6" and "T" respectively. The former is a possible alternative nomenclature, while we are not sure of the latter, it might simply be a typo in the code. We change all instances of these labels to "S6", and "T", after SymMol outputs them. The libmsym software has been modified as suggested in the GitHub issue #17⁴ to properly output the group C1, instead of an error message, when that is the case. All modifications to the source codes done for the purpose of this test are available as diff patches in the Zenodo reference [1].

The data sets containing the atomic structures used for testing the code are taken from the Cambridge Cluster Database (CCD) website [5], more specifically the sets where PG information is available. The ones used in our test are listed below, referred to by their name as it appears on the CCD website:

- Lennard-Jones clusters N=3-150 [6],
- Quantum Lennard-Jones clusters [7],
- Sutton-Chen clusters 10-8, 9-6, and 12-6 [8],
- Glue clusters Al, [9], and Pb [10],
- Gupta clusters (Zn, Cd, Pb, Na) [11, 12, 13],
- Murrel-Mottram clusters (Na) [12],
- Finnis-Sinclair clusters Mo and Fe [14],
- C60 clusters [15],
- C60-Pacheco clusters [16],
- Morse clusters [17, 18, 19],

¹https://data.mendeley.com/datasets/xd4g8hyjf2/1

²https://github.com/nutjunkie/IQmol3/blob/09e9f6b832e8a7cb6bde1e787a93a03993023713/src/Fortran/symmol.f90 ³https://github.com/mcodev31/libmsym/releases/tag/v0.2.3

⁴https://github.com/mcodev31/libmsym/issues/17

- Dzugutov [20], and Dzugutov-mod clusters [21],
- $(NaCl)_N CL^-$ for Coulomb/Born-Meyer and Welch potentials [22],
- binary Lennard-Jones clusters [23].

The format of the files containing atomic structures was changed into the regular xyz format, and all atomic types have been assigned to character (string) symbol values. In cases when the atomic type is not obvious (i.e. in the binary LJ, or morse dataset), H and/or He were used as surrogate symbols.

The total dataset of atomic structures thus contains 3858 structures, with number of atoms ranging from 3 to 380. The only set of structures containing more than one atomic type is the bin_LJ set, which contains two atomic types.

2 Methodology

2.1 The tolerance values

The algorithms SYVA [2], SymMol [3], and SOFI have a more or less equivalent definition of the tolerance parameter (symmetry threshold in SOFI), which is that the maximal displacement of any atom of the symmetry-transformed structure, with respect to the original structure, should be below the tolerance. Due to the equivalent definition and meaning of the tolerance value, the results of these three algorithms can be directly compared at the same value of tolerance.

We have performed the tests with the tolerance at two values, (i) with tol=0.001, which is the default value for the tolerance in the SYVA code, and (ii) at the value tol=0.05. These values were applied to the SYVA, SymMol, and SOFI algorithms. The software libmsym [4] does not have a single value for the tolerance parameter, but instead several values related to different aspects of the respective algorithm. For the present test, we took three different sets of values for the tolerance in libmsym, which are also used in the avogadro software [24], in which they are labelled as "tight" or "default", "medium", and "loose" (see link ⁵).

2.2 Reported values

For each input structure we compute the PG with a given tolerance, using each algorithm. The symbol "-" in any entry indicates a failure of the software to find any PG, where the error or failure was either reported by the code, the code has crashed with no output, or in the case of SymMol the computation has timed out.

The leading hypothesis for differences in the results of the compared algorithms is that the use of principal axes of inertia can be ambiguous when its eigenvalues are very similar. For this reason, we explicitly compute the matrix of inertia for each structure, and diagonalize it to obtain the principal axes. We then perform the scalar product between each of the principal axes of inertia, and each of the principal axes of symmetry as found by SOFI, and store the highest value of the dot product among all the possible combinations. The absolute value 1.0 of this dot product indicates that any one of the principal axes of inertia is indeed along any one of the principal axes of symmetry, while a value significantly lower than 1.0 indicates that none of the principal axes of inertia are aligned with any of the principal axes of symmetry. The value is reported in the tables under the column "dot product". For the C1 point groups, the reported value is irrelevant since the C1 group has no principal axis of symmetry.

The columns labelled N_{op} report the number of symmetry operations associated to the respective PG.

3 Results

For a more compact representation, the results are plotted in form of 2D histograms (*i.e.* Fig. S1), where each of the axes represents the result for a given atomic structure by a given algorithm, at a given tolerance value. All cases of failure are omitted from the 2D histograms. The values inside the plot are positioned such that their (x, y) position encodes the PGs resulting from each of the two algorithms, and their numerical value represents the number of input structures where such combination of PGs occurred. The values on the diagonal of the plot represent cases when the two compared algorithms returned the same result for the same structure. The off-diagonal values represent cases where the two algorithms have returned a different result.

The point groups are ordered on the axes by their order/cardinality (number of elements). All values appearing on the upper side of the diagonal indicate that the resulting PG by algorithm reported on the *y*-axis has a higher order than the same result with the algorithm on the *x*-axis, and the opposite for values below the diagonal.

⁵https://github.com/OpenChemistry/avogadrolibs/blob/master/avogadro/qtplugins/symmetry/symmetrywidget.cpp

In the big majority of structures, the algorithms agree among each other in the resulting PG, there are however some cases of different results. In the following sections we analyze the cases of differences, mainly from the point of view of SOFI. That is, we are not interested in analysing and resolving each particular problematic case of every algorithm, but rather only those where there is a difference with respect to SOFI. In cases where SOFI finds a lower-order PG, we find the value of tolerance needed by SOFI to obtain the same PG. In the opposite case, we do not perform any further computation. Due to this, the comparison tests performed here cannot be viewed as fair benchmarking of algorithms, but merely as a way to expose the performance of SOFI, by means of comparison to other established algorithms.

The Sections 3.1, 3.2, and 3.3 contain the comparisons to SYVA, SymMol, and libmsysm, respectively. The Section 5 lists the results of all algorithms and structures used in the test. The summary of reported failures is provided in the Tab. S8.

3.1 Comparison with SYVA

The SYVA software is by implementation limited to max 250 atoms, we thus ignore all structures with more than 250 atoms, they are not included in the following analysis.



Figure S1: Comparison of SYVA and SOFI at (left) tol = 0.001, and (right) tol = 0.05.

3.1.1 Value *tol* = 0.001

The case with tol = 0.001 is shown on Fig. S1(left). All the resulting PGs agree with the result of SYVA(tol = 0.001), except the five cases listed in Tab. S1, which we analyzed further:

set	struc name	SYVA	N_{op}	SOFI	N_{op}	dot product	needed tol
glue_Pb	54	-	0	S10	10	1.00000	
gupta/Co	174	Cs	2	C1	1	1.00000	0.00131
gupta/Co	183	-	0	C2	2	1.00000	
gupta/Co	190	D5	10	D5h	20	1.00000	
QLJ	75A	Cs	2	C1	1	0.96203	0.0014

Table S1: Cases of different results between SYVA and SOFI at tol = 0.001. There are two cases of failure by SYVA. In cases where SYVA has found a PG with a higher order, the column labelled "needed tol" indicates the value of tol such that SOFI(tol) retrieves the same PG as SYVA.

• structure glue_Pb:54, SYVA reports "unable to determine PG", however the symmetry operations that it reports correspond to point group S10. SOFI reports group S10.

- structure Gupta/Co:174, SYVA reports group Cs, while SOFI reports group C1. The S0 symmetry operation that is missed by SOFI(tol = 0.001) is found with SOFI(tol = 0.00131).
- structure Gupta/Co:183, SYVA reports 3 symmetry operations, but reports a failure to find PG. SOFI(tol = 0.001) reports 2 symmetry operations and the group C2. The extra symmetry operation found by SYVA(tol = 0.001) is found by SOFI(tol = 0.0012), which finds an additional symmetry for the group C2v.
- structure Gupta/Co:190, SYVA find D5, SOFI finds D5d-, and D5h after combinations, with maximal distortion value 0.0012.
- structure QLJ:71A, SYVA finds Cs, SOFI finds C1. The S0 symmetry missed by SOFI(tol = 0.001) is retrieved with SOFI(tol = 0.0014).

Upon some analysis of the SYVA source code, we find a table of hard-coded point groups, and the group S10 is not among them (see file blockdata.f in SYVA source). It also seems like SYVA does not attempt to deal with slightly broken symmetries (as in structure Gupta/Co:183), but instead directly reports a failure.

Henceforth we skip listing and analysing any of the reported failures.

3.1.2	Value	tol =	0.05

set	struc name	SYVA	N_{op}	SOFI	N_{op}	dot product	needed tol
glue_Al	134	C2v	4	C2	2	1.00000	0.059
glue_Al	181	C2v	4	Cs	2	1.00000	0.062
glue_Al	183	Cs	2	C1	1	1.00000	0.061
gupta/Co	37	C2	2	C1	1	0.99998	0.051
gupta/Na	246	D5	10	C5	5	1.00000	0.051
murrel-mottram/Na	109	Cs	2	C1	1		
murrel-mottram/Na	112	Cs	2	C1	1		
murrel-mottram/Na	113	Cs	2	C1	1		
murrel-mottram/Na	120	C2v	4	C2	2	1.00000	
NaCl_N/CBM	15	Cs	2	C1	1		

Table S2: Cases of different results between SYVA and SOFI at tol = 0.05. There are 290 cases of failure by SYVA. In cases where SYVA has found a PG with a higher order, the column labelled "needed tol" indicates the value of tol such that SOFI(tol) retrieves the same PG as SYVA.

In the case of tol = 0.05, the number of differences between SYVA and SOFI is 10. The number of failures reported by SYVA(tol = 0.05) is 290, without counting the structures with more than 250 atoms. The cases of different results are given in the Tab. S2.

In the last 5 cases of the Tab. S2 (the murrel-mottram and NaCl_N cases), SYVA has returned a PG of higher order than SOFI, and we were not able to determine the value of *tol* for which SOFI(*tol*) would retrieve the same groups. Upon further inspection into these cases, the symmetry operations in the SYVA output seem unconventional, for example the reported axes of symmetry are far from normalized (normally the axes output by SYVA are normalized), the angles of rotation have peculiar values such as 179.95 degrees (which we have not observed in other SYVA outputs). These observations make us suspect a possible (unknown) software bug in SYVA, which might be further supported by the fact that none of the included software reports the groups found by SYVA for these structures, at any tolerance value (see the complete results in Sec. 5, namely the corresponding entries in Tables S45, S46, and S50). In fact, all other software agree in the resulting PG.

3.2 Comparison with SymMol

In some cases, the SymMol software seems to get trapped in what appears to be an infinite loop (a process that never terminates). To mitigate this, we constrain every call to SymMol with a timeout value of 10 seconds. If a computation takes more than 10 seconds, the call is terminated and result recorded as failure.

SymMol software labels the S6 group as C3i. We have changed all occurrences of C3i in the results into S6, a-posteriori.

3.2.1 Value *tol* = 0.001

The number of different results between SymMol(tol = 0.001) and SOFI(tol = 0.001) is 225, where in all cases SOFI has found a higher order PG that SymMol. On top of that, the number of cases where SymMol fails due to the timeout constraint is 112. We skip listing all these cases here, but they could easily be filtered from all the results.



Figure S2: Comparison of SymMol and SOFI at (left) tol = 0.001, and (right) tol = 0.05.

3.2.2 value tol = 0.05

set	struc name	SymMol	N_{op}	SOFI	N_{op}	dot product	needed tol
glue_Al	134	C2v	4	C2	2	1.00000	0.059

Table S3: Case of higher-order symmetry obtained by SymMol than SOFI at tol = 0.05. The column labelled "needed tol" indicates the value of tol such that SOFI(tol) retrieves the same PG as SymMol.

The number of different results between SymMol(tol = 0.05) and SOFI(tol = 0.05) is 221, where in all cases except for one, SOFI has found a higher order PG that SymMol. The single case where SymMol(tol = 0.05) found a higher order symmetry is reported in Tab. S3. With the modified tolerance, SOFI(tol = 0.059) retrieves the C2v group reported by Symmol(tol = 0.05). On top of that, the number of cases where SymMol fails due to the timeout constraint is 112.

3.2.3 General observations

		SY	VA	Sym	Mol		libmsym		so	FI	
set	name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	dot product
bin_LJ/1.05	55	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.98152
$bin_LJ/1.1$	45	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.99961
bin_LJ/1.15	45	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.99898
$bin_LJ/1.2$	45	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.97000
$bin_LJ/1.25$	45	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.95774
bin_LJ/1.3	45	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.96335
dzugutov	13	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.99682
dzugutov_mod	13	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.93269
gupta/Co	13	Ih	-	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.97125
gupta/Na	13	Ih	-	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.93316
gupta/Na	297	-	-	Ci	Ci	Ih	Ih	Ih	Ih	Ih	1.00000
gupta/Pb	13	Ih	-	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.97225
gupta/Pb	54	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.95000
gupta/Pb	55	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.95450
LJ	13	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	1.00000
LJ	135	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.91305
LJ	147	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.89257
morse	13A	Ih	-	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.96634
morse	45A	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.98813
morse	55B	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.94555
morse	147B	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.97282
sutton_9_6	13	Ih	-	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.98001
sutton_9_6	55	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.98488
sutton_10_8	13	Ih	-	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.99522
sutton_12_6	13	Ih	-	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.94451
sutton_12_6	55	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	0.97111

Table S4: Cases where SymMol fails to recognize the Ih point group.

It is worth noting that the SymMol algorithm seems to have some trouble in recognising the Ih group. Out of 53 structures in the dataset where Ih group appears, SymMol only recognizes 27 of them correctly, even when all other algorithms seem to agree on the Ih group. Moreover, SymMol systematically labels these as the Ci group. All such

cases are noted in the Tab. S4. It is also worth noting that in many of these cases, the value of "dot product", which is the maximal scalar product between the symmetry axes and the principal axes of inertia, is below 1.0. This is significant since there are 6 principal axes of symmetry in the Ih group, and none of them seem to perfectly align with any of the principal axes of inertia. Based on this data, one could make a statement about the idea of basing the identification of symmetry axes solely on the inertial axes, or more precisely a statement about the ambiguity of such procedure.

3.3 Comparison with libmsym

Since the libmsym software has a completely different definition of tolerance, we cannot directly compare the obtained value. We thus compare each of the three sets of tolerance values used in libmsym, with each of the two tolerance values used in SOFI.

3.3.1 libmsym(tol = "default")



Figure S3: Comparison of libmsym(tol = "default") with (left) SOFI(tol = 0.001), and (right) SOFI(tol = 0.05).

There are 20 cases of failure of libmsym(tol = "default"), the number of cases where SOFI(tol = 0.001) found a higher-order PG than libmsym(tol = "default") is 18, while in 23 cases libmsym(tol = "default) found a higher-order PG. The latter 23 cases are listed in Tab. S5. We can observe that SOFI can retrieve the PG found by libmsym in all the cases, by setting a slightly higher tolerance value.

In case of SOFI(tol = 0.05), there are 57 differences with respect to libmsym(tol = "default"), in all of which SOFI has found a higher-order PG than libmsym.

3.3.2 libmsym(tol = "medium")

At the "medium" tolerance level, libmsym reports a failure for 227 cases. The number of cases where SOFI(tol = 0.001) produces a higher-order PG than libmsym(tol = "medium") is 33, while vice-versa the number of cases is 28. The latter 28 cases are reported in Tab. S6.

With SOFI(tol = 0.05) there are 58 cases where SOFI finds a higher-order PG, and 3 cases where libmsym(tol = "medium") finds a higher-order PG. These 3 cases can be inferred from Tab. S6, as the cases where "needed tol" is beyond 0.05, namely structures in the glue_Al set, 79, 134, and 183. It can be observed that all of those can be retrieved in SOFI by raising the tolerance.

3.3.3 libmsym(tol = "loose")

With the libmsym(tol = "loose"), there are 782 failures reported by libmsym. In 82 cases SOFI(tol = 0.001) has found higher-order PG, while in 37 cases libmsym(tol = "loose") found a high-order PG.

set	struc name	libmsym	Nop	SOFI	Nop	dot product	needed tol
gupta/Co	174	Cs	2	C1	1	1.00000	0.0014
gupta/Co	175	Cs	2	C1	1	1.00000	0.0035
gupta/Co	179	Cs	2	C1	1	1.00000	0.0021
gupta/Co	184	Cs	2	C1	1	1.00000	0.0020
murrel-mottram/Na	40	Cs	2	C1	1	1.00000	0.0032
murrel-mottram/Na	99	C2	2	C1	1	0.99994	0.0051
murrel-mottram/Na	107	C2	2	C1	1	1.00000	0.0067
murrel-mottram/Na	111	C5	5	C1	1	1.00000	0.0015
murrel-mottram/Na	132	Cs	2	C1	1	1.00000	0.0078
murrel-mottram/Na	152	Cs	2	C1	1	1.00000	0.0026
murrel-mottram/Na	153	C3v	6	C1	1	1.00000	0.0026
murrel-mottram/Na	154	Cs	2	C1	1	1.00000	0.0015
murrel-mottram/Na	157	C2v	4	C1	1	1.00000	0.0038
murrel-mottram/Na	158	Cs	2	C1	1	1.00000	0.002
murrel-mottram/Na	182	C2	2	C1	1	1.00000	0.0026
murrel-mottram/Na	207	C3	3	C1	1	1.00000	0.0035
murrel-mottram/Na	216	т	12	C1	1	0.95174	0.0032
murrel-mottram/Na	222	C3	3	C1	1	1.00000	0.0024
murrel-mottram/Na	232	D3	6	C1	1	1.00000	0.0014
murrel-mottram/Na	242	C2	2	C1	1	1.00000	0.0029
murrel-mottram/Na	321	Cs	2	C1	1	1.00000	0.0017
murrel-mottram/Na	327	C2v	4	Cs	2	1.00000	0.002
QLJ	75A	C5v	10	C1	1	1.00000	0.0053

Table S5: Cases of higher-order symmetry obtained by libmsym(tol = "default") than SOFI(tol = 0.001). The column labelled "needed tol" indicates the value of tol such that SOFI(tol) retrieves the same PG as libmsym.



Figure S4: Comparison of libmsym(tol = "medium") with (left) SOFI(tol = 0.001), and (right) SOFI(tol = 0.05).

When using SOFI(tol = 0.05), there are 93 cases where SOFI finds a higher-order PG, and 13 cases where libmsym(tol = "loose") finds a higher-order PG. All these 13 cases can be inferred from Tab. S7, as cases where the "needed tol" exceeds 0.05. It can also be observed that for all these cases, SOFI can retrieve the higher-order PG with an appropriate value of tol.

set	struc name	libmsym	Nop	SOFI	Nop	dot product	needed tol
bin_LJ/1.1	82	D3d	12	S6	6	1.00000	0.024
glue_Al	70	C2v	4	C2	2	1.00000	0.0047
glue_Al	79	C2v	4	Cs	2	0.99984	0.0908
glue_Al	96	C2v	4	C2	2	1.00000	0.0432
glue_Al	134	C2v	4	C2	2	1.00000	0.0589
glue_Al	183	Cs	2	C1	1	1.00000	0.0609
gupta/Co	174	Cs	2	C1	1	1.00000	0.0014
gupta/Co	175	Cs	2	C1	1	1.00000	0.0036
gupta/Co	179	Cs	2	C1	1	1.00000	0.0021
gupta/Co	183	C2v	4	C2	2	1.00000	0.0013
gupta/Co	184	Cs	2	C1	1	1.00000	0.0020
murrel-mottram/Na	40	Cs	2	C1	1	1.00000	0.0032
murrel-mottram/Na	78	C2	2	C1	1	1.00000	0.0116
murrel-mottram/Na	83	D3	6	C1	1	1.00000	0.0159
murrel-mottram/Na	92	Т	12	C1	1	0.98969	0.0195
murrel-mottram/Na	107	C2	2	C1	1	1.00000	0.0067
murrel-mottram/Na	111	C5	5	C1	1	1.00000	0.0015
murrel-mottram/Na	132	Cs	2	C1	1	1.00000	0.0078
murrel-mottram/Na	153	C3v	6	C1	1	1.00000	0.0026
murrel-mottram/Na	157	C2v	4	C1	1	1.00000	0.0038
murrel-mottram/Na	180	Ci	2	C1	1	1.00000	0.0046
murrel-mottram/Na	216	Т	12	C1	1	0.95174	0.0032
murrel-mottram/Na	222	C3	3	C1	1	1.00000	0.0024
murrel-mottram/Na	318	Cs	2	C1	1	1.00000	0.0012
murrel-mottram/Na	321	Cs	2	C1	1	1.00000	0.0017
murrel-mottram/Na	324	Cs	2	C1	1	0.99996	0.0056
murrel-mottram/Na	326	Cs	2	C1	1	1.00000	0.0012
murrel-mottram/Na	327	C2v	4	Cs	2	1.00000	0.0020

Table S6: Cases of higher-order PG obtained by libmsym(tol = "medium") than SOFI(tol = 0.001). The column labelled "needed tol" indicates the value of tol such that SOFI(tol) retrieves the same PG as libmsym.



Figure S5: Comparison of libmsym(tol = "loose") with (left) SOFI(tol = 0.001), and (right) SOFI(tol = 0.05).

4 Discussion

The tolerance value as defined and used by SYVA, SymMol, and SOFI is based on real distances between the atoms. Thus, such value can scale with the scale of the structure (interatomic distances). As noted in the main article of SOFI, as a rule of thumb, the tolerance value can be chosen as up to about half the nearest neighbor distance. In all the structures included in the present comparison test, the nearest neighbor distance is well beyond the used tolerance values tol = 0.001 and tol = 0.05. This comparison test does not go deeper into investigation of the tolerance value, or its relationship to the nearest neighbor distance. A preprocessing procedure to determine the largest sensible tolerance value could potentially be very useful for these algorithms, since it could be used to determine the highest-order PG of a structure, from which the subgroups with a more stringent tolerance could easily be extracted by a postprocessing.

Throughout the test, we observe minor differences in the values of distortion (i.e. score, or distance), in terms of the distance value, for the symmetry operations reported by different algorithms (where the data is available). These could be explained by the different ways algorithms find and set the axes of each symmetry operation, which could result in minor differences in the actual matrix representation of the operation, which in turn leads to small differences in the symmetry-transformed structures, and thus slightly different values of the distance computed between the original, and the symmetry-transformed structure.

It appears that SYVA and libmsym algorithms do not attempt to deal with incomplete groups (in the sense

set	struc name	libmsym	Nop	SOFI	Nop	dot product	needed tol
bin_LJ/1.15	71	Cs	2	C1	1	0.95403	0.27549
C60	12	C5v	10	Cs	2	1.00000	0.2268
finnis-sinclair/Mo	8	D2d	8	C2v	4	1.00000	0.0590
finnis-sinclair/Mo	26	Td	24	S4	4	0.81061	0.1886
finnis-sinclair/Mo	27	Cs	2	C1	1	1.00000	0.1999
finnis-sinclair/Mo	29	C2v	4	C2	2	1.00000	0.2743
finnis-sinclair/Mo	31	C3	3	C1	1	0.99905	0.0409
finnis-sinclair/Mo	41	Cs	2	C1	1	0.99977	0.2409
finnis-sinclair/Mo	48	C3v	6	C3	3	1.00000	0.1860
glue_Pb	8	D2d	8	C2v	4	1.00000	0.0426
glue_Pb	26	C2v	4	Cs	2	1.00000	0.5462
glue_Pb	98	Cs	2	C1	1	0.76817	0.2175
glue_Al	70	C2v	4	C2	2	1.00000	0.0047
glue_Al	77	C6v	12	C3v	6	1.00000	0.0905
glue_A1	96	C2v	4	C2	2	1.00000	0.0432
gupta/Co	179	Cs	2	C1	1	1.00000	0.0021
gupta/Co	184	Cs	2	C1	1	1.00000	0.0020
gupta/Co	189	Cs	2	C1	1	1.00000	0.0011
gupta/Na	38	Oh	48	Th	24	0.70421	0.1677
morse	11D	C2v	4	Cs	2	0.99983	0.0463
morse	12C	C5v	10	Cs	2	1.00000	0.0767
murrel-mottram/Na	89	C3	3	C1	1	0.99991	0.0110
murrel-mottram/Na	92	Т	12	C1	1	0.98969	0.0195
murrel-mottram/Na	104	C2	2	C1	1	0.99999	0.0267
murrel-mottram/Na	119	Cs	2	C1	1	0.99992	0.0216
murrel-mottram/Na	132	Cs	2	C1	1	1.00000	0.0078
murrel-mottram/Na	151	Cs	2	C1	1	0.99839	0.0087
murrel-mottram/Na	152	Cs	2	C1	1	1.00000	0.0026
murrel-mottram/Na	153	C3v	6	C1	1	1.00000	0.0026
murrel-mottram/Na	154	Cs	2	C1	1	1.00000	0.0015
murrel-mottram/Na	156	Cs	2	C1	1	0.99810	0.0095
murrel-mottram/Na	207	C3	3	C1	1	1.00000	0.0035
murrel-mottram/Na	216	Т	12	C1	1	0.95174	0.0033
murrel-mottram/Na	318	Cs	2	C1	1	1.00000	0.0012
murrel-mottram/Na	319	C3v	6	Cs	2	1.00000	0.0434
murrel-mottram/Na	321	Cs	2	C1	1	1.00000	0.0017
murrel-mottram/Na	324	Cs	2	C1	1	0.99996	0.0056

Table S7: Cases of higher-order PG obtained by libmsym(tol = "loose") than SOFI(tol = 0.001). The column labelled "needed tol" indicates the value of tol such that SOFI(tol) retrieves the same PG as libmsym.

	SY	VA	Sym	Mol	I	libmsym		so	FI
set	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05
bin_LJ/1.05	0	0	3	3	0	1	6	0	0
bin_LJ/1.1	0	0	2	2	1	2	11	0	0
bin_LJ/1.15	0	0	2	2	0	2	13	0	0
bin_LJ/1.2	0	0	4	3	0	0	11	0	0
bin_LJ/1.25	0	0	3	4	0	3	21	0	0
bin_LJ/1.3	0	0	2	3	0	2	18	0	0
C60	0	0	3	2	0	4	7	0	0
C60_pacheco	0	92	1	1	0	3	24	0	0
dzugutov	0	0	1	0	0	0	16	0	0
dzugutov_mod	0	0	4	3	2	20	64	0	0
finnis-sinclair/Fe	0	0	2	2	0	1	9	0	0
finnis-sinclair/Mo	0	0	1	1	0	5	18	0	0
glue_Pb	1	13	5	3	0	5	19	0	0
glue_Al	0	0	4	3	1	12	37	0	0
gupta/Cd	0	1	0	0	0	2	8	0	0
gupta/Co	1	1	9	9	1	20	62	0	0
gupta/Na	0	2	20	21	6	48	142	0	0
gupta/Pb	0	2	4	3	0	5	31	0	0
gupta/Zn	0	1	1	0	0	1	8	0	0
LJ	0	0	8	8	0	11	36	0	0
morse	0	2	12	12	0	13	58	0	0
murrel-mottram/Na	0	132	13	12	9	57	100	0	0
NaCl_N/welch	0	21	0	0	0	0	6	0	0
NaCl_N/CBM	0	19	0	0	0	0	4	0	0
QLJ	0	0	0	0	0	3	6	0	0
sutton_9_6	0	2	2	3	0	3	17	0	0
sutton_10_8	0	1	1	1	0	2	16	0	0
sutton_12_6	0	1	5	6	0	2	14	0	0
total	2	290	112	107	20	227	782	0	0

Table S8: The count of failures of each algorithm and tolerance value used. Failures are counted only for cases when the output of an algorithm actually reports a failure, or the program crashes. For SYVA, the count does not include structures with more than 250 atoms. For SymMol the count includes cases of timed-out computations.

of group completeness), but rather just report a failure. On the other hand, it is possible that SymMol performs combinations of elements with the goal of group completeness. We have not found a routine explicitly dedicated to that in SymMol, but we also did not spend much time investigating the source code. In SOFI, the incomplete groups are explicitly labelled with + or - signs, which are related to the number of actual elements, and the expected number of elements for a PG identified via flowchart. These cases can optionally be explicitly made into complete groups, via combinations of the symmetry elements.

The comparison tests performed in this paper show that the developed SOFI algorithm is capable of identifying the PG symmetry in atomic structures. Among all the structures and tolerance values included in the test, there is no case of failure of SOFI, contrary to other algorithms (See Tab. S8). In all cases of disagreement between algorithms, SOFI is capable to find a PG of the same order, or higher, when computed with an appropriate tolerance value.

5 All results

The following Tables contain the results by each algorithm used, at each tolerance value, for each structure in the dataset. The first column reports the exact name of the structure as it appears in the dataset, the column marked "diff" contains an exclamation mark (!) if there is a disagreement between the algorithms, and the letter "M" if the PG assignment changes with raising the threshold value.

They are separated by dataset, as follows. Bin LJ results in Tab. S9, S10, S11, S12, S13, and S14. C60 and C60-Pacheco results in Tab S15, and S16. Dzugutov and Dzugutov_mod results in Tab. S17, S18, S19, and S20. Finnis-Sinclair results in Tab S21 and S22. Glue results in Tab S23, and S25. Gupta results in Tab S27, S28, S29, S30, S31, S32, S33, S34, S35, S36, S37, and S38. LJ results in Tab. S39, and S40. Morse results in Tab S41, S42, S43, and S44. Murrel-Mottram in Tab S45, S46, S47, S48. NaClN results in Tab. S49, and S50. Quantum LJ results in Tab. S51. Sutton results in Tab S52, S53, and S54.

	SY	VA	Sym	Mol		libmsym		SO	FI		
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
5	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
6	D4h	D4h	D4h	D4h	D4h	D4h	D4h	D4h	D4h		1.00000
7	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
8	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
9	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
10	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
11	C2v	C2v	C2v	C2v	C2v C5	C2v	C2v	C2v	C2v		1.00000
12	Cov	Cov	Cov	Cov	Cov	Cov	Cov	Cov	Cov		1.00000
13	- In CD	In	In	In	In Cla	In	In	In	In		0.99906
14	C3v	C3v	C3V	C3V	C3v	C3v	C3v	C3v	C3v		1.00000
16	Cs	Ca	Cs	Cs	Ca	Cs	Cs	Cs	Ca		1.00000
17	Cav	Cav	C3v	Cav	Cav	Cav	Cav	Cav	Cav		1.00000
18	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
19	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
20	C2v	C2v	C2v	C_{2v}	C_{2v}	C2v	C2v	C_{2v}	C_{2v}		1.00000
21	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	Cs	\mathbf{Cs}	Cs		1.00000
22	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
23	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
24	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
25	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
26	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.89941
27	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
28	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
29	D3h C9	D3h C0	D3h C0	D3h C9	D3h C9	D3h C9	-	D3h C9	D3h Co		1.00000
30	C2v	C2v	C2v	C2v	C1	C2v	C_{2v}	C2v	C2v		1.00000
32	Carr	Car	C2.	Car	C277	Carr	C2**	Carr	Carr		1.00000
33	C°	C=	C.	C=	C ²	C2v	C2v	C°	C°		1,00000
34	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1,00000
35	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1,00000
36	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
37	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
38	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}	\mathbf{Cs}	\mathbf{Cs}		1.00000
39	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
40	Cs	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	\mathbf{Cs}		1.00000
41	C2	C2	C2	C_2	C2	C2	C_2	C_2	C2		1.00000
42	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
43	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
44	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
45	C1	C-		C1		C1	C1	C1	C-		1.00000
40	CI	C1	CI	CI	CI	CI	C1	C1	C1		0.00000
47	C1	C1		C1		C1	C1	C1	Cl		0.00000
49	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
50	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
51	C2v	C2v	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v		1.00000
52	C3v	C3v	_	_	C3v	C3v	C3v	C3v	C3v		1.00000
53	C2v	C2v	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
54	C5v	C5v	C5	C5	C5v	C5v	-	C5v	C5v	!	1.00000
55	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	!	0.98791
56	C3v	C3v	-	-	C3v	-	C3v	C3v	C3v		1.00000
57	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
58	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
59	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
60	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
61	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C_{2v}	C_{2v}		1.00000
62	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
63		C1	C1	C1		C1	C1		C1		0.00000
64	Cs C=	Cs C-	Cs C-	Cs C-	Cs C-	Cs C-	Cs C=	Cs C-	Cs C-		1.00000
66	CI	C1	CI	CI	CI	CI	CI	CI	C1		0.00000
67	C	C		C		Ce	Ce	C	C		1.00000
68	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
69	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
70	C5v	C5v	C5	C5	C5v	C5v	-	C5v	C5v	!	1.00000
71	C5v	C5v	C5	C5	C5v	C5v	-	C5v	C5v	!	1.00000
72	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
73	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
74	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
75	Cs	Cs	Cs	Cs	Ci	Cs	Cs	Cs	Cs		1.00000
70		C-		C-		C1 C-	C-	C-	C-		1.00000
78	C1	C1	CI	C1		C1	CI	C1	C1		1.00000
79	C1	C1		C1		C1	C1	C1	C1		0.00000
80	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1,00000
81	C2v	C2v	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
82	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
83	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
84	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}		1.00000
85	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
86	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	Cs	Cs	\mathbf{Cs}	\mathbf{Cs}		1.00000
87	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	Cs		1.00000
88	C3v	C3v	-	_	C3v	C3v	C3v	C3v	C3v		1.00000
89	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
90	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
91	Ci	Ci	CI	CI	Ci	Ci	Ci	Ci	Ci		1.00000
92	Carr	Car	C2.	Car	C277	Carr	C1	Carr	Carr	,	1.00000
94	Cs	Cs Cs	Cs	Cs Cs	Cs	Cs	Cs	Cs Cs	Cs	l ,	1,00000
95	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1,00000
96	Cs	Cs	Cs	Cs	Cs	Čs	Cs	Cs	Cs		1.00000
97	C1	C1	C1	C1	Cĩ	C1	C1	C1	C1		0.00000
98	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
99	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
100	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000

Table S9: Dataset: $bin_LJ/1.05$, part 1.

	SY	VA	Sym	Mol		libmsym		so	FI		
name 5	0.001 D2b	0.05 D2b	0.001 D2b	0.05 D2b	'default'	'medium'	'loose'	0.001 D2b	0.05 D2b	diff	dot product
6	D3h D4h	D3h D4h	D3h D4h	D3h D4h	D3h D4h	D3h D4h	D3h D4h	D3h D4h	D3h D4h		1.00000
7	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
8	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
9	Cs C2v	Car	Car	Car	Cs C2v	Cs	Car	Cau	Car		1.00000
10	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
12	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
13	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih		0.95688
14	C3v Ca	C3v Ca	C3v Ca	C3v Ca	C3v	C3v Ca	C3v Ca	C3v Ca	C3v Ca		1.00000
16	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
17	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
18	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
19	D5h C2w	D5h C2w	D5h C2v	D5h C2v	D5h C2v	D5h C2v	D5h C2v	D5h C2w	D5h C2w		1.00000
20	C2v C2v	C_{2v}	C2v C2v	C_{2v}	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C_{2v}		1.00000
22	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
23	C3v	C3v	C3v	C3v	C3v	C3v	_	C3v	C3v		1.00000
24 25	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
26	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.99856
27	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	Cs		1.00000
28	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
29	C2v	C2v	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
31	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
32	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
33	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
34	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
36	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
37	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
38	Cov Cov	Cav	Con Con	C2v	Cs C2v	Cav	C2v	C2v	C2v		1.00000
40	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
41	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
42	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
43 44	C5v	C5v	C2v C5v	C5v	C5v	C2v C5v	C2v C5v	C5v	C5v		1.00000
45	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	!	0.99949
46	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
47	Cs C2v	Car	Cs C2v	Cau	Cs C2v	Cs C2	Cs C2v	Cs C2v	Car		1.00000
43	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
50	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	Cs		1.00000
51	D6d	D6d	C6	C6	D6d	D6d	-	D6d	D6d	!	1.00000
52 53	Cs C2	Cs C2	Cs C2	Cs C2	Cs C2	Cs _	 C2	Cs C2	Cs C2		1.00000
54	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
55	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
56 57	C2 Td	C2 Td	C2 Td	C2 Td	C2 Td	C2 Td	C2 Td	C2 Td	C2 Td		1.00000
58	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
59	C2v	C2v	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
60	C3v	C3v	-	-	C3v	C3v	_	C3v	C3v		1.00000
62	C1	C1	C1	C1		C1	C1	C1	C1		0.88139
63	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
64	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
65 66	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1		0.00000
67	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
68	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	\mathbf{Cs}	Cs	Cs		1.00000
69	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
70	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
72	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	\mathbf{Cs}	Cs	Cs		1.00000
73	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
74 75	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs Cs	Cs		1.00000
76	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
77	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
78	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
79	Cs C2	Cs C2	Cs C2	Cs C2	Cs C2	Cs C2	_	Cs C2	Cs C2		1.00000
81	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
82	S6	D3d	S6	S6	-	D3d	-	S6	D3d	!M	1.00000
83	C1 C1	C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1		0.00000
85 85	C1	C1	C1	C1		C1	C1		C1		0.00000
86	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
87	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
68 89	C1	C1	C1	C1		C1	C1		C1		0.00000
90	Cs	Cs	Cs	Ċs	Cs	Cs	Cs	Cs	Ċs		1.00000
91	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
92	C1	C1		C1		C1	C1		C1		0.00000
94	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
95	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v	C_{2v}		1.00000
96 97	C1 C1	C1	C1 C1	C1	C1 C1	C1	C1	C1 C1	C1		0.00000
98	C1	C1		C1	C1	C1	C1		C1		0.00000
99	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
100	C1	C1	C1	C1	C1	C1	C1	C1	C1	I	0.00000

Table S10: Dataset: $bin_LJ/1.1$, part 1.

	SY	VA	Sym	Mol		libmsym		SO	FI		
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
5	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
6	D4h	D4h	D4h	D4h	D4h	D4h	D4h	D4h	D4h		1.00000
7	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
8	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
9	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
10	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
11	C3v	C3v	-	_	C3v	C3v	C3v	C3v	C3v		1.00000
12	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
13	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih		0.91992
14	C3v	C3v	C3v	C3v	C3v	_	C3v	C3v	C3v		1.00000
15	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C_{2v}	C_{2v}		1.00000
16	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
17	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
18	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
19	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
20	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
21	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
22	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
23	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
24	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
25	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
26	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.94640
27	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
28	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
29	D3h	D3h	D3h	D3h	D3h	D3h	-	D3h	D3h		1.00000
30	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
31	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
32	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
33	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	\mathbf{Cs}	Cs	Cs		1.00000
34	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
35	C3v	C3v	C3v	C_{3v}	C3v	C3v	C3v	C3v	C_{3v}		1.00000
36	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
37	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
38	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
39	C2v	C2v	C2v	C2v	C2v	C_{2v}	C_{2v}	C2v	C2v		1.00000
40	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
41	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
42	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
43	C2v	C2v	C2v	C2v	C2v	C2v	-	C_{2v}	C2v		1.00000
44	C5v	C5v	C5	C5	C5v	C5v	_	C5v	C5v		1.00000
45	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	!	0.99851
46	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	_	C2v	C_{2v}		1.00000
47	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
48	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
49	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
50	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}	C2v	C2v		1.00000
51	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
52	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
53	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
54	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
55	CI	CI		CI		CI	CI		CI		0.00000
56	C2	C2	C2 C1	C2	C2	C2	C2	C2 C1	C2		1.00000
57	CI	CI		CI		CI	CI		CI		1.00000
58	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs C1		1.00000
59	CI	CI		CI		CI	CI		CI		1.00000
61	C1	C2	C1	C2	C1	C1	C2		C2		1.00000
62		Ca				Ca	Ca		Ca		1.00000
62	Ca	Ca	Ca	Ca	Ca	Ca	Ca	Ca	Ca		1.00000
64	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
65	Ce	Ce	Ce	Ce	C	C	Ce	Ce	Ce		1.00000
66	CI	C1	C1	C1	C1	C1	CI	C1	C1		0.00000
67	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
68	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
69	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
70	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
71	C1	C1	C1	C1	C1	C1	Cs	C1	C1	1	0.00000
72	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
73	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
74	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
75	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
76	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
77	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
78	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
79	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
80	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
81	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
82	D2h	D2h	D2h	D2h	D2h	D2h	D2	D2h	D2h	!	1.00000
83	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
84	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
85	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
86	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
87	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
88	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
89	Cs	Cs	Cs	Cs	Cs	Cs		Cs	Cs		1.00000
90	C1	C1	C1	C1		C1	C1		C1		0.00000
91	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
92	C2h	C2h	C2h	C2h	C2h		-	C2h	C2h		1.00000
93		CI		C1		01	_		C1		0.00000
94		C1 C		C1		C1	Ci		C1 C		0.00000
95	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
96		C1		C1		C1	C1		C1		0.00000
97	C1 C2	C1		C1		C1	-		C1		0.00000
98	C2	C2	C2	C2	C2	C2	_		C2		1.00000
99	C1 D2	C1	C1 D2	C1		C1	C1		C1	Ι.	0.00000
100	103	13	1 13	13	1 13	03	U1	1 13	13	1 1	1.00000

Table S11: Dataset: bin_LJ/1.15, part 1.

	SY	VA	Sym	Mol		libmsym		SC	FI		
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001 Dat	0.05	diff	dot product
6	D3fi D4h	D3h D4h	D3h D4h	D3fi D4b	D3h D4h	D3h D4h	D3h D4h	D3n D4b	D3fi D4b		1.00000
7	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
8	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
9	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
10	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
11	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
12	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
13	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
14	C3v C2w	C3v C2w	C3v C2v	C3v C2v	C3v C2v	C3v C2··	C3v C2v	C3v C2v	C3v C2w		1.00000
10	C2V	C2V	C2V	C2V	C2V	C2V	C2V	C2V	C2V		1.00000
17	C_2	C_2	C2	C_2	C2	C2	-	C2	C_2		1.00000
18	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
19	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
20	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
21	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
22	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
24	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
25	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
26	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
27	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
28	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
29	C1	C1	Cs	C1	Cs C1	Cs C1	Cs C1	C1	C1		0.00000
31	C1	C1	C1	C1		C1	C1	C1	C1		0.00000
32	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
33	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}		1.00000
34	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
35	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
36	Ca	Ca	Ca	Ca		Cs Ca	Cs		Ca		1.00000
38	C1	C1	C1	C1		C1	C1	C1	C1		0.00000
39	C5v	C5v	C5	Č5	C5v	C5v	C5v	C5v	C5v	!	1.00000
40	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
41	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}		1.00000
42	C3v	C3v	_	-	C3v	C3v	C3v	C3v	C3v		1.00000
43	C2v C5v	C2v C5v	C2v C5	C2v C5	C2v C5v	C2v C5v	-	C2v C5v	C2v C5v		1.00000
44	Th	Th	Ci	Ci	Ih	Th	Ib	Th	Th		0.95604
46	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	_	C2v	C_{2v}		1.00000
47	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	Cs		1.00000
48	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
49	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
50	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C_{2v}	C2v	C_{2v}		1.00000
52	Ce	C		C.		Ce	Ce		Ce		1.00000
53	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
54	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
55	C5v	C5v	C5	C5	C5v	C5v	-	C5v	C5v	!	1.00000
56	D5h	D5h	C5	C5	D5h	D5h	-	D5h	D5h	!	1.00000
57	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
58 59	C2V Ce	C2V	C2V Ce	C2V	C2V	C2V	_	C2V Ce	C2V Ce		1.00000
60	C1	C1	-	C1		C1	C1	C1	C1		0.00000
61	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
62	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
63	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
64	C1 C1	C1	C1 C1	C1	C1 C1	C1	C1	C1	C1		0.00000
66	Ce	C		C.		Ce	Ce		Ce		1.00000
67	C1	C1	C1	C1		C1	C1	C1	C1		0.00000
68	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
69	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
70	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
71	Cs C1	Cs	Cs	Cs C1	Cs	Cs C1	Cs	Cs	Cs C1		1.00000
73	C1	C1		C1		C1	C1		C1		0,00000
74	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
75	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	\mathbf{Cs}	Cs	\mathbf{Cs}		1.00000
76	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}		1.00000
77	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
78		C1		C1					C1		0.00000
79 80	Cs	Cs	Cs	Cs		Cs	Cs		Cs		1.00000
81	Cs	Cs	Cs	Cs	Cs Cs	Cs	Cs	Cs	Cs		1.00000
82	D2h	D2h	D2h	D2h	D2h	D2h	D2	D2h	D2h	!	1.00000
83	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
84	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
85	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
86 87		C1		C1			C1		C1		0.00000
88	C1	C1		C1		C1	C1		C1		0.00000
89	Cs	Ċs	Cs	Cs	Cs	Ċs	Cs	Cs	Cs		1.00000
90	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
91	C3v	C3v	-	-	C3v	C3v	-	C3v	C3v		1.00000
92	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
93		C1		C1			C1		C1		0.00000
94 95	C1	C1		C1		C1	C1		C1		0,00000
96	C1	Č1	C1	Č1	C1	C1	C1	C1	Č1		0.00000
97	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
98	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
99	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
100	C1	C1	C1	C1	C1	C1	C1	C1	C1	I	0.00000

Table S12: Dataset: $bin_LJ/1.2$, part 1.

	SY	VA	Sym	Mol		libmsym		SO	FI		
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
5	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
6	D4h	D4h	D4h	D4h	D4h	D4h	D4h	D4h	D4h		1.00000
7	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
8	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
9	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
10	D3h	D3h	D3h	_	D3h	_	D3h	D3h	D3h		1.00000
11	C2	C2		C2		C2 C-	C2		C2		1.00000
12	C5v	C5v	CS	CS	C5v	C5r	C5v	C5v	CS		1.00000
14	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
15	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
16	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
17	$\tilde{C2}$	C_2	C2	C_2	C2	$\tilde{C2}$	_	C2	C_2		1.00000
18	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
19	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
20	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
21	C2	C2	C2	C2	C2	C_2	C2	C2	C2		1.00000
22	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
23	C2v	C2v	C2v	C_{2v}	C2v	C_{2v}	_	C2v	C2v		1.00000
24	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
25	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
26	C3v	C3v	_	_	C3v	C3v	C3v	C3v	C3v		1.00000
27	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
28	Can	Con	Ca	Carr	Ca	Ca	Con	Ca	Con		1.00000
29	C2V	C1	C2V	C2V	C1	C2V	C2V	C2V	C1		0.00000
31	C1	C1		C1		C1	C1		C1		0.00000
32	Cs	Cs.	Cs	Cs.	Cs	Cs	Cs	Cs	Cs		1,00000
33	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
34	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
35	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
36	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	Cs		1.00000
37	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	\mathbf{Cs}		1.00000
38	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
39	C5v	C5v	C5	C5	C5v	C5v	C5v	C5v	C5v	!	1.00000
40	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
41	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}		1.00000
42	C3v	C3v	_	_	C3v	C3v	C3v	C3v	C3v		1.00000
43	C_{2v}	C2v	C2v	C_{2v}	C2v	C2v	-	C2v	C2v	.	1.00000
44	USV	USV	C5	C5	USV TL	Cov	TL.	USV Th	USV		1.00000
40	C2v	Con	Car	Car		C2v	m	Car	CON		1.00000
40	C2V	C2V	C2V	C2V	C2V	C2V	 C=	C2V	C2V		1.00000
47	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
40	C1	C1	C1	Cl	C1	C1	CI	CI	C1		0.00000
50	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
51	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
52	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
53	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
54	D5h	D5h	C5	C_{5}	D5h	D5h	-	D5h	D5h	!	1.00000
55	C5v	C5v	C5	C5	C5v	C5v	-	C5v	C5v	!	1.00000
56	D5h	D5h	C5	C5	D5h	D5h	-	D5h	D5h	!	1.00000
57	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
58	C2v	C2v	C2v	C_{2v}	C2v	C_{2v}	_	C2v	C2v		1.00000
59	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
60	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
61	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
62	D3h C2	D3h Ca	D3h	D3h	D3h Ca	D3h C2	-	D3h C2	D3h C9		1.00000
64	Dab	D2h	Dah	Dap	Dah	Dap	—	Dab	Dap		1.00000
65	Ce	Ce	Ce	C	Ce	Ce	C.		C.		1.00000
66	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
67	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
68	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
69	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
70	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
71	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
72	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
73	CI	CI		CI		CI	CI		CI		0.00000
(4) 75		CI		CI		C1	CI		CI		0.00000
70	C	Ca		Ca		Ca	Ca		Ca		1.00000
70	C1	C1	C1	C1		C1	C1	C1	C1		0.00000
78	C2v	C^{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1,00000
79	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1,00000
80	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
81	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	Cs		1.00000
82	Cs	Cs	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	-	Cs	\mathbf{Cs}		1.00000
83	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
84	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}		1.00000
85	C2v	C2v	C2v	C_{2v}	C_{2v}	-	-	C2v	C2v		1.00000
86	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
87	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	-	C2v	C_{2v}		1.00000
88	Co	Co	Co	Co	Co	Cs C2	-	Com	Com		1.00000
09	C2V	Cav	C2V C2	C2V C2	Ca	Ca	_		C2v		1.00000
91	C2v	C2v	C2v	C2v	C27	_	_	C2v	C2v		1.00000
92	C1	C1	C1	C1	C1	 C1	C1	C1	C1		0.00000
93	C1	Č1	C1	C1	C1	Č1	Č1	C1	C1		0.00000
94	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
95	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
96	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
97	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
98	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
99	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
100	C1	C1	C1	C1	C1	C1	C1	C1	C1	I	0.00000

Table S13: Dataset: bin_LJ/1.25, part 1.

	SY	VA	Sym	Mol		libmsym		SO	FI		
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
5	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
6	D4h	D4h	D4h	D4h	D4h	D4h	D4h	D4h	D4h		1.00000
7	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
8	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
9	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
10	D3h	D3h	D3h	-	D3h	D3h	D3h	D3h	D3h		1.00000
11	D4d	D4d	S8	S8	D4d	D4d	D4d	D4d	D4d	!	1.00000
12	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
13	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
14	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
15	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
16	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
17	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
18	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
19	Don	Don	Don	Don	Don	Don	Don	Don	Don		1.00000
20	Cs	Ci	CI	Cs	Cs	Cs	CI	Cs	Cs		1.00000
21		Ca		C		Ca		C	Ca		1.00000
22	Dah	D2h	Dah	Dap	Dap	Dap	Dab	Dap	D2h		1.00000
20	Ce	Ce	Ce	Ce	Ce	Ce	Ce	Ce	Ce		1.00000
25	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
26	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
27	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
28	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
29	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
30	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
31	Č1	C1	Č1	Č1	Č1	Č1	Č1	C1	C1		0.00000
32	C2	C_2	C2	C_2	C2	C2	C_2	C2	C_2		1.00000
33	Cs	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs		1.00000
34	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
35	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
36	Cs	Cs	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	\mathbf{Cs}		1.00000
37	Cs	Cs	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	\mathbf{Cs}		1.00000
38	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
39	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
40	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}		1.00000
41	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
42	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
43	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
44	C5v	C5v	C5	C5	C5v	-	-	C5v	C5v	!	1.00000
45	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	!	0.96564
46	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
47	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
48	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
49	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
50	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
51	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
52	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
53	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
54	D5h	D5h	C5	C5	D5h	D5h	-	D5h	D5h		1.00000
55	C5v	C5v	C5	C5	C5v	C5v	-	C5v	C5v		1.00000
56	D5h	D5h	C5	C5	D5h	D5h	-	D5h	D5h	! !	1.00000
57	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
58	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
59	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
60	C2v	C2V	C2V	C2V	C2V	C2v	C2v	C2V	C2V		1.00000
62	Dah	D2h	Dah	Dap	Dap	Dap	—	Dap	D2h		1.00000
63	C3v	C3v	531	50	C3v	C3v	_	C3v	C3v		1.00000
64	C	C	C.	C.	C	Ce	C.	C3V	C.		1.00000
65	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
66	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.89647
67	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
68	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
69	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
70	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
71	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
72	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
73	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
74	C2v	C2v	C2v	C2v	C2v	C_{2v}	C_{2v}	C2v	C2v		1.00000
75	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
76	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
77	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
78	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C_{2v}	C_{2v}		1.00000
79	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
80	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
81	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
82	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
83		C1 C		CI		C1	01		C1 C		0.00000
84	Ci	Cs	Cs	CI	Ci	Cs	Cs	Ci	CI		1.00000
80		Ca		Ca	C1	C1	C1 C2-	Ca	Ca		1.00000
80	C2v	C2v	C2v	C2v	C-	C2v	C_{2v}	C2v	C2v		1.00000
87	Deb	Deb	Deb	US Deb	Deb	US Deb	_	Deb	US Deb		1.00000
89	C.	C	C.	C	C	Ce	_	C.	Ce		1.00000
90	Corr	Corr	Co.	Corr	Car	Carr	_	Corr	Carr		1.00000
01	C2v	C2v	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
92	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
93	C2	C2	C2	C2	C2	C2	_	C2	C2		1 00000
94	C1	C1	CI	C1		C1	C1	C1	C1		0.00000
95	C2v	C^{2v}	C2v	C_{2v}	C2v	_	_	C_{2v}	C_{2v}		1,00000
96	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
97	C1	CI	C1	CI	C1	C1	C1	C1	C1		0.00000
98	C1	C1	C1	CI	C1	C1	C1	C1	C1		0,00000
99	C1	Č1	C1	C1	Ci	Č1	Č1	C1	C1		0.00000
100	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000

Table S14: Dataset: $bin_LJ/1.3$, part 1.

name	0.001	VA 0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
5	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
6	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		1.00000
7	D5h Ca	D5h Ca	D5h Ca	D5h Ca	D5h Ca	D5h Ca	D5h Ca	D5h Ca	D5h Ca		1.00000
9	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
10	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
11	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	\mathbf{Cs}	Cs	Cs		1.00000
12	Cs	Cs	Cs	Cs	Cs	-	C5v	Cs	Cs	!	1.00000
13	Ih C2v	Th C2v	In C2v	Th C2v	Ih C2v	Ih C2v	Ih C2v	1h C2v	Ih C2v		0.98239
15	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
16	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
17	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
18	D5h C2m	D5h C2m	C5 C2w	C5 C2···	D5h C2m	D5h C2m	D5h C2m	D5h C2m	D5h C2m	!	1.00000
20	C2v C2v	C_{2v}	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C_{2v}	C2v C2v	C_{2v}		1.00000
21	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
22	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
23	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
24	C2v C3v	C2v C3v	C2v C3v	C2v C3v	C2v C3v	C2v C3v	C2v C3v	C2v C3v	C2v C3v		1.00000
26	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
27	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
28	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
29 30	C2v C1	C_{2v}	C2v	C_{2v}	C2v C1	C2v C1	C2v C1	C2v C1	C_{2v}		1.00000
31	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
32	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
33	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
34	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
35	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1		0.00000
37	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
38	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		0.99846
39	C4v	C4v	C4	C4	C4v	C4v	C4v	C4v	C4v	!	1.00000
40	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2	C2v C2v	C2v C2v		1.00000
41	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
43	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
44	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
45	Cs	Cs C-	Cs	Cs C-	Cs	Cs C-	Cs	Cs C-	Cs		1.00000
40	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
48	C2v	C2v	C2v	C2v	C2v	C_{2v}	C_{2v}	C2v	C2v		1.00000
49	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	\mathbf{Cs}	Cs	Cs		1.00000
50	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
51	Cov Cov	Cav	Con Con	C2v	C2v	Cav	C21	C2v	C2v		1.00000
53	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
54	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
55	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
50 57	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
58	D3h	D3h	D3h	D3h	D3h	D3h	_	D3h	D3h		1.00000
59	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.99983
60	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
62	C3v C1	C3v C1	C3v C1	C3v C1				C3v C1	C3v C1		1.00000
63	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
64	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
65	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
66 67	Cs	Cs	Cs	Cs	Cs	Cs	Cs C2v	Cs	Cs		1.00000
68	C2v C3v	C3v		C2v	C3v	C2v C3v	C2v C3v	C3v	C3v		1.00000
69	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
70	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
71	C2v	C_{2v}	C2v C1	C_{2v}	C2v	C2v	C_{2v}	C2v	C_{2v}		1.00000
73	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
74	C5v	C5v	C5	C_{5}	C5v	-	-	C5v	C5v	!	1.00000
75	D5h	D5h	D5h	C5	D5h	-	-	D5h	D5h	!	1.00000
76	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Ι.	1.00000
78	C1	C1	C1	C1		C1	C1		C1	'	1.00000
79	D3h	D3h	-	_	D3h	D3h	D3h	D3h	D3h		1.00000
80	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000

Table S15: Dataset: C60, part 1.

name	SY 0.001	VA 0.05	Sym 0.001	Mol 0.05	'default'	libmsym 'medium'	'loose'	SO 0.001	FI 0.05	diff	dot product
3	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	um	1.00000
4	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.99800
5	D3h Oh	D3h Oh	D3h Oh	D3h Oh	D3h Oh	D3h Ob	D3h Oh	D3h Oh	D3h Oh		1.00000
7	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
8	Cs	\mathbf{Cs}	Cs	Cs	Cs	\mathbf{Cs}	\mathbf{Cs}	Cs	Cs		1.00000
9	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C_{2v}	C2v	C_{2v}		1.00000
10	C3v C2v	C3v C2v	C3v C2v	C3v C2v	C3v C2v	C3v C2v	C3v C2v	C3v C2v	C3v C2v		1.00000
12	C5v	C_{2v}	C5v	C_{2v}	C5v	C5v	C5v	C5v	C_{2v}		1.00000
13	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih		0.97445
14	C3v	-	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
15	C2v C2v	_	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C_{2v}		1.00000
17	C2v	-	C2v	C_{2v}	C2v	C2v	C_{2v}	C2v	C_{2v}		1.00000
18	D5h	-	C5	C5	D5h	D5h	D5h	D5h	D5h	!	1.00000
19	C2v C2v	_	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C_{2v}		1.00000
20	Cs	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
22	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
23	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
24 25	C3v	_	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
26	C2v	-	C2v	C2v	C2v	C2v	-	C2v	C_{2v}		1.00000
27	Cs	-	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	Cs		1.00000
28	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs D51	Cs		1.00000
30	C2v	_	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
31	C2v	-	C2v	C_{2v}	C2v	C2v	C_{2v}	C2v	C_{2v}		1.00000
32	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
33	C2v C1	_	C2v C1	C2v C1	C2v C1	C2v C1	C_{2v}	C2v C1	C2v C1		1.00000
35	C2v	_	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}		1.00000
36	C1	-	-	C1	C1	C1	C1	C1	C1		0.00000
37	C2v	-	C2v	C_{2v}	C2v	C2v	C_{2v}	C2v	C2v		1.00000
38 39	C4v	_	C4	C4	C4v	C4v	C4v	C4v	C4v		1.00000
40	C2v	-	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
41	C_{2v}	-	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}		1.00000
42	Cs C2v	-	Cs	Cs	Cs	Cs C2rr	Cs	Cs	Cs		1.00000
43	Cs	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
45	C2v	-	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
46	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
47	C2v C2v	_	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2V	C2v C2v	C2v C2v		1.00000
49	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
50	D3h	-	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
51 52	Cs C2v	_	Cs C2v	Cav	Cs C2v	Cs C2v	_	Cs C2v	Cs C2v		1.00000
53	Cs	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
54	C2v	-	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
55	C2v	-	C2v	C_{2v}	C2v	C2v	C_{2v}	C2v	C_{2v}		1.00000
57	C2v	_	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
58	D3h	-	D3h	D3h	D3h	D3h	-	D3h	D3h		1.00000
59	Td	-	Td	Td	Td	Td	Td	Td	Td		0.99667
60 61	Car	-	Car	Car	Car	Cs	Cs	Cau	Cau		1.00000
62	C1	_	C1	C1	C1 C1	C1	C1	C1	C1		0.00000
63	Cs	-	Cs	Cs	Cs	\mathbf{Cs}	-	Cs	Cs		1.00000
64	C2v C2v	-	C2v C2v	C2v C2v	C2v C2v	C2v C2v	-	C2v C2v	C_{2v}		1.00000
66	Cs Cs	_	Cs Cs	C ₂ v	C2V C5	Cs Cs	_	Cs Cs	C ₂ v		1.00000
67	C2v	-	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
68	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
70	Cs	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
71	C2v	-	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v		1.00000
72	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
73 74	Cs C5v	_	Cs C5	Cs C5	Cs C5v	Cs	Cs	Cs C5v	C5v	Ι,	1.00000
75	D5h	_	D5h	D5h	D5h	_	_	D5h	D5h	· ·	1.00000
76	Cs	-	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
77	C2v	-	C2v	C_{2v}	C2v	C2v	C_{2v}	C2v	C_{2v}		1.00000
78 79	D3h	_	D3h	-	D3h	D3h	-	D3h	D3h		1.00000
80	Cs	-	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
81	C2v	-	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C_{2v}		1.00000
82	C2v C2v	_	C2v C2v	C2v C2v	C2v C2v	C2v C2v	_	C2v C2v	C2v C2v		1.00000
84	C2v	_	C2v	C2v	C2v	C2v	_	C2v	C_{2v}		1.00000
85	C3v	-	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
86	C3v	-	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
87	Cs	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
89	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
90	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
91 02	C3v Ce	_	C3v Cs	C3v Cs	C3v	C3v	C3v	C3v Cs	C3v Cs		1.00000
93	Cs	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
94	Cs	-	Cs	Cs	Cs	\mathbf{Cs}	\mathbf{Cs}	Cs	\mathbf{Cs}		1.00000
95	C2v	-	C2v	C_{2v}	C2v	C2v	-	C2v	C_{2v}		1.00000
96 97	C1	_	C1	C1	Cs C1	Cs C1	Cs C1	C1	C1		1.00000
98	Cs	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
99	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}		1.00000
100	Td D5b	-	Td D5b	Td C ⁵	Td DEb	Td D5b	Td	Td D5b	Td D5b	,	0.97270
101	C2v	_	C2v	C_{2v}	C2v	C2v	_	C2v	C_{2v}	[:]	1.00000
103	Cs	-	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	\mathbf{Cs}		1.00000
104	C2v	-	C2v	C_{2v}	C2v	C2v		C2v	C_{2v}		1.00000
105	Us	-	Us	Us	l Us	Us	Cs		Us	I	1.00000

Table S16: Dataset: C60_pacheco, part 1.

		SY	VA	Sym	Mol		libmsym		so	FI		
-	name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
	3	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
	4	Dar	Td Dat	1.0	Dar	Td Dah	Td	Td	110	Td Dat		0.99481
	6	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
	7	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
	8	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}		1.00000
	9	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
	10	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C_{3v}		1.00000
	11	C2v	C2v C5w	C2v C5v	C2v	C2v C5v	C2v C5v	C2v C5v	C2v C5v	C2v		1.00000
	12	Th	Th	Ci	Ci	Th	Th	Th	Th	Th	1	0.99682
	14	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
	15	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
	16	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
	17	Cs C=	Cs C-	Cs C-	Cs C-	Cs C-	Cs C-	Cs Ca	Cs C-	Cs C-		1.00000
	10	D5h	D5h	C5	C5	D5h	D5h	D5h	D5h	D5h	, I.	1.00000
	20	C2v	C2v	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v		1.00000
	21	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
	22	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}		1.00000
	23	D3h	D3h	D3h	D3h	D3h	D3h	-	D3h	D3h		1.00000
	24	Co	Co	Cs	Co	Cs	Cs		Cs	Con		1.00000
	26	Cs Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs Cs		1.00000
	27	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}		1.00000
	28	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
	29	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
	30	C1 D5h	C1 DFL	C1 D5h	C1	C1 DFh	C1 DFL	C1	C1 DEL	C1 DEL		0.00000
	32	Cs	Cs	Cs	Cs	Cs	Cs	Cs.	Cs	Cs	·	1.00000
	33	D3d	D3d	S6	S6	D3d	D3d	-	D3d	D3d	!	1.00000
	34	C1	C1	C1	C1	C1	C1	-	C1	C1		0.00000
	35	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
	36	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	,	1.00000
	37	D6b D6b	D6P D6P	Deb	Deb	Deb	Dep	_	D6P D6P	D6D D6b	1	1.00000
	39	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
	40	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
	41	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
	42	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
	43	C1 C1	C1 C-	C1 C1	C1 C-		C1 C-	C1 C1		C1 C-		0.00000
	44	C2	C2	C2	C2	C2	C2	C1	C2	C2	,	1.00000
	46	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
	47	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
	48	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
	49	C1 C1	C1 C1		C1 C1		C1 C1	C1		C1 C1		0.00000
	50 51	C1	C1		C1		C1	C1		C1		0.00000
	52	C2	C2	C2	C2	C2	C2	-	C2	C2		1.00000
	53	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
	54	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
	55	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
	57	Cs Td	Cs Td	Cs Td	Cs Td	Cs Td	Cs Td	US Td	Cs Td	US Td		0.81200
	58	C2h	C2h	C2h	C2h	C2h	C2h	-	C2h	C2h		1.00000
	59	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
	60	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
	61	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
	62	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		1.00000
	64	C1	C1	C1	C1	C1	C1	C1		C1		0.00000
	65	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
	66	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}		1.00000
	67	D2d	D2d	S4	S4	D2d	D2d	_	D2d	D2d	!	1.00000
	69	C1	C1		C1		C1	C1		C1		0.00000
	70	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
	71	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
	72	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
	73	C1	C1		C1		C1	C1		C1		0.00000
	74	C	C		C		C	Ce		C		1.00000
	76	D3d	D3d	S6	S6	D3d	D3d	-	D3d	D3d	!	1.00000
	77	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	-	Cs	Cs		1.00000
	78	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
	79	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
	80	C1	C1	CI	Ci	Cs C1	Cs C1	C1	CI	C1		1.00000
	82	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
	83	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
	84	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
	85	C2	C2	C2	C_2	C2	C_2	-	C2	C2		1.00000
	86	D3	D3	D3	D3		D3			D3		1.00000
	88	C2	C2	C2	C2	C2	C2		C2	C2		1.00000
	89	C1	C1	C1	C1		C1	C1	C1	C1		0.00000
	90	C_2	C_2	C2	C_2	C2	C2	-	C2	C2		1.00000
	91	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
	92	D3	D3	D3	D3	D3	D3	C2	D3	D3	!	1.00000
	93 94	C1	C1		C1		C1	C1		C1		0.00000
	95 95	C1	C1	C1	C1		C1	C1		C1		0.00000
	96	Č1	Č1	Č1	Č1	či	či	C1	Č1	Č1		0.00000
	97	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
	98	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
	99	C1	C1		C1		C1	C1		C1		0.00000
	100	01	01		01		01	01		01	1	0.00000

Table S17:Dataset: dzugutov, part 1.

	SY	VA	Sym	Mol		libmsym		SO	FI		
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
3	D3h Td	D3h Td	D3h Td	D3h Td	D3h Td	D3h Td	D3h Td	D3h Td	D3h Td		1.00000
5	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
6	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
7	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
8	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
10	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
11	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
12	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
13	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1 00000
15	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
16	\mathbf{Cs}	\mathbf{Cs}	Cs	Cs	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs		1.00000
17	Cs	Cs C5v	Cs C5	Cs C5	Cs C5v	Cs C5v	Cs C5v	Cs	Cs C5v		1.00000
19	D5h	D5h	C5	C5	D5h	D5h	D5h	D5h	D5h	i	1.00000
20	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
21	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
22	Cs D3h	Cs D3h	D3h	Cs D3h	Cs D3h	Us D3h	Us D3h	Cs D3b	US D3h		1.00000
24	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
25	\mathbf{Cs}	\mathbf{Cs}	C1	Cs	Cs	Cs	Cs	\mathbf{Cs}	\mathbf{Cs}	!	1.00000
26	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.83025
27	Cs Cs	Cs Cs	Cs Cs	Cs Cs	C2V C5	Czv	- C2V	Cs Cs	Cs Cs		1.00000
29	D3h	D3h	D3h	D3h	D3h	D3h	-	D3h	D3h		1.00000
30	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
31	C2	C2	C2 C2	C2	C2	C2	C2	C2	C2		1.00000
32	C2V	C2V C1	C1	C1	C1	C2V	C1	C2V C1	C2V		0.00000
34	D2d	D2d	D2d	D2d	D2d	D2d	D2	D2d	D2d	!	1.00000
35	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
30 37	Cs Cs	C_{S}	Cs Cs	Cs Cs	Cs Cs	Cs Cs	02v	C_{S}	Cs Cs		1.00000
38	D6h	D6h	D6h	D6h	D6h	D6h		D6h	D6h		1.00000
39	C6v	C6v	C6	C6	C6v	C6v	C6v	C6v	C6v	!	1.00000
40	D6h C2	D6h C2	C6h C2	C6h C2	D6h C2	D6h		D6h C2	D6h C2	!	1.00000
41 42	C_{2v}	C_{2v}	C2v C2v	C_{2v}	C2v C2v	C_{2v}	C_{2v}	C_{2v}	C_{2v}		1.00000
43	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
44	\mathbf{Cs}	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}	\mathbf{Cs}	\mathbf{Cs}		1.00000
45	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
46	C2v Ce	C2v	C2v	C2v Ce	C2v	C2v C*	C2v C*	C2v Cs	C2v Ce		1.00000
48	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
49	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
50	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
51 52	C1	C1 C1		C1 C1		C1	C1	C1 C1	C1 C1		0.00000
53	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}		1.00000
54	\mathbf{Cs}	\mathbf{Cs}	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs		1.00000
55	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C_{2v}	C_{2v}		1.00000
57	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.80280
58	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
59	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
60	C3v C3v	C3v C3v	C3v C3v	C3v C3v	C3v C3v	C3v C3v	C3v C2v	C3v C3v	C3v C3v		1.00000
62	C3v Cs	Cs	Cs	Cs	Cs	Cs	Cs	C3v Cs	Cs		1.00000
63	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
64	\mathbf{Cs}	\mathbf{Cs}	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	\mathbf{Cs}		1.00000
65	C1 Cr	C1 C-	C1 C1	C1 C-	C1	C1	C1	C1	C1		0.00000
67	Cs	Cs	Cs	Cs	Cs	Cs		Cs	Cs		1.00000
68	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
69	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
70	C1	C1		C1 C1		CI	C1	C1	CI		0.00000
72	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
73	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
74 75	Cs C-	Cs C-	Cs C-	Cs C-	Cs C-	C1 C-	-	Cs C-	Cs C-	!	1.00000
70 76	D3d	D3d	S6	S6	D3d	D3d	_	D3d	D3d	1	1.00000
77	Cs	Cs	Cs	Cs	Cs		-	Cs	Cs		1.00000
78	C2h	C2h	C2h	C2h	-	_	-	C2h	C2h		1.00000
79 80	Cr Cr	C1 C2		C1 C2	Cs Cs	C1 Cs	C1 _	C1 Ce	C1 C2		1.00000
81	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
82	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
83	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
84 85	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1		0.00000
86	C1	C1	Ci	C1	C1	C1	C1	C1	Ci		0.00000
87	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
88	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
89 90	C27	C2v	C2v	C2v	C2w	C_{2v}	C1 _	C27	C2v		1.00000
91	Cs	Cs	Cs	Cs	Cs	Cs		Cs	Cs		1.00000
92	C2	C_2	C_2	C_2	C2	C_2	-	C2	C_2		1.00000
93	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
94 95	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	C2v Cs	Cs	Cs Cs	Cs Cs		1.00000
96	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	-	C2v	C_{2v}		1.00000
97	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
98	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
99 100	Ce Ce	C.		C.		Cs	Cs Cs	C.	C.		1.00000
101	Cs	Cs	Cs	Cs	Cs	Čs	Čs	Cs	Cs		1.00000
102	Cs	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs		1.00000
103	Cs	Cs	Cs	Cs	Cs C1	Cs	Cs	Cs	Cs		1.00000
104	C1	CI	CI	CI	C1	C1	C1	C1	CI		0.00000
106	C1	Č1	C1	Č1	C1	Č1	Č1	C1	Č1		0.00000
107	Cs	Cs	Cs	Cs	Cs	Cs		Cs	Cs		1.00000
108	C1	C1	C1 Cc	C1	C1 Ca	C1 Ca	C1	C1	C1		0.00000
109	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs	Cs Cs	Cs Cs		1.00000
111	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000

 Table S18:
 Dataset: dzugutov_mod, part 1.

	SY	VA	Syn	Mol	,	libmsym	,1,	SC 0.001)FI]	
112	C2h	C2h	C2h	C2h	C2h	C2		C2h	C2h	!	1.00000
113	C1	C1	C1 C1	C1	C1 C1	C1 C1	C1 C1	C1	C1		0.00000
114	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
116	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
118	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
119	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
120	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
122	Cs C-	Cs C=	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs C-	Cs C-		1.00000
123	C1	C1	C1	C1	C1 C1	C1	C1	C1	C1		0.00000
125	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
120	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
128 129	C1 D3d	C1 D3d	C1 56	C1 56	C1 D3d	C1 D3	C1	C1 D3d	C1 D3d	, I	0.00000
130	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
131	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		1.00000
133	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
134	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		1.00000
136	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
137	C1	C1	C1	C1	C1 C1	C1	C1	C1	C1		0.00000
139	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
140 141	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1		0.00000
141	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
143 144	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs		0.00000
145	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
146 147	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		1.00000
148	D3h	D3h	D3h	D3h	D3h	-	-	D3h	D3h		1.00000
149 150	C3v C2v	C3v C2v			C3v C2v	_	_	C3v C2v	C3v C2v		1.00000
151	C_{2v}	C_{2v}	C2v	C_{2v}	C2v C2v	-	-	C2v	C_{2v}		1.00000
152 153	Cs C2	Cs C2	Cs C2	Cs C2	Cs C2		_	Cs C2	Cs C2		1.00000
154	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
155 156	C_{2v}	C2v	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
157	C_{2v}	C_{2v}	C2	C_{2v}	C2v	C2v	-	C_{2v}	C_{2v}	!	1.00000
158 159	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs		1.00000
160	C2	C2	C2	C2	C2	-	-	C2	C_2		1.00000
161 162	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1	C1 C2v	C1 C2v	C1 C2v		0.00000
163	Cs	Cs	C1	Cs	Cs	-	-	Cs	Cs	!	1.00000
164 165	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs _	Cs Cs	Cs Cs		1.00000
166	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.83919
167 168	C3v C2v	C3v C2v	C2v	C_{2v}	C3v C2v	C3v C2v	C3v C2v	C3v C2v	C_{2v}		1.00000
169	C_{2v}	C_{2v}	C2v	C2v	-	C2v	C2v	C2v	C_{2v}		1.00000
170 171	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		Cs C1	Cs C1	Cs C1		1.00000
172	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
173 174	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		1.00000
175	\mathbf{Cs}	\mathbf{Cs}	Cs	Cs	Cs	Cs	-	\mathbf{Cs}	Cs		1.00000
176 177	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1		0.00000
178	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
179 180	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs		1.00000
181	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	\mathbf{Cs}	Cs	Cs		1.00000
182	C3V C1	C3V C1	C3V C1	C3V C1	C3V C1	_	C1	C3V C1	C3V C1		0.00000
184	D3h	D3h	D3h	C3h	D3h	D3h	-	D3h	D3h	!	1.00000
185	C1	C1	C1	C1	C1 C1	C1	C1	C1	C1	· ·	0.00000
187	Cs C-	Cs C=	Cs	Cs	Cs			Cs C-	Cs C-		1.00000
189	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
190 191	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	- C1	Cs C1	Cs C1		1.00000
192	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
193 194	Cs	Cs C	Cs C ²	Cs C°	Cs C ²	Cs C°	Cs	Cs C	Cs C°		1.00000
195	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
196 197	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	_	Cs Cs	Cs Cs		1.00000
198	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
199 200	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	C1	Cs C1	Cs C1		1.00000
201	C_2	C2	C2	C2	C2	-	-	C_2	C2		1.00000
202 203	Cs D3d	Cs D3d	Cs S6	Cs S6	Cs D3d	_ D3d	_	Cs D3d	Cs D3d		1.00000
204	C1	C1	C1	C1	C1	-	C1	C1	C1	. 	0.00000
205 206	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1	C1 C1	C1 C1		0.00000
207	C1	C1	C1	C1	C1	C1	_	C1	C1		0.00000
208 209	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1		0.00000
210	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
211 212	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 -	C1 Cs	C1 Cs		0.00000
213	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
214 215	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs		0.00000
216	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
217 218	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs C1	Cs Cs	Cs Cs	!	1.00000
219	C3v	C3v	C3v	C3v	C3v	C3v	-	C3v	C3v		1.00000
220 221	Cs C3v	Cs C3v	Cs C3v	Cs C3v	Cs C3v	Cs -	Cs -	Cs C3v	Cs C3v		1.00000 1.00000

 Table S19:
 Dataset: dzugutov_mod, part 2.

	SY	VA	Sym	Mol	I	libmsym		so	FI	I	I
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
222	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
223	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
224	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
225	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
226	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
227	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
228	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
229	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
230	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
231	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
232	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
233	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
234	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
235	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
236	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
237	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
238	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
239	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
240	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
241	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
242	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
243	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
244	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
245	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
246	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
247	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
248	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
249	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
250	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000

Table S20:	Dataset:	dzugutov_	_mod,	part 3.
------------	----------	-----------	-------	---------

	SY	VA	Sym	Mol		libmsym		SC	FI		
name	0.001 D2b	0.05 D2b	0.001 D2b	0.05 D2b	'default'	'medium'	'loose'	0.001 D2b	0.05 D2b	diff	dot product
4	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.72205
5	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
6	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		0.99353
7	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
8	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
9 10	C3v	C3v	C3v	C3v	C3v	C2v C3v	C3v	C3v	C3v		1.00000
11	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}	C2v	C2v		1.00000
12	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
13	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih		0.96549
14	C3v C2v	C3v C2v	C3v C2v	C3v C2v	C3v C2v	C3v C2v	C3v C2v	C3v C2v	C3v C2v		1.00000
16	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
17	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
18	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
19	D5h C0	D5h	C5	C5	D5h	D5h	D5h	D5h C0	D5h	!	1.00000
20	C2V	C2V	C2V	C2V	C1	C2V	C2V	C2V	C2V		0.00000
21	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
23	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
24	C2v	C2v	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
25	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
20	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1 00000
28	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
29	D3h	D3h	D3h	D3h	D3h	D3h	-	D3h	D3h		1.00000
30	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C_{2v}	C2v	C_{2v}		1.00000
31	Car	Car	Car	Car	Car	Car	Car	Car	Car		1.00000
33	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
34	D5h	D5h	C5	C5	D5h	D5h	D5h	D5h	D5h	!	1.00000
35	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
36	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
37	D6h	D6h	D6h	D6h	D6h	Us D6h	Cs	D6h	D6h		1.00000
39	C6v	C6v	C6	C6	C6v	C6v	C6v	C6v	C6v	!	1.00000
40	D6h	D6h	C6h	C6h	D6h	D6h	D6h	D6h	D6h	!	1.00000
41	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
42	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
43	C2v	C2v	C2v	C2v	C2v	C2v	Cav	C2v	C2v		1.00000
45	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
46	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}		1.00000
47	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	Cs		1.00000
48	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
49	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
51	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
52	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
53	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
55	D3n Ce	D3n Ce	D3n Ce	D3n Ce	D3n Ce	D3n Ce	C.	D3n Ce	D3n Ce		1.00000
56	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
57	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.97651
58	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
59	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}	C2v	C_{2v}		1.00000
60	C3v Td	C3v Td	- Td	- Td	C3v Td	C3v Td	C3v Td	C3v Td	C3v Td		1.00000
62	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
63	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
64	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
65	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C_{2v}	C2v	C_{2v}		1.00000
67	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
68	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
69	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	\mathbf{Cs}	Cs	Cs		1.00000
70	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
72	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
73	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
74	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
75	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs	.	1.00000
76	C6v	C6v	C6	C6	C6v	C6v	C6v	C6v	C6v		1.00000
78	D6h	D6h	D6h	D6h	D6h	D6h	_	D6h	D6h	l .	1.00000
79	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
80	C2	C2	C2	C2	C2	C_2	C1	C2	C2	!	1.00000
81	Cs	Cs	Cs	Cs	Cs		-	Cs	Cs	.	1.00000
82 83	C2v	C_{2v}	Cs	50 C2v	C2v	C2v	C2v	C2v	C_{2v}		1,00000
84	C2	C_2	C2	C_2	C2	C2	C2	C2	C2	· ·	1.00000
85	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
86	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
87		C1		C1		CI	C1		CI		0.00000
89	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
90	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
91	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
92	Cs C2v	Cs C2v	C2v	C2v		Cs C2v	Us C2v	Car	C2v		1.00000
94	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
95	C1	C1	C1	C1	Cĩ	C1	C1	C1	C1		0.00000
96	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
97	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
98				C1		C ¹	C ¹		C.		1.00000
100	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
			•		•						

Table S21: Dataset: finnis-sinclair/Fe, part 1.

	SY	VA	Sym	Mol		libmsym		SC	FI		
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
3	D3n Td	D3n Td	D3n Td	D3n Td	D3n Td	D3n Td	D3n Td	D3n Td	D3n Td		1.00000
5	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1 00000
6	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		1.00000
7	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
8	C2v	C2v	C2v	C2v	C2v	C2v	D2d	C2v	C2v	!	1.00000
9	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
10	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
11	C2V C5v	C2V C5v	C2V C5v	C2v C5v	C2V C5v	C2v C5v	C2V C5v	C2v C5v	C2v C5v		1.00000
13	Th	Th	Th	Th	Ih	Th	Th	Th	Th		0.98729
14	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
15	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
16	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
17	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
18	C1 DFL	C1 DFL	C1	C1	C1 D5h	C1 DEL	C1 DFh	C1 D5h	C1 D51	Ι.	0.00000
20	D31 D3	D31 D3	D3	D3	D31	D3n		D31 D3	D31 D3		1.00000
21	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
22	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
23	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
24	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
25	CI	CI		CI CI		C1 S4		CI CI	CI CI		0.00000
20	C1	C1	C1	C1	C1	C1	Cs	C1	C1		0.00000
28	C2	C2	C2	C_2	C2	-	C_2	C2	C_2		1.00000
29	C2	C2	C2	C2	C2	C2	C2v	C2	C2	!	1.00000
30	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
31	C1	C3	C1	C1	C1	_	C3	C1	C3	!M	0.99905
32	C1	C1		CI		CI	C1		CI		0.00000
34	C1	C1		Ci		C1	C1	C1	Ci		0.00000
35	D3	D3	D3	D3	D3	D3	-	D3	D3		1.00000
36	C1	C1	Ci	Ci	Ci	C1	C1	C1	Ci		0.00000
37	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
38	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	.	1.00000
39	D5 C-	D5 C-	C5 C-	C5	D5 C-	D5 C-	D5 C-	D5 C-	D5 C-	! !	1.00000
40	C1	C1	C1	C1	C1	C1	Cs	C1	C1	· ·	0.00000
42	C2	C_2	C2	C_2	C2	-	C_2	C_2	C_2		1.00000
43	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
44	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
45	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
46	C1 C	C1		C1		C1	C1	C1 C	C1 C		0.00000
47	C3	C3	C3	C3	C3	C3	Cav	C3	C3		1.00000
48	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
50	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
51	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
52	C2v	C2v	C2v	C2v	C2v	C_{2v}	C2v	C2v	C_{2v}		1.00000
53	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
55 55	D5	D5	D5	D5	D5	D5	_	D5	D5		1.00000
56	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
57	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
58	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
59	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		0.99639
60	C4v	C4v	C4v	C4v	C4v	C4v	-	C4v	C4v		1.00000
61	D4h C2u	D4h C2w	D4h C2u	D4h C2v	D4h C2v	D4h C2v	D4h	D4h C2w	D4h C2v		1.00000
63	D4h	D4h	C4h	C4h	D4h	D4h	D4h	D4h	D4h	· ·	1.00000
64	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v		1.00000
65	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
66	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
67	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	_	C_{2v}	C_{2v}		1.00000
60 60	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
70	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v C2v	C2v	C_{2v}	C_{2v}		1.00000
71	\mathbf{Cs}	\mathbf{Cs}	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}		1.00000
72	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
73	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
74	C1	C1		C1		C1	C1		C1		0.00000
76	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1,00000
77	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
78	D3d	D3d	D3d	D3d	D3d	D3	-	D3d	D3d	!	1.00000
79	\mathbf{Cs}	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	-	\mathbf{Cs}	\mathbf{Cs}	\mathbf{Cs}		1.00000
80	C2h	C2h	C2h	C2h	C2h	C1	~	C2h	C2h	!	1.00000
81	Car	Car	Car	C1 C2F		C1	C1	C1 C21	C1 C2F	,	0.00000
04 83	Cs ∪2n	Cs ∪2n	C_{s}^{2n}	Cs Cs	Cs Cs	_	Cs	Cs Cs	Cs Cs	[`]	1.00000
84	C1	C1	C1	Č1	C1	C1	Č1	C1	C1		0.00000
85	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
86	C2	C2	C2	C_2	C2	C_2	C2	C_2	C_2		1.00000
87	C1	C1	C1	C1	C1	C1	C1	C1	C1	.	0.00000
88	D4h C4w	D4h C4v	D4h C4v	C4h C4w	D4h C4v	D4h C4v	_	D4h C4w	D4h C4w	'	1.00000
90 99	C2	C_{4v}	C2	C2	C2	C ₄ v C ₂		C2	C2		1.00000
91	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	-	C2v	C_{2v}		1.00000
92	\mathbf{Cs}	\mathbf{Cs}	Cs	Cs	Cs	\mathbf{Cs}	-	Cs	\mathbf{Cs}		1.00000
93	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
94	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
95	C2v	C_{2v}	C2v	C2v		C2v	_	C2v	C2v		1.00000
97	C1	C1	C1	C1		C1	C1	C1	C1		0,00000
98	Cs	Cs	Cs	Cs	Cs	Cs	Čs	Cs	Cs		1.00000
99	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
100	D2d	D2d	D2d	D2d	D2d	C_2	D2	D2d	D2d	!	1.00000

Table S22: Dataset: finnis-sinclair/Mo, part 1.

name	SY	VA 0.05	Sym	Mol 0.05	, default,	libmsym 'medium'	'loose'	SC	FI 0.05	diff	dot product
3	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	um	1.00000
4	Td D2b	Td Dab	Td D2b	Td D2b	Td D2h	Td D2b	Td D2b	Td D2b	Td D2b		0.92867
6	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		0.99980
7	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
8	C2v C2v	C2v C2v	C2v C2v	C_{2v} C_{2v}	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C_{2v} C_{2v}		1.00000
10	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
11	C2v C5v	C2v C5v	C2v C5v	C2v C5v	C2v C5v	C2v C5v	C2v C5v	C2v C5v	C2v C5v		1.00000
13	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih		0.99686
14	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
15 16	C2v Ce	C2v Ce	C2v Ce	C2v	C2v	C2v	C2v Ce	C_{2v}	C2v Ce		1.00000
17	C2	C_2	C2	C_2	C2	\tilde{C}^{2}	C2	C_2	C_2		1.00000
18	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Ι.	1.00000
20	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C_{2v}	C2v		1.00000
21	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
22 23	Cs D3h	Cs D3h	Cs D3h	Cs D3h	Cs D3h	Cs D3h	Cs D3h	Cs D3h	Cs D3h		1.00000
24	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C_{2v}	C_{2v}		1.00000
25	Cs	Cs	C1	Cs	Cs	Cs	Cs	Cs	Cs	!	1.00000
20	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
28	\mathbf{Cs}	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	\mathbf{Cs}		1.00000
29 30	D3h C2y	D3h C2y	D3h C2y	D3h C2v	D3h C2v	D3h C2v		D3h C2v	D3h C2v		1.00000
31	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
32	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C_{2v}	C_{2v}		1.00000
33 34	D5h	D5h	C5 C5	C5	D5h	D5h	D5h	D5h	D5h		1.00000
35	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
36 37	Cs	Cs	Cs	Cs Cs	Cs	Cs	Cs	Cs Cs	Cs Ce		1.00000
38	D6h	D6h	D6h	D6h	D6h	D6h	-	D6h	D6h		1.00000
39	C6v	C6v	C6	C6	C6v	C6v	C6v	C6v	C6v	!	1.00000
40 41	D6h C2v	D6h C2v	C6h C2v	C6h C2v	C2v	D6h C2y	D6h C2v	D6h C2v	C2v	!	1.00000
42	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
43	Cs	Cs	Cs	Cs	Cs	Cs	Cs C2v	Cs	Cs		1.00000
44	C1	C1	C2V C1	C1	C1	C1	C2V C1	C1	C1		0.00000
46	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
47	Cs C3v	Cs C3v	Cs C3v	Cs C3v	Cs C3v	Cs C3v	 C3v	Cs C3v	Cs C3v		1.00000
49	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
50	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
51 52	C1	C1	C1	C1		C1	C1	C1	C1		0.00000
53	\mathbf{Cs}	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	\mathbf{Cs}		1.00000
54 55	C5v Ib	C5v Ib	C5 Ib	C5 Ib	C5v Ih	C5v Ih	– Ih	C5v Ib	C5v Ib	!	1.00000
56	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
57	D2d	D2d	D2d	D2d	D2d	D2d	D2	D2d	D2d	!	1.00000
58 59	C2v	C_{2v}	C2v	C2v	Cs C2v	C2v	Cs	C2v	C2v	!	1.00000
60	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
61 62	Td Cs	Td Cs	Td Cs	Td Cs	Td Cs	Td _	Td Cs	Td Cs	Td Cs		0.96580
63	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
64	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C_{2v}	C_{2v}		1.00000
66	C1	C1	-	C1	C1	C1	C1	C1	C1		0.00000
67	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
68 69	C3	C3	C3	C3		C1	C1	C3	C3		1.00000
70	C2	C2v	C_2	C2	C2	C2v	C2v	C2	C2v	!M	1.00000
71 72	Cs	Cs	Cs	Cs Cs	Cs	Cs	Cs	Cs Cs	Cs Ce		1.00000
73	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
74	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
75 76	D3h	D3h	C3h	C3h	D3h	D3h		D3h	D3h		1.00000
77	C3v	C3v	-	-	C3v	C3v	C6v	C3v	C3v	!	1.00000
78 79	D3h Cs	D3h Cs	D3h Cs	D3h Cs	D3h Cs	D3h C2y	_	D3h Cs	D3h Cs	,	1.00000
80	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
81	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
82 83	C1	C1	C1	C2 C1	C1	C1	C1	C2 C1	C2 C1		0.00000
84	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
85 86	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v	C2v Cs	C2v Cs		1.00000
87	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
88	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
90	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
91	D3	D3	D3	D3	D3	C1	-	D3	D3	!	1.00000
92 93	C2 C1	C2 C1	C2 C1	C2 C1	C2 C1	 C1	C2 C1	C2 C1	C2 C1		1.00000
94	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C_{2v}	C_{2v}		1.00000
95 06	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	114	1.00000
90 97	C1	C1	C1	C1	C1	C1	C1	C1	C1	1111	0.00000
98	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
99 100	C1 C1	C1 C1	C1 C1	C1 C1		C1 C1	C1 C1	C1 C1	C1 C1		0.00000
101	C1	C1	C1	Č1	C1	Č1	Č1	C1	C1		0.00000
102	C1	C1	C1 C1	C1	C1 C1	C1 C1	C1	C1	C1		0.00000
104	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
105	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
$106 \\ 107$	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs		1.00000
108	Ċs	Ċs	Cs	Ċs	Cs	Čs	Ċs	Cs	Ċs		1.00000
109	C1	C1	C1	C1	C1	C1 C1	C1	C1	C1		0.00000
111	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000

Table S23: Dataset: glue_Al, part 1.

	SY	VA	Sym	Mol		libmsym		SC	FI		
112	0.001 C1	0.05 C1	0.001 C1	0.05 C1	C1	C1	C1	0.001 C1	0.05 C1	diff	dot product 0.00000
113	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
114	C1	C1	C1 C1	C1	C1	C1	C1	C1 C1	C1		0.00000
116	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	\mathbf{Cs}		1.00000
117 118	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1		0.00000
119	Č1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
120	C2 C1	C2	C2 C1	C2	C2 C1		C2	C2 C1	C2		1.00000
121 122	C1 C2	C1 C2	C1 C2	C2	C1 C2	-	C2	C1 C2	C2		1.00000
123	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
124 125	C1	C1		C1		C1 C1	C1		C1		0.00000
126	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
127 128	C1 C1	C1 C1		C1 C1		C1 C1	C1 C1		C1 C1		0.00000
129	C3	C3	C3	C3	-	-	C3	C3	C3		1.00000
130 131	C1 C1	C1 C1	C1 C1	C1 C1		C1 C1	C1 C1		C1 C1		0.00000
132	C2	C_2	C2	C_2	C2	C2	C1	C2	C_2	!	1.00000
133	Cs C2	Cs C2v	Cs C2	Cs C2v	Cs C2	Cs C2v	Cs	Cs C2	Cs C2	,	1.00000
135	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
136	Cs C=	Cs C-	Cs	Cs C-	Cs C-	Cs	Cs C-	Cs	Cs C-		1.00000
137	C2v	C_{2v}	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
139	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
140 141	Cs	Cs Cs	Cs Cs	Cs	Cs Cs	Cs	_	Cs Cs	Cs		1.00000
142	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v	C2v		1.00000
143 144	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs	Cs C2v	Cs C2v		1.00000
145	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
146 147	C1 Ib	C1 Ih	C1 Ih	C1 Ih	C1 Ib	C1 Ib	C1 Ib	C1 Ih	C1 Ih		0.00000
148	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
149 150	C1 Ce	C1 Ce	C1 Ce	C1 Ce	C1 Ce	C1 Ce	C1 Ce	C1 Ce	C1 Ce		0.00000
151	C2v	C_{2v}	C2v	C_{2v}	C2v	-	-	C2v	C_{2v}		1.00000
152	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
154	Cs	Cs	Cs	Cs	Cs	-	-	Cs	Cs		1.00000
155	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	-	Cs	Cs		1.00000
157	C3V C1	C3V C1	 C1	 C1	C3V C1	C1	C1	C3V C1	C1		0.00000
158	C2	C_2	C2	C_2	C2	-	-	C2	C_2		1.00000
159 160	Cs D3h	Cs D3h	Cs D3h	Cs D3h	Cs D3h	D3h	Cs	Cs D3h	Cs D3h		1.00000
161	C1	C1	C1	C1	C1	C1	-	C1	C1		0.00000
162 163	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	_	Cs Cs	Cs Cs		1.00000
164	C2	C_2	C2	C_2	C2	C_2	-	C2	C_2		1.00000
165 166	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs	_	_	Cs Cs	Cs Cs		1.00000
167	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
168	C2 C1	C2	C2 C1	C2	C2 C1	C2	-	C2 C1	C2		1.00000
170	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
171	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs	Ι.	1.00000
172	C2	C2	C2	C2	C2	C2	C_2	C2	C2	·	1.00000
174	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
175 176	C1 C1	C1 C1		C1 C1		C1 C1	C1 C1		C1 C1		0.00000
177	C2	C2	C_2	C2	C_2	C_2	_	C_2	C2		1.00000
178 179	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1		0.00000
180	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
181 182	Cs C1	C_{2v}	Cs C1	Cs C1	Cs C1	Cs C1		Cs C1	Cs C1	!	1.00000
183	C1	Cs	C1	C1	C1	Cs	-	C1	C1	!	0.00000
184 185	C2 C1	C2 C1	C2 C1	C2 C1	C2 C1	C2 C1	C2	C2 C1	C2 C1		1.00000
186	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
187	C1	C1	C1	C1	C1	C1	-	C1	C1		0.00000
188	C1	C1	C1	C1	C1	C1	C1		C1		0.00000
190	C2	C2	C2	C2	C2	C2	-	C2	C2		1.00000

Table S24: Dataset: glue_Al, part 2.

	SY	VA	Sym	Mol		libmsym	., ,	SO	FI		
3	D3h	D3h	D3h	0.05 D3h	D3h	D3h	D3h	D3h	0.05 D3h	аіп	1.00000
4	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.93647
5	D3h Oh	D3h Ob	D3h Oh	D3h Ob	D3h Oh	D3h Ob	D3h Ob	D3h Ob	D3h Oh		1.00000
7	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
8	C2v	D2d	C2v	D2d	C2v	C2v	D2d	C2v	D2d	!M	1.00000
9	D3h C2v	D3h C2v	D3h C2u	D3h C2v	D3h C2v	D3h C2v	D3h C2v	D3h C2w	D3h C2u		1.00000
11	C3v	C3v			C3v	C3v	C3v	C3v	C3v		1.00000
12	D3h	D3h	D3h	D3h	D3h	D3h	-	D3h	D3h		1.00000
13	D5h C2v	D5h C2v	C5 C2w	C5 C2rr	D5h C2v	D5h C2v		D5h C2v	D5h C2u	!	1.00000
15	C_{2v}	C_{2v}	C2v C2v	C_{2v}	C2v C2v	C2v C2v	C2v C2v	C_{2v}	C_{2v}		1.00000
16	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
17	C3v C1	C3v C1	C3v C1	C3v C1	C3v C1	C3v C1	C3v C1	C3v C1	C3v C1		1.00000
19	C_{2v}	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}		1.00000
20	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C_{2v}	C_{2v}		1.00000
21 22	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1	C_{2v}	C2v C1		0.00000
23	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}		1.00000
24	D2h	D2h	D2h	D2h	D2h	_	D2h	D2h	D2h		1.00000
25 26	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v C2v	C2v Cs	C2v Cs		1.00000
27	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C_{2v}	C_{2v}	· ·	1.00000
28	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
29 30	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
31	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
32	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C_{2v}	C_{2v}		1.00000
33 34	C1	C1		C1		C1	C1	C1	C1		0.00000
35	\mathbf{Cs}	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	\mathbf{Cs}	\mathbf{Cs}	\mathbf{Cs}		1.00000
36 37	D3d C3v	D3d C3v	_	_	D3d C3v	D3d C3r	D3d C3r	D3d C3v	D3d C3v		1.00000
38	D3d	D3d	D3d	D3d	D3d	D3d	D3d	D3d	D3d		1.00000
39	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
40 41	C2 Ce	C2 Ce	C2 Ce	C2	C2 C2	C2 Cs	- Cs	C2	C2		1.00000
42	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
43	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
44 45	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs	Cs	Cs Cs	Cs Cs	Cs Cs		1.00000
46	C1	C1	-	C1	C1	C1	C1	C1	C1		0.00000
47	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
48 49	C1 C2	C1 C2	C1 C2	C1 C2		C1 C2	-	C1 C2	C1 C2		1.00000
50	C1	C1	C1	C1	C1	Č1	C1	C1	C1		0.00000
51	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
52 53	C1	C1		C1		C1	C1	C1	C1		0.00000
54	_	_	S10	S10	S10	S10	_	S10	S10		1.00000
55 56	C1	C1	C1 C1	C1	C1 C1	C1 C1	C1	C1	C1		0.00000
57	C1	C1	C1	C1		C1	C1	C1	C1		0.00000
58	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
59 60	C1	C1	C1 C1	C1	C1 C1	C1 C1	C1	C1	C1		0.00000
61	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
62	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
63 64	C1 C2	C1 C2	C1 C2	C1 C2		C1 C2	C1 C2	C1 C2	C1 C2		0.00000
65	C2	C2	C2	C2	C2	-	C2	C2	C2		1.00000
66	S4	S4	S4	S4	S4	S4	C2	S4	S4	!	1.00000
67 68	C1 C1	C1 C1		C1 C1		C1 C1	C1 C1	C1 C1	C1 C1		0.00000
69	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
70	C1 C2	C1 C2	C1	C1 C2	C1 C2	C1 C2	C1	C1 C2	C1 C2		0.00000
71 72	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
73	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
74 75	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1		0.00000
76	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
77	C1	C1	C1	C1	C1	C1	C1	C1	C1	l .	0.00000
78 79	C2 C2	C2 C2	C2 C2	C2 C2	C2 C2	C1 C2	C2 C2	C2 C2	C2 C2	!	1.00000
80	C1	Č1	C1	C1	C1	Č1	Č1	C1	C1		0.00000
81	C1 D2	C1 D2	C1 D2	C1 D2	C1 D2	C1	C1	C1 D2	C1		0.00000
82	D3 C1	D3 C1	C1	D3 C1	C1	 C1		D3 C1	D3 C1		0.00000
84	D2	D2	D2	D_2	D2	D2	D2	D2	D_2		1.00000
85 86	C1 C2	C1	C1	C1	C1 C2	C1 C2	C1	C1	C1		0.00000
87	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
88	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
89 90	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}	C2v		1.00000
91	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	-	C2v	C_{2v}		1.00000
92	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
93 94	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1	C1 C2v	C1 C2v		0.00000
95	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C_{2v}	C_{2v}		1.00000
96	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
97 98	C1	C1		C1 C1		C1	Cs	C1	C1 C1	1	0.00000
99	Č1	Č1	Č1	Č1	C1	Č1	Č1	Č1	Č1	·	0.00000
100	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
101	C1	C1		C1	C1	C1	C1	C1	C1		0.00000
103	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
104 105	C1 C1	C1 C1	C1 C1	C1	C1 C1	C1	C1 C1	C1 C1	C1		0.00000
106	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
107	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	-	Cs	Cs		1.00000
108	C_{2v}	C_{2v}	C2v C2v	C_{2v}	C2v C2v	 Cs		C_{2v}	C_{2v}	, I	1.00000
110	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	[']	1.00000
111	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000

Table S25: Dataset: glue_Pb, part 1.

	SY	VA	Sym	Mol		libmsym		SO SO	FI		
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
112	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
113	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
114	C2	C2	C2	C2	C2	C2	C1	C2	C2	!	1.00000
115	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
116	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
117	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
118	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
119	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
120	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
121	C2	C_2	C2	C_2	C2	C2	C2	C2	C2		1.00000
122	Č1	Č1	Č1	C1	Č1	Č1	Č1	Č1	Č1		0.00000
123	C2	\tilde{C}^2	C2	$\tilde{C2}$	C2	_	C2	C2	\tilde{C}^2		1.00000
124	C2	C2	Č2	C2	C2	C2	_	C2	C2		1 00000
125	C1	CI	CI	CI	C1	C1	C1	CI	CI		0.00000
126	C1	C1		C1	C1	C1	C1		C1		0.00000
127	C1	C1		C1	C1	C1	C1		C1		0.00000
127	C1	C1	C1	C1	C1	C1	C1		C1		0.00000
120	C1	C1		C1	C1	C1	C1		C1		0.00000
129	CI	CI		CI	CI	CI	C1		CI		0.00000
121		CI		CI		CI	C1		CI		0.00000
122	C1	C1		C1	C1	C1	C1		C1		0.00000
132	CI	CI		CI	CI	CI	C1		CI		0.00000
133	CI	CI		CI		CI	CI		CI		0.00000
134	CI	CI		CI		CI	CI		CI		0.00000
135		C1		CI		CI	CI		CI		0.00000
136		C1		CI		CI	CI		CI		0.00000
137	CI	CI		CI		CI	CI		CI		0.00000
138	C2	C2		C2	C2 C1	02	CI		CZ	!	1.00000
139		C1 G1		CI		CI	CI		CI		0.00000
140	CI	CI		CI	CI	CI	CI		CI		0.00000
141	CI	CI		CI	CI	CI	CI		CI		0.00000
142	CI	CI	CI	CI	CI	CI	CI	CI	CI		0.00000
143	CI	CI	CI	CI	CI	CI	CI	CI	CI		0.00000
144	C2	C_2	C2	C2	C2	C2	-	C2	C2		1.00000
145	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
146	C2	C2	C2	C2	C2	C2	_	C2	C2		1.00000
147	Cs	Cs	Cs	Cs	Cs	Cs	CI	Cs	Cs	!	1.00000
148	D3d	D3d	S6	S6	D3d	D3d	_	D3d	D3d	!	1.00000
149	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
150	Cs	-	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
151	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
152	C2	-	C2	C_2	C2	C2	_	C2	C2		1.00000
153	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
154	C2	-	C2	C_2	C2	C2	-	C2	C2		1.00000
155	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
156	C2	-	C2	C2	C2	C2	C2	C2	C2		1.00000
157	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
158	C2	-	C2	C2	C2	C2	C2	C2	C2		1.00000
159	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
160	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000

Table S26: Dataset: glue_Pb, part 2.

	SY	VA	Syn	Mol		libmsym		sc	FI		
3	0.001 D3h	0.05 D3h	0.001 D3h	0.05 D3h	'default' D3h	'medium' D3h	'loose' D3h	0.001 D3h	0.05 D3h	diff	dot product 1.00000
4	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.62381
5	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
7	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
8	D2d	D2d	D2d	D2d	D2d	D2d	D2d	D2d	D2d		1.00000
9	C2v D4d	C2v D4d	C2v D4d	C2v D4d	C2v D4d	C2v D4d	C2v D4d	C2v D4d	C2v D4d		1.00000
11	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
12	C2	C2	C2	C2	C2	C_2	C2	C2	C2		1.00000
13	Cs D6d	Cs	Cs D6d	Cs D6d	Cs D6d	Cs D6d	Cs D6d	Cs D6d	Cs D6d		1.00000
15	D3	D3	D3	D3	D3	D3	-	D3	D3		1.00000
16	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
18	C_{2v}	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v		1.00000
19	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
20	C_{2v}	C_{2v}	C2v C1	C_{2v}	C2v C1	C2v C1		C2v C1	C_{2v}		1.00000
22	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
23	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
24 25	C1 C2	C1 C2	C1 C2	C2	C1 C2	C1 C2	C1 C2	C2	C2		1.00000
26	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
27 28	C1 C2	C1 C2	C1 C2	C1 C2		C1 C2	C1 C2	C1 C2	C1 C2		0.00000
29	C1	C1	C1	C1	C1	Č1	C1	C1	C1		0.00000
30	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
32	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
33	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
34 35	C1 C1	C1 C1	C1 C1	C1 C1		C1 C1	C1 C1	C1 C1	C1 C1		0.00000
36	D2h	D2h	D2h	D2h	D2h	_	D2h	D2h	D2h		1.00000
37	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
38 39	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	D2d C2v	C2v	C2v	C_{2v}		1.00000
40	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
41 42	C2v	C_{2v}	C2v	C_{2v}	C2v	C_{2v}	C_{2v}	C2v	C_{2v}		1.00000
42	C4	C4	C4	C4	C4	-	-	C4	C4		1.00000
44	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
45 46	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs		1.00000
47	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
48	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
49 50	Cs	Cs Cs	C2v Cs	C2v Cs	C2V Cs	C2V Cs	C2v Cs	C2V Cs	C2V Cs		1.00000
51	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
52 52	C1	C1	C1 C1	C1	C1 C1	C1 C1	C1	C1	C1		0.00000
55 54	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
55	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
56 57	C2 C1	C2 C1	C2 C1	C2 C1	C2 C1	C2 C1	C2 C1	C2 C1	C2 C1		1.00000
58	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
59	C1	C1	C1	C1	C1 C1	C1	C1	C1	C1		0.00000
61	C2	C_2	C2	C_2	C2	C2	C2	C2	C_2		1.00000
62	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
63 64	C1 C2	C1 C2	C1 C2	C1 C2		C1 C2	C1 C2	C1 C2	C1 C2		0.00000
65	C1	C1	C1	C1	C1	Č1	C1	C1	C1		0.00000
66	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
68	C1	C1	C1	C1		C1	C1		C1		0.00000
69	Č1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
70 71	C1	C1	C1 C1	C1	C1 C1	C1 C1	C1	C1	C1		0.00000
71 72	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
73	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}		1.00000
74 75	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		1.00000
76	C1	C1	C1	C1	Ci	Č1	C1	C1	C1		0.00000
77	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	C1 C1	Cs C1	Cs C1	!	1.00000
79	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
80	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
81 82	Cs C1	Cs C1	Cs C1	Cs C1	C1 Cs	Cs C1	Cs C1	Cs C1	Cs C1		0,00000
83	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
84 8F	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
80 86	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
87	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}		1.00000
88 89	C2v Ce	C2v	C2v Ce	C2v	C2v C°	C2v Cs	C2v Cs	C2v	C2v Ce		1.00000
90	C1	C1	C1	C1	C1	Č1	C1	C1	C1		0.00000
91	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	C_{2v}	C2v	C_{2v}		1.00000
92 93	Cs Cs	C_{2v}	C2v Cs	C2v Cs	Cs Cs	C2v Cs	Cs Cs	Cs	C2v Cs		1.00000
94	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}		1.00000
95 96	Cs Ce	Cs C	Cs C ²	Cs C	Cs C ²	Cs C=	Cs Ce	Cs C	Cs Ce		1.00000
97	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
98	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	.	1.00000
99 100	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	-	Cs Cs	Cs Cs	'	1.00000
101	Cs	Čs	Cs	Čs	Cs	Cs	C1	Cs	Čs	!	1.00000
102	C1	C1	C1 C1	C1	C1 C1	C1	C1	C1	C1		0.00000
103	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
105	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
106 107	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1		0.00000
108	C1	C1	C1	C1	C1	Č1	Č1	C1	C1		0.00000
109	C1	C1	C1 C1	C1	C1 C1	C1	C1	C1 C1	C1		0.00000
111	C2	C2	C2	C_2	C2	C2	C2	C2	C_2		1.00000
										1	

Table S27: Dataset: gupta/Cd, part 1.

	SY	VA	Sym	Mol		libmsym		SO	FI		
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
112	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
113	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
114	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
115	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
116	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
117	C1	C1	C1	C1	C1	C1	-	C1	C1		0.00000
118	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
119	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
120	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
121	C2	C2	C2	C2	C2	C2	-	C2	C2		1.00000
122	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
123	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
124	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
125	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000

Table S28:	Dataset:	gupta/Cd,	part	2.

	SY	VA	Syn	Mol		libmsym		SC	FI		
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
4	Td	Td	Td	Td	Td D3h	Td	Td	Td D3n	Td		0.99763
5	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
6	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		0.96601
7	D5h D2d	D5h D2d	D5h D2d	D5h D2d	D5h D2d	D5h D2d	D5h D2d	D5h D2d	D5h D2d		1.00000
9	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
10	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
11	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
13	Th	C3V	Ci	Ci	Th	Th	Th	Th	Th		0.97125
14	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
15	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
16	Cs C2	Cs C2	Cs C2	Cs C2	Cs C2	Cs C2	Cs C2	Cs C2	Cs C2		1.00000
18	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
19	D5h	D5h	C5	C5	D5h	D5h	D5h	D5h	D5h	!	1.00000
20	C2v C1	C_{2v}	C2v C1	C_{2v}	C2v C1	C_{2v}	C_{2v}	C2v C1	C_{2v}		1.00000
21	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
23	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
24	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C_{2v}	C2v	C_{2v}		1.00000
25 26	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.91836
27	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
28	T	T	T	Т	T	Т	Т	T	Т		0.97817
29 30	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
31	C3	C3	C3	C3	C3	C3	C3	C3	C3		1.00000
32	D3	D3	D3	D3	D3	D3	_	D3	D3		1.00000
33	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
35	C2v	C_{2v}	C2	C_{2v}	C2v	C_{2v}	C2v	C2v	C_{2v}	!	1.00000
36	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	.	1.00000
37 38	Ob Ob	C2 Ob	C1 Ob	C1 Ob	C1 Ob	C1 Ob	C1 Ob	C1 Ob	C1 Ob	'	0.00000
39	C5v	C5v	C5	C5	C5v	C5v	_	C5v	C5v	!	1.00000
40	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}		1.00000
41	Cs	Cs	C1 C2	Cs	Cs	Cs	Cs	Cs	Cs	!	1.00000
42	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
44	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
45	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
46 47	C2V C1	C1	C2v C1	C2V C1		C2V	C2v	C2V C1	C2V C1		0.00000
48	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
49	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	Ι.	1.00000
50 51	C2v	C2v		C2v	C2v	C2v	Cs _	C2v	C2v		1.00000
52	C3v	C3v	-	_	C3v	C3v	-	C3v	C3v		1.00000
53	C2v	C2v	Cs	C2v	C2v	C2v	Cs	C2v	C2v	!	1.00000
54 55	C5v Th	C5v Ib	C5 1b	C5 Th	C5v Th	C5v Ib	C5v Ib	C5v Th	C5v Ib	1 '	0.95414
56	C3v	C3v	-	-	C3v	-	_	C3v	C3v		1.00000
57	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
58 59	C3v C1	C3v C1	C3v C1	C3v C1	C3v C1	C3v C1	C3v C1	C3v C1	C3v C1		1.00000
60	Cs	Cs	C1	Cs	Cs	Cs	Cs	Cs	Cs	!	1.00000
61	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}	C2v	C2v		1.00000
62 63	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		1.00000
64	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
65	C2	C2	C2	C2	C2	C_2	C_2	C2	C2		1.00000
66 67	C1 C2	C1 C2	C1 C2	C1 C2	C1 C2	C1 C2	C1 C2	C1 C2	C1 C2		0.00000
68	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
69	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
70	C5v	C5v	C5v	C5v	C5v	C5v	-	C5v	C5v		1.00000
71	Cs	Cs	C1	Cs	Cs	Cs	_	Cs	Cs		1.00000
73	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	Cs		1.00000
74	C5v	C5v	C5	C5	C5v	-	-	C5v	C5v	!	1.00000
75 76	Cs	Cs	C1	Cs	C1	Cs	_	Cs Don	Cs		1.00000
77	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
78 70	C1	C1	C1 C2	C1	C1 C2	C1 C2:	C1 C2::	C1 C2	C1		0.00000
80	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
81	C2	C_2	C2	C_2	C2	C_2	-	C2	C_2		1.00000
82	C1	C1	C1	C1	C1	C1	C1	C1	C1	Ι.	0.00000
83 84	C1	C1	C1	C1	C1	C2v C1	C1	C1	C1	'	0.00000
85	C1	C1	C1	C1	C1	Č1	C1	C1	C1		0.00000
86	C3	C3	C3	C3	C3	_	C3	C3	C3		1.00000
87 88	Cs	Cs Cs	Cs C1	Cs Cs	Cs Cs	Cs	Us Cs	Cs Cs	Cs Cs	1	1.00000
89	C3v	C3v	-	-	C3v	C3v	C1	C3v	C3v	i	1.00000
90	Cs	Cs	C1	Cs	Cs	Cs	Cs	Cs	Cs	!	1.00000
91	Cs C2v	Car	C1	Cs	Cs C2v	Cs	Cs	Cs C2v	Cs C2v	! !	1.00000
93	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
94	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
95 96	C1 C1	C1	C1 C1	C1		C1	C1		C1		0.00000
97	C2v	C_{2v}	C2v	C2v	C2v	C2v	Cs	C2v	C_{2v}	!	1.00000
98	\mathbf{Cs}	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	\mathbf{Cs}	\mathbf{Cs}	\mathbf{Cs}		1.00000
99	C2v	C2v	C2v	C2v	C1 Cc	C2v		C2v	C2v	'	1.00000
101	C2v	C_{2v}	Cs	C2v	C2v	C2v	-	C2v	C_{2v}	!	1.00000
102	C2v	C2v	C2v	C2v	C2v		C2v	C2v	C2v		1.00000
103	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
104	C2v	C_{2v}	C2v C1	C2v	C2V C2	C2v C2	C1	C2	C_{2v}	!	1.00000
106	C1	Č1	C1	C1	C1	Č1	Č1	C1	Č1	. 	0.00000
107	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
108	Cs C1	Cs C1	Cs C1	Cs C1	C1 C1	Cs C1	Cs C1	C1 C1	Cs C1		0.00000
110	Cs	Ċs	Cs	Ċs	Cs	Čs	Cs	Cs	Ċs		1.00000
111	Cs	Cs	C1	Cs	Cs	\mathbf{Cs}	-	Cs	Cs	!	1.00000

Table S29: Dataset: gupta/Co, part 1.

	SY	VA	Sym	Mol		libmsym		SC	FI		
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
112	Ca	Ca	Ca	Cs	Cs	Cs	 	Ca	Ca		1.00000
113	Cs	Cs	C1	Cs	Cs	Cs	Cs	Cs	Cs	· ·	1.00000
115	C5v	C5v	C5v	C5v	C5v	_	-	C5v	C5v	· ·	1.00000
116	C5v	C5v	C5v	C5v	C5v	-	-	C5v	C5v		1.00000
117	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
118	Cs	Cs	C1	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	!	1.00000
119	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
120	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
121	C1 C1	C1 C1	C1 C1	C1	C1	C1 C1	C1	C1 C1	C1 C1		0.00000
122		Ca		C		C1	Ca				1.00000
123	Cs	Cs	C1	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
125	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	· ·	1.00000
126	Cs	Cs	C1	Cs	Cs	Cs	Cs	Cs	Cs	!	1.00000
127	C2v	C2v	C2	C2v	C2v	C2v	-	C2v	C2v	!	1.00000
128	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
129	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
130	Con	Can	Can	Con	Co	Ca	Cs	Can	Carr		1.00000
131	C1	C1	C1	C1	C1	C1	 C1	C1	C1		0.00000
133	Cs	Cs	C1	Cs	Cs	Cs	Cs	Cs	Cs	1	1.00000
134	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
135	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
136	Cs	Cs	C1	Cs	Cs	Cs	-	Cs	Cs	!	1.00000
137	C3v	C3v	C3v	C3v	C3v	C3v	-	C3v	C3v		1.00000
138	C3v	C3v			C3v	C3v	-	C3v	C3v	.	1.00000
139	C2v	C2v		C2v		C2v	-	C2v	C2v		1.00000
140	C5v	C5v		C_{5v}	C5v		_	C5v	C5v		0.99999
142	Cs	Cs	C1	C1	Cs	Cs	C1	Cs	Cs	i	0.99983
143	C2v	C2v	C2v	C2v	C2v	-	-	C2v	C2v	. 	1.00000
144	C3v	C3v	-	-	C3v	C3v	-	C3v	C3v		1.00000
145	C2v	C2v	C1	C2v	C2v	C2v	-	C2v	C2v	1	1.00000
146	C5v	C5v	C1	C_{5}	C5v	-	-	C5v	C5v	!	1.00000
147	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ι.	0.98344
148	Ca	Ca		Ca	Cs C1	 C	-	Ca	Ca		1.00000
149	C3v	C3v	_		C3v	C3v	_	C3v	C3v		1.00000
151	Cs	Cs	C1	Cs	Cs	_	Cs	Cs	Cs	!	0.99998
152	Cs	Cs	Cs	Cs	Cs	-	_	Cs	Cs		1.00000
153	C3v	C3v	-	-	C3v	-	C3v	C3v	C3v		1.00000
154	C2v	C2v	C2	C2v	C2v	C2v	-	C2v	C2v	!	1.00000
155	Cs	Cs	C1	Cs	Cs	Cs	_	Cs	Cs	!	1.00000
156	Cs	Cs	C1 C2	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
157	C2V Ce	C2V		C2V		C2V Ce	 C_	C2V	C2V Ce		1.00000
159	C2v	C_{2v}	C2v	C2v	C2v	C2v	-	C_{2v}	C_{2v}	· ·	1.00000
160	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
161	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
162	Cs	Cs	C1	Cs	Cs	C1	Cs	Cs	Cs	!	1.00000
163	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
164	C1	C1	C1 C1	C1		C1	C1	C1 C	C1	Ι.	0.00000
165	Ca	Ca		Cs	Cs	Cs	Cs	Ca	Ca		1.00000
167	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
168	C3v	C3v	C3v	C3v	C3v	C3v	_	C3v	C3v		1.00000
169	C2	C2	C1	C2	C2	C2	-	C2	C2	!	1.00000
170	C2v	C2v	C2v	C2v	C2	C2v	C2v	C2v	C2v	!	1.00000
171	Cs	Cs	C1	Cs	Cs	Cs	-	Cs	Cs	!	1.00000
172	C5v	C5v	C5	C5	C5v	C5v	-	C5v	C5v	!	1.00000
173	Cov	Cav	C5V C1	Cav	Cov	Cov	-	C5V C1	Cav	114	1.00000
175	C1	Cs	C1	Cs	Čs	Cs	_	C1	Cs	!M	1.00000
176	Cs	Cs	C1	Cs	Cs	Cs	-	Cs	Cs	!	1.00000
177	C5v	C5v	C5v	C5v	C5v	-	-	C5v	C5v		1.00000
178	C5v	C5v	C5	C5	C5v	-	-	C5v	C5v	!	1.00000
179	C1	Cs	C1	Cs	Cs	Cs	Cs	C1	Cs	!M	1.00000
180	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
181		Ca		Ca		CI			Ca	,	1.00000
182	- 05	C_{2v}	C1	C_{2v}		C2v	_	C2	C_{2v}	IM	1.00000
184	C1	Cs	C1	Cs	Cs	Cs	Cs	C1	Cs	!M	1.00000
185	C1	Č1	C1	C1	C1	Č1	Č1	Č1	Č1		0.00000
186	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
187	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	Cs		1.00000
188	Cs	Cs	C1	Cs	C1	Cs	Cs	Cs	Cs	1	1.00000
189	C1	Cs	C1	Cs	C1	C1	Cs	C1	Cs	!M	1.00000
190	D5 C5v	D5h C5u	D5 C5v	C5	C5v	D5h	-	D5h C5u	D5h C5v		1.00000
191	D5h	D5h	D5h	C5	D5h	D5h	_	D5h	D5h		1.00000
193	C2v	C_{2v}	C2v	C_{2v}	C2v		-	C_{2v}	C_{2v}	· ·	1.00000
194	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	C1	C1	_	Cs	\mathbf{Cs}	!	1.00000
195	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
196	C2v	C2v	Cs	C_{2v}	C2v	C1	-	C2v	C2v	!	1.00000
197	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs	.	1.00000
198	C2 C1	C2		C2		C1	C1	C2 C1	C2	'	1.00000
200	C1	C1		C1		C1	C1	C1	C1		0.00000
200	U U 1	01	U U 1	01	1 01	01	01	01	01	I	1 0.00000

Table S30: Dataset: gupta/Co, part 2.

	SY	VA	Sym	Mol		libmsym		SC	FI	I	
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
3	D3h	D3h TJ	D3h TJ	D3h TJ	D3h TJ	D3h	D3h T-	D3h TJ	D3h		1.00000
4 5	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
6	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		0.99970
7	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
8	D2d D3h	D2d D3h	D2d D3h	D2d D3h	D2d D3h	D2d D3h	D2d D3h	D2d D3h	D2d D3h		1.00000
10	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
11	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
12	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	Ι.	1.00000
13	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1 00000
15	D6d	_	C6	C6	D6d	D6d	D6d	D6d	D6d	!	1.00000
16	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
17	Td C5v	Td C5v	Td C5	Td C5	Td C5v	Td C5v	Td C5v	Td C5v	Td C5w		0.98972
19	D5h	D5h	C5	C5	D5h	D5h	D5h	D5h	D5h		1.00000
20	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
21	C_{2v}	C_{2v}	C_{2v}	C_{2v}	C2v	C2v	C2v	C_{2v}	C_{2v}		1.00000
22	US D3h	Cs D3h	Cs D3h	Cs D3h	US D3h	Us D3h	Us D3h	Cs D3b	US D3h		1.00000
23	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
25	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
26 27	Td	Td	Td Ca	Td Ca	Td Ca	Td	Td	Td Ca	Td		0.89129
28	T	T	T	T	T	T	T	T	T		0.84607
29	D3h	D3h	D3h	D3h	D3h	D3h	-	D3h	D3h		1.00000
30	C2v	C2v	C_{2v}	C_{2v}	C2v	C2v	_	C_{2v}	C_{2v}		1.00000
31	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v		0.00000
33	D3	D3	D3	-	D3	C3	-	D3	D3	!	1.00000
34	т	т	т	т	т	т	т	т	т		0.81925
35	D3 C2	D3 C2	D3 C2	D3 C2	D3 C2	-		D3 C2	D3 C2		1.00000
30 37	C3	C2 C3	C2 C3	C2 C3	C2 C3	C3	C3	C2 C3	C3		1.00000
38	Th	Th	Th	Th	Th	Th	Oh	Th	Th	!	0.70421
39	C5	C5	C5	C5	C5	C5	C5	C5	C_{5}		1.00000
40	Cs	Cs	Cs	Cs	Cs	Cs		Cs C2	Cs		1.00000
41 42	D_2	D_2	D_2^2	D_2^{-2}	D2	D_2^{02}	-	D2	D_2^2		1.00000
43	C2	C2	C2	C2	C2	_	C2	C2	C2		1.00000
44	C2v	C2v	C_{2v}	C_{2v}	C2v	C2v	C2v	C_{2v}	C_{2v}		1.00000
45 46	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v		0.00000
40	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
48	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
49	C5v	C5v	C_{5}	C_{5}	C5v	C5v	_	C5v	C5v	!	1.00000
50 51	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v		1.00000
52	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
53	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
54	C5v	C5v	C5	C5	C5v	C5v	C5v	C5v	C5v	!	1.00000
56	C3v	C3v			C3v	-	C3	C3v	C3v	1	1.00000
57	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
58	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
59 60	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	- Cs	C2v Cs	C2v Cs		1.00000
61	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.86453
62	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
63	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
64 65	C1 C2	C1 C2	C1 C2	C1 C2		C1 C2	C1 C2	C1 C2	C1 C2		1.00000
66	C2v	C2v	C2v	C2v	C2v	C_{2v}	C2v	C2v	C2v		1.00000
67	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
68	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
70	C5	C5	C5	C5	C5		_	C5	C5		1.00000
71	C5	C5	C5	C5	C5	-	C1	C5	C5	!	1.00000
72	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
73	C2h	C2h	C2h	C2h	C2h	C2h	-	C2h	C2h		1.00000
75	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
76	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
77	Cs	Cs	Cs	Cs	Cs	CI	Cs	Cs	CI		1.00000
79	C2v	C2v	C2v	C_{2v}	C2v	C2v	Cs	C2v	C2v	!	1.00000
80	\mathbf{Cs}	\mathbf{Cs}	Cs	Cs	Cs	\mathbf{Cs}	C1	Cs	\mathbf{Cs}	!	1.00000
81	C_{2v}	C_{2v}	C_{2v}	C_{2v}	C2v	C2v	Cs	C_{2v}	C_{2v}	!	1.00000
82 83	D3	Cs D3	Cs D3	Cs D3	D3	Cs C3	Cs _	Cs D3	D3	, I	1.00000
84	C1	C1	C1	C1	C1	C1	C1	C1	C1	· ·	0.00000
85	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
86	C3	C3	C3	C3	C3	_	C3	C3	C3		1.00000
87 88	C3v	C3v	Cs _	Cs _	Cav	C3v	C3v	C3v	C3v		1.00000
89	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
90	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
91	C1 T	C1 T	C1 T	C1 T	C1 T	C1 T	C1 T	C1 T	C1 T		0.00000
92 93	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.84597
94	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
95	C3	C3	C3	C3	C3	C3	C3	C3	C3		1.00000
96 97	Corr.	Car	Car	Car	Cs	Cs	Cs	Car	Cs		1.00000
98	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
99	C2v	C2v	C2v	C2v	C2v	C2v	\mathbf{Cs}	C2v	C2v	1	1.00000
100	C1	C1	C1	C1	C1	C1	C1	C1	C1	.	0.00000
101	D3 Ce	D3 Cs	D3 C=	D3 C=			_	D3 C=	D3 Ce	'	1.00000
103	C2v	C2v	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
104	D5	D5	C5	C5	D5	C5	-	D5	D5	!	1.00000
105	C5	C5	C5	C5	C5		-	C5	C5	.	1.00000
105	C1	C1	C1	D5 C1	C1	C5 C1		C1	D5 C1	'	0,00000
108	Č1	Č1	C1	Č1	C1	Č1	Č1	C1	Č1		0.00000
109	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
110 111	C5 C5	C5 C5	C5 C5	C5 C5	C5 C5	C5 C5	_	C5 C5	C5 C5		1.00000
* * *	00	00	00	00		00		00	0	1	1.00000

Table S31: Dataset: gupta/Na, part 1.

	SY	VA	Sym	Mol		libmsym	., ,	sc	FI	1.0	
112	C1	C1	C1	C1	C1	C1	C1	C1	C1	am	0.00000
$113 \\ 114$	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1	C1 _	C1 Cs	C1 Cs		0.00000 1.00000
115	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ι.	0.90510
117	C2v	C_{2v}	C2v	C_{2v}	C2v	c_{2v}	_	C2v	C_{2v}	i i	1.00000
118 119	C3v C2	C3v C2		$\overline{C2}$	C3v C2		_	C3v C2	C3v C2		1.00000
120	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
121 122	C1	C1	C1	C1	C1	C1	C1	C1	C1	· ·	0.00000
123 124	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C1 Cs	C2v Cs	C2v Cs	!	1.00000
125	C2v	C_{2v}	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C_{2v}		1.00000
126	C1	C1	C1 C1	C1	C1 C1	C1	C1	C1	C1		0.00000
128 129	C3v Cs	C3v Cs	- Cs	Cs	C3v Cs	_ Cs	_	C3v Cs	C3v Cs		1.00000
130	C5v	C5v	C5v	C5v	C5v	C5v	-	C5v	C5v		1.00000
131	Cs	Cs	Cs	Cs	Cs			Cs	Cs		1.00000
133 134	Cs Cs	Cs Cs	Cs	Cs Cs	Cs	Cs Cs	_	Cs Cs	Cs Cs		1.00000
135	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih		0.99815
136	D5d	D5d	S10	S10	D5d	D5d	D5d	D5d	D5d	l i	1.00000
138 139	C3v C2v	C_{2v}	C2v	$\overline{C_{2v}}$	C3v C2v	_	_	C3v C2v	C3v C2v		1.00000
140	Cs	Cs	Cs	Cs	Cs	-	-	Cs	Cs		1.00000
$141 \\ 142$	C2 Cs	C2 Cs	C2 Cs	C2 Cs	C2 Cs	_	Cs	C2 Cs	C2 Cs		1.00000
143 144	C2v C3v	C2v C3v	C2v	C_{2v}	C2v C3v	C2v	C2v C3v	C2v C3v	C2v C3v		1.00000
145	D5d	D5d	S10	S10	D5d	D5d	D5d	D5d	D5d	!	1.00000
140	Ih	Ih	Ih	Ih	Ih	 Ih	Ih	Ih	Ih	i i	0.87989
148 149	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs _	_	_	Cs Cs	Cs Cs		1.00000
150	C3v	C3v	-	-	C3v	C3v	-	C3v	C3v		1.00000
$151 \\ 152$	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	C2v	_	Cs C2v	Cs C2v		1.00000
153 154	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	_	Cs C2v	Cs C2v		1.00000
155	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
156	Cs C2v	C_{2v}	Cs C2v	C_{2v}	Cs C2v	Cs C2v	Cs -	Cs C2v	C_{2v}		1.00000
158 159	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 _	C1 C1	C1 C1		0.00000
160	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
161 162	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs	Cs	Cs	Cs Cs	Cs		1.00000
163 164	Cs	Cs Cs	Cs	Cs Cs	Cs	Cs	Cs	Cs Cs	Cs		1.00000
165	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
$166 \\ 167$	C5v Cs	C5v Cs	C5v Cs	C5v Cs	C5v Cs	Cs	_	C5v Cs	C5v Cs		1.00000
168 169	Cs	Cs Cs	Cs	Cs Cs	Cs	Cs	_	Cs Cs	Cs		1.00000
170	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
171 172	C5v C5v	C5v C5v	C5v C5v	C5v C5v	C5v C5v	C5v C5v	_	C5v C5v	C5v C5v		1.00000
173	C5v C1	C5v	C5v C1	C5v	C5v C1	C5v C1		C5v C1	C5v		1.00000
175	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
176 177	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 _	C1 Cs	C1 Cs		1.00000
178	C1 C1	C1	C1 C1	C1	C1 C1	C1 C1	C1	C1	C1		0.00000
180	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
181 182	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v	C2v Cs	Cs	C2v Cs	C2v Cs		1.00000
183 184	C1 C1	C1	C1 C1	C1	C1 C1	C1 C1	C1	C1	C1		0.00000
185	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
186	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	_	C2v Cs	C2v Cs		1.00000
188 189	Cs Cs	Cs Cs	Cs	Cs Cs	Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs		1.00000
190	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
191 192	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	_	Cs C2v	Cs C2v		1.00000
193	Cs	Cs	Cs	Cs	Cs	Cs		Cs	Cs		1.00000
194	Cs Cs	Cs Cs	Cs	Cs Cs	Cs	Cs	Cs	Cs Cs	C2V Cs	i i	1.00000
196 197	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs		0.00000
198	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
199 200	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs		1.00000
201 202	C3v Cs	C3v Cs	– Cs	Cs	C3v Cs	C3v Cs	C1 Cs	C3v Cs	C3v Cs	!	1.00000
203	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
$204 \\ 205$	C1 Cs	C1 Cs	Ci	C1 Cs	Cs	Cs	Cs	CI	C1 Cs		1.00000
206 207	Cs C3v	Cs C3v	Cs _	\mathbf{Cs}	Cs C3v	Cs C3v	_	Cs C3v	Cs C3v		1.00000
208	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	-	Cs	Cs		1.00000
209 210	Cs C3v	Cs C3v	Cs -	Cs _	Cs C3v	Cs C3v	Cs _	Cs C3v	Cs C3v		1.00000 1.00000
211 212	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs		1.00000
213	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
214 215	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs		1.00000 1.00000
216	C2v	C_{2v}	C2v	C2v	C2v		C	C2v	C2v		1.00000
218	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
219 220	C1 C2	C1 C2	C1 C2	C1 C2	C1 C2	C1 C2	C1 C2	C1 C2	C1 C2		0.00000 1.00000
221	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000

Table S32: Dataset: gupta/Na, part 2.

	SY	VA	Syn	Mol		libmsym		sc	FI		
222	0.001 C1	0.05 C1	0.001 C1	0.05 C1	C1	C1	C1	0.001 C1	0.05 C1	diff	dot product 0.00000
223	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
$224 \\ 225$	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	_	C2v Cs	C2v Cs		1.00000
226	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
227 228	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs		0.00000
229	\mathbf{Cs}	\mathbf{Cs}	\mathbf{Cs}	\mathbf{Cs}	Cs	\mathbf{Cs}	\mathbf{Cs}	\mathbf{Cs}	\mathbf{Cs}		1.00000
230 231	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs		0.00000
232	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
233	C1 Ca	C1 Ca	C1 Ca	C1 Ca	C1 Ca	C1	C1 Ca	C1 Ca	C1 Ca		0.00000
234	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
236	C5v C5v	C5v C5v	C5v C5v	C5v C5v	C5v C5v	C5v C5v	-	C5v C5v	C5v C5v		1.00000
237	C1	C1	C1 C1	C1	C1 C1	C1	C1	C3V C1	C1		0.00000
239	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
240 241	C1 C5v	C1 C5v	C1 C5v	C5v	C1 C5v	C1 C5v	-	C1 C5v	C1 C5v		1.00000
242	C5v	C5v	C5v	C5v	C5v	-	-	C5v	C5v		1.00000
243 244	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs	_	Cs Cs	Cs Cs		1.00000
245	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
246 247	C5 C5	D5 C5	C5 C5	C5 C5		C1	C1 C1	C5 C5	C5 C5		1.00000
248	C_5	D5	C5	D5	-	C1	C1	C5	D_{5}	!M	1.00000
249 250	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		Cs C1	Cs C1		1.00000
251	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
252	-	-			C3v	C3v	-	C3v	C3v Ca		1.00000
253	_	_	C1 C1	C1	C1 C1	C1	C1	C1	C1		0.00000
255	-	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
$\frac{256}{257}$	_	_	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		0.00000
258	-	-	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
259 260	_	_	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		1.00000
261	-	-	C5v	C5v	C5v	-	-	C5v	C5v		1.00000
262 263	_	_	C5v Cs	C5v Cs	C5v Cs	_	_	C5v Cs	C5v Cs		1.00000
264	-	-	Cs	Cs	Cs	-	-	Cs	Cs		1.00000
265	-	-	Cs	Cs	Cs	Cs		Cs	Cs		1.00000
267	_	_	Ih	Ih	Ih	Ih	Ih	Ih	Ih		0.91407
268	-	-	C5v C2v	C5	-		-	C5v C2v	C5v C2w	!	1.00000
209 270	_	_	C2V Cs	C ₂ v Cs	Cs	Cs	_	Cs	C ₂ V Cs		1.00000
271	-	-	C2v	C_{2v}	C2v	C2v	-	C2v	C2v		1.00000
272 273	_	_	Cs C2	Cs C2	Cs C2	Cs C2	_	Cs C2	Cs C2		1.00000
274	-	-	C1	C1	C1	C1	_	C1	C1		0.00000
275 276	_	_	Cs –	Cs _	Cs C3v	Cav	Cs _	Cs C3v	Cs C3v		1.00000
277	-	-	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
278	_	_	Cs	Cs	Cs	Cs Cs	Cs	Cs	Cs		1.00000
280	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
281	-	-	C1 Ca	C1 Ca	C1 Ca	C1 Ca	C1	C1 Ca	C1 Ca		0.00000
283	_	_	C1 C1	C1	C1 C1	C1 C1	C1	C1	C1		0.00000
284	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
285 286	_	_	C2v	C_{2v}	C3v C2v	C2v	_	C3v C2v	C_{2v}		1.00000
287	-	-	C2v	C_{2v}	C2v	C2v	-	C2v	C_{2v}		1.00000
288 289	_	_	C1 C1	C1	C1 C1	Cs C1	C1	Cs C1	C1		0.00000
290	-	-	C1	C1	C1	C1	-	C1	C1		0.00000
291 292	_	_	Cs C5v	C_{5v}	Cs C5v	Cs _	_	C5v	C5v		1.00000
293	-	-	Cs	\mathbf{Cs}	Cs	Cs	-	Cs	Cs		1.00000
$\frac{294}{295}$	_	_	Cs Cs	Cs Cs	Cs –	Cs Cs	_	Cs Cs	Cs Cs		1.00000
296	-	-	Cs	Cs	Cs	Cs	-	Cs	\mathbf{Cs}		1.00000
297 298	_	_	Ci C5v	Ci C5	C5v	1h _	1h _	C5v	1h C5v		1.00000
299	-	-	S10	S10	D5d	D5d	D5d	D5d	D5d	!	1.00000
300 301	_	_	C2v	-C2v	C3v C2v	$\overline{C2v}$	- C3v	C3v C2v	C_{2v}		1.00000
302	-	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
303 304	_	_	C2 Cs	C2 Cs	C2 Cs	C2	C2 Cs	C2 Cs	C2 Cs		1.00000
305	-	-	C2v	C_{2v}	C2v	-	-	C2v	C_{2v}		1.00000
306 307	-	-			C3v C3v	-	C3v	C3v C2v	C3v		1.00000
307	_	_	C5v	C_{2v}	C5v	_	_	C5v	C_{2v} C5v	!	1.00000
309	-	-	Ih	Ih	Ih	Ih	Ih	Ih	Ih		1.00000
310 311	_	_	Cs C2v	Cs C2v	Cs C2v	C2v	Us —	C2v	C_{2v}		1.00000
312	-	-	Cs	Cs	Cs	Cs		Cs	Cs		1.00000
313 314	_	_	Cs Cs	Cs Cs	Cs	Cs Cs	Cs -	Cs	Cs Cs		1.00000
315	-	-	C2v	C2v	C2v	C2v	-	C2v	C_{2v}		1.00000
316 317	_	_	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		1.00000
318	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
319	-	-	C1 Ca	C1 Ca	C1 Ca	C1 C2	C1 Ca	C1 C2	C1 Ca		0.00000
321	_	_	C1	C1	C1	C1	C1	C1	C1		0.00000
322	-	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
323 324	_	_	C1	C1	C1	C1	C1	C1	C1		0.00000
325	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
326 327	_	_	Cs C1	Cs C1	Cs C1	Cs C1	_	Cs C1	Cs C1		1.00000
328	-	_	C5v	C5v	C5v	C5v	-	C5v	C5v		1.00000
329 330	_	_	Cs Ce	Cs Ce	Cs Ce	Cs Ce	_	Cs Ce	Cs Ce		1.00000
331	-	_	C1	C1	C1	Č1	C1	C1	Č1		0.00000

Table S33: Dataset: gupta/Na, part 3.

	SY	VA	Sym	Mol		libmsym		SO SO	FI		
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
332	-	-	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
333	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
334	-	-	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
335	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
336	-	_	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
337	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
338	_	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
339	_	_	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
340	_	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
341	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
342	_	_	C1	C1	C1	C1	C1	C1	C1		0.00000
343	_	_	C1	C1	C1	C1	C1	C1	C1		0.00000
344	_	_	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
345	_	_	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
346	_	_	C1	C1	C1	C1	C1	C1	C1		0.00000
347	_	_	Cs	Cs	Cs	_	_	Cs	Cs		1.00000
348	_	_	C5v	C5v	C5v	_	_	C5v	C5v		1.00000
349	_	_	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
350	_	_	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
351	_	_	Cs	Cs	Cs	_	_	Cs	Cs		1.00000
352	_	_	C1	C1	Č1	C1	_	Č1	C1		0.00000
353	_	_	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
354	_	_	Cs	Cs	Čs	Cs	_	Cs	Cs		1.00000
355	_	_	Cs	Cs	Čs	Cs	Cs	Cs	Cs		1.00000
356	_	_	Cs	Cs	Čs	Cs	Cs	Cs	Cs		1.00000
357	_	_	C1	C1	CI	C1	CI	C1	C1		0.00000
358	_	_	C1	C1	C1	C1	C1	C1	C1		0.00000
359	_	_	C1	Č1	C1	C1	Č1	Č1	Č1		0.00000
360	_	_	C1	Č1	C1	C1	Č1	Č1	Č1		0.00000
361	_	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
362	_	_	Cs	Cs	Čs	Cs	Cs	Cs	Cs		1.00000
363	_	_	C1	C1	Č1	C1	Č1	Č1	C1		0.00000
364	_	_	C1	Č1	C1	C1	Č1	Č1	Č1		0.00000
365	_	_	C1	Č1	C1	C1	Č1	Č1	Č1		0.00000
366	_	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
367	_	_	C1	C1	Č1	C1	Č1	Č1	C1		0.00000
368	_	_	C1	Č1	C1	C1	Č1	Č1	Č1		0.00000
369	_	_	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
370	_	_	C1	C1	C1	C1	C1	C1	C1		0.00000
371	_	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
372	_	_	C1	C1	CI	C1	CI	C1	C1		0.00000
373	_	_	_	_	C3v	_	C3v	C3v	C3v		1 00000
374	_	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
375	_	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
376	_	_	-	_	C3v	C3v	C3v	C3v	C3v		1.00000
377	_	_	C1	C1	C1	C1	C1	CI	C1		0.00000
378	_	_	C1	C1	Ci	CI	CI	C1	C1		0.00000
379	_	_	C1	C1	Ci	C1	C1	C1	C1		0.00000
			~ -		~ -	~ -					0.00000

Table S34: Dataset: gupta/Na, part 4.

	SY	VA	Sym	Mol		libmsym		SC	FI		
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
3	D3h Td	D3h Td	D3h Td	D3h Td	D3h Td	D3h Td	D3h Td	D3h Td	D3h Td		1.00000
5	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
6	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		0.98814
7	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
8	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
10	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
11	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
12	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
14	C6v	C6v	C6v	C6v	C6v	C6v	C6v	C6v	C6v		1.00000
15	D6d	-	C6	C6	D6d	D6d	D6d	D6d	D6d	!	1.00000
16	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
17	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v		1.00000
19	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
20	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
21	C6v	C6v	C6	C6	C6v	C6v	C6v	C6v	C6v	!	1.00000
22	Cs C2	Cs C2	Cs C2	Cs C2	Cs C2	Cs	Cs C2	Cs C2	Cs C2		1.00000
23	Cs Cs	Cs Cs	Cs	Cs Cs	Cs	Cs	Cs	Cs Cs	Cs		1.00000
25	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
26	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
27	C1	C1	C1	C1	C1	C1	Cs C1	C1	C1		0.00000
29	C2	C_2	C2	C_2	C2	C2	C2	C2	C_2		1.00000
30	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
31	C3	C3	C3	C3	C3	C3	C3	C3	C3		1.00000
33	C1	C1	D20	C1	C1	C1	C1	C1	C1		0.00000
34	C2	C_2	C2	C_2	C2	C2	C_2	C2	C_2		1.00000
35	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
36	C2 C2v	C2 C2v	C2 C2v	C2 C2v	C2 C2v	C2 C2v	C2 C2v	C2 C2v	C2 C2v		1.00000
38	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		0.99984
39	C4v	C4v	C4	C4	C4v	C4v	C4v	C4v	C4v	!	1.00000
40	D2	D2	D2	D2	D2	D2	C1	D2	D2	!	1.00000
41 42	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs		0.00000
43	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
44	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
45	C1	C1	C1 C2	C1	C1	C1	C1	C1	C1		0.00000
46 47	C3 C1	C3 C1	C3 C1	C3 C1	C3 C1	C3 C1	 C1	C3 C1	C3 C1		0.00000
48	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
49	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
50	D3h C-	D3h	D3h C-	D3h	D3h	D3h	D3h	D3h C-	D3h		1.00000
52	C2v	C2v	C2v	C2v	C2v	C2v		C2v	C2v		1.00000
53	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
54	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	!	0.95000
55 56	Ih D2h	Ih D2h	Ci D2h	Ci D2h	Ih D2h	Ih D2h	Ih	Ih D2h	Ih D2h	!	0.95450
57	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
58	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
59	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
61	C3v	C3v	C2v C3v	C3v	C2v C3v	C2v C3v	_	C2v C3v	C2v C3v		1.00000
62	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
63	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}		1.00000
64	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	_	C2v C2v	C2v C2v		1.00000
66	Cs Cs	Cs Cs	C2V Cs	C ₂ v	C2V Cs	C2V Cs	Cs	Cs Cs	C ₂ v		1.00000
67	C2v	C2v	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
68	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
69 70	C1 Ca	C1 Ca	C1 Ca	C1 Ca	C1 Ca	C1 Ca	C1 Ca	C1 Ca	C1 Ca		0.00000
70	C2v	C_{2v}	C2v	C2v	C2v	C2v	Cs	C2v	C2v	1	1.00000
72	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
73	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Ι.	1.00000
74	D5h	D5h	D5h	05 D5h	D5h	D5h	_	D5h	D5h		1.00000
76	C2v	C2v	C2v	C2v	C2v	C_{2v}	-	C2v	C2v		1.00000
77	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	_	C2v	C2v		1.00000
78	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		0.99543
80	C4v	C4v	C4v	C4v	C4v	C4v	_	C4v	C4v		1.00000
81	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
82	C2v	C2v	C2v	C2v	C2v C2v	C2v C2v	C2v	C2v	C2v		1.00000
84	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
85	Cs	Cs	Cs	Cs	Cs	Cs	Čs	Cs	Cs		1.00000
86	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
87 88	Cs	Cs	Cs	Cs	Cs Ca		Cs	Cs	Cs		1.00000
89	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
90	Cs	Ċs	Cs	Ĉs	Cs	Cs	Cs	Cs	Ĉs		1.00000
91	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C_{2v}	C2v	C_{2v}		1.00000
92 93	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		1.00000
94	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
95	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}	C2v	C2v		1.00000
96	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
97 98	Cs	Cs Cs	Cs	Cs Cs		Cs Cs	C1	Cs Cs	Cs	· ·	1.00000
99	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	l .	1.00000
100	C5v	C5v	C5v	C5	C5v		C5v	C5v	C5v	!	1.00000
101	D5h D2b	D5h	D5h D2b	C5	D5h	D5h	-	D5h	D5h	'	1.00000
102	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
104	C2v	C_{2v}	C2v	C2v	C2v	C_{2v}	-	C2v	C_{2v}		1.00000
105	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
106	Cs	Cs	Cs	Cs	Cs	Cs Ce	Cs	Cs	Cs		1.00000
107	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
109	Cs	Cs	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	\mathbf{Cs}	Cs	\mathbf{Cs}		1.00000
110	Cs C-	Cs C-	Cs C-	Cs C-	Cs C-	Cs C-	Cs C-	Cs C-	Cs C-		1.00000
111	Us	Us		US		US	Cs.		Us	I	1 1.00000

Table S35: Dataset: gupta/Pb, part 1.

	I SY	VA	l Svm	Mol	I	libmsym		l so	FI	I	I
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
112	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
113	C2v	C_{2v}	C2v	C_{2v}	C_{2v}	C2v	_	C2v	C_{2v}		1.00000
114	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
115	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
116	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
117	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
118	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
119	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
120	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
121	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
122	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
123	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
124	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
125	C3v	C3v	-	_	C3v	C3v	C3v	C3v	C3v		1.00000
126	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
127	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
128	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
129	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
130	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
131	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
132	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
133	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
134	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
135	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
136	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v		1.00000
137	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
138	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
139	C2v	C2v	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
140	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		1.00000
141	C2v	C2v	C2v	C_{2v}	C2v	C2v	-	C2v	C_{2v}		1.00000
142	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
143	C3v	C3v	-	_	C3v	-	C3v	C3v	C3v		1.00000
144	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
145	C5v	C5v	C5v	C5v	C5v		-	C5v	C5v		1.00000
146	D5h	D5h	D5h	D5h	D5h	D5h	-	D5h	D5h		1.00000
147	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
148	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	-	C2v	C2v		1.00000
149	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
150	C2v	C2v	C2v	C2v	C2v	C_{2v}	-	C2v	C2v		1.00000

Table S36: Dataset: gupta/Pb, part 2.

	SY	VA	Syn	Mol		libmsym		sc	FI		
3	0.001 D3h	0.05 D3h	0.001 D3h	0.05 D3h	D3h	D3h	D3h	0.001 D3h	0.05 D3h	diff	dot product 1.00000
4	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.95632
5 6	D3h Oh	D3h Oh	D3h Oh	D3h Oh	Oh D3h	D3h Oh	D3h Oh	D3h Oh	D3h Oh		0.93051
7	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
8	D2d C2v	D2d C2v	D2d C2v	D2d C2v	D2d C2v	D2d C2v	D2d C2v	D2d C2v	D2d C2v		1.00000
10	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
11	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
12	C2 Cs	C ₂	C2 Cs	C ₂	Cs	C ₂ Cs	C ₂ Cs	Cs Cs	C ₂		1.00000
14	C6v	C6v	C6v	C6v	C6v	C6v	C6v	C6v	C6v		1.00000
15 16	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs	Cs Cs	Cs Cs	Cs Cs		1.00000
17	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
18	C4v D4d	C4v D4d	C4v S8	C4v	C4v D4d	C4v D4d	C4v D4d	C4v D4d	C4v D4d	Ι,	1.00000
20	C2v	C2v	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	· ·	1.00000
21	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
22 23	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1		0.00000
24	C2	C2	C2	C2	C2	C_2	C2	C2	C2		1.00000
25 26	C2 C2	C2 C2	C2 C2	C2 C2	C2 C2	C2 C2	C2 C2	C2 C2	C2 C2		1.00000
27	C_2	C_2	C2	C_2	C2	C2	C_2	C2	C_2		1.00000
28	D6d C2	-	C6 C2	C6 C2	D6d	D6d C2	D6d C2	D6d C2	D6d C2	!	1.00000
30	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
31	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
32 33	C1 C1	C1 C1	C1 C1	C1 C1		C1 C1	C1 C1	C1 C1	C1 C1		0.00000
34	C3	C3	C3	C3	C3	C3	C3	C3	C3		1.00000
35	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
37	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
38	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
39 40	Cs	Cs Cs	C2v Cs	Cs Cs	C2V Cs	C2V Cs	C2V Cs	Cs Cs	C2v Cs		1.00000
41	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	\mathbf{Cs}		1.00000
42 43	D4 C4	C4	D4 C4	C4	C4	D4	D4 C4	D4 C4	D4 C4		1.00000
44	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}		1.00000
45 46	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs		1.00000
40	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
48	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
49 50	Cs	C ₂ v Cs	C2V Cs	C ₂ v Cs	Cs	Cs	Cs Cs	Cs	C ₂ v Cs		1.00000
51	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
52 53	C_{2v} C1	C_{2v} C1	C2v C1	C_{2v} C1	C2v C1	C2v C1	C_{2v} C1	C2v C1	C_{2v} C1		1.00000
54	Č1	C1	C1	Č1	C1	C1	C1	Č1	C1		0.00000
55 56	C1	C1	C1 C1	C1	C1 C1	C1 C1	C1	C1	C1		0.00000
57	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
58 59	C1 C1	C1	C1 C1	C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1		0.00000
60	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
61	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
63	C1	C1	C1	C1		C1 C1	C1	C1	C1		0.00000
64	C2	C2	C2	C2	C2	C_2	C2	C2	C2		1.00000
65 66	C1 C1	C1 C1		C1 C1		C1 C1	C1 C1	C1 C1	C1 C1		0.00000
67	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
68 60	C1	C1	C1 C1	C1	C1 C1	C1 C1	C1	C1	C1		0.00000
70	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
71	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
72 73	Cs Cs	Cs	Cs Cs	Cs	Cs	Cs	Cs Cs	Cs Cs	Cs		1.00000
74	\mathbf{Cs}	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	\mathbf{Cs}	\mathbf{Cs}	\mathbf{Cs}		1.00000
75 76	C_{2v}	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1		1.00000
77	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
78 70	C1 C2v	C1 C2w	C1 C2w	C1 C2v	C1 C2v	C1 C2v	C1 Ca	C1 C2v	C1 C2w	Ι.	0.00000
80	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	· ·	1.00000
81	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
82 83	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs	Cs Cs	Cs Cs	Cs Cs		1.00000
84	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
85 86	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1	C1 C2v	C1 C2v		0.00000
87	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v C2v	C_{2v}	C2v	C_{2v}		1.00000
88	C2v	C_{2v}	C2v	C2v	C2v	C2v	Cs	C2v	C_{2v}	!	1.00000
89 90	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
91	C_{2v}	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
92 93	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs		1.00000
94	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
95 96	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs _	Cs C2v	Cs C2v		1.00000
97	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
98	C2v	C_{2v}	C2v	C2v	C2v	C2v	- C-	C2v	C_{2v}		1.00000
99 100	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	Us —	C2v	C_{2v}		1.00000
101	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
102	C1 C1	C1 C1		C1 C1		C1 C1	C1 C1	C1 C1	C1 C1		0.00000
104	C1	C1	C1	C1	C1	Č1	C1	C1	C1		0.00000
105 106	C1 C1	C1	C1 C1	C1	C1 C1	C1 C1	C1 C1	C1 C1	C1		0.00000
107	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
108	C1	C1	C1 C1	C1	C1	C1	C1	C1	C1		0.00000
1109	C1	C1	C1	C1		C1	C1	C1	C1		0.00000
111	C2	C2	C2	C2	C2	C2	-	C2	C2		1.00000

Table S37: Dataset: gupta/Zn, part 1.

	SY	VA	Sym	Mol		libmsym		SO	FI	I	
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
112	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
113	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
114	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
115	C2	C2	C2	C2	C2	C2	-	C2	C2		1.00000
116	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
117	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
118	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
119	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
120	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
121	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
122	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
123	C2v	C2v	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
124	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
125	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000

Table S38:	Dataset:	gupta/Zn,	part	2.

	SY	VA	Syn	Mol		libmsym	., ,	SC	OFI OF		
3	D3h	0.05 D3h	D3h	0.05 D3h	D3h	D3h	D3h	D3h	0.05 D3h	аіп	1.00000
4	Td	Td	Td	\mathbf{Td}	Td	Td	Td	Td	Td		0.94001
5	D3h Oh	D3h Oh	D3h Ob	D3h Ob	D3h Oh	D3h Ob	D3h Oh	D3h Oh	D3h Ob		1.00000
7	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
8	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
9 10	C2v C3v	C2v C3v	C2v C3v	C2v C3v	C2v C3v	C2v C3v	C2v C3v	C2v C3v	C2v C3v		1.00000
11	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
12	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
13	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
15	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}		1.00000
16	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
18	C5v	C_{5v}	C5	C_{5}^{2}	C5v	C5v	C5v	C5v	C_{5v}	!	1.00000
19	D5h	D5h	C5	C5	D5h	D5h	D5h	D5h	D5h	!	1.00000
20 21	C2v C2v	C_{2v}	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C_{2v} C_{2v}		1.00000
22	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
23	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
24 25	Cs	Cs	Cs C1	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
26	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.99957
27	C2v Ca	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C2v Ca		1.00000
29	D3h	D3h	D3h	D3h	D3h	D3h	_	D3h	D3h		1.00000
30	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
31	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v		1.00000
33	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
34	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
36	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
37	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
38	Oh C5v	Oh	Oh C5	Oh C5	Oh C5rr	Oh C5w	Oh	Oh C5v	Oh C5v	,	0.80819
39	C5v	C_{5v}	C5	C5	C5v	C5v	_	C5v	C_{5v}	i	1.00000
40	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
41	Cs	Cs Cs	Cs	Cs	Cs	Cs Ce	Cs	Cs Ce	Cs		1.00000
43	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
44	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
45 46	C1 C2v	C1 C2v	C1 C2v	C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C2v		1.00000
47	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
48	Cs C2v	Cs	Cs C2v	Cs	Cs C2v	Cs C2v	Cs	Cs C2v	Cs		1.00000
49 50	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
51	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
52 53	C3v C2v	C3v C2v	C2v	C2v	C3v C2v	C3v C2v	C3v	C3v C2v	C3v C2v		1.00000
54	C5v	C5v	C5	C5	C5v	C5v	C5v	C5v	C5v	!	1.00000
55	Ih	Ih C2	Ih	Ih	Ih	Ih	Ih C2	Ih	Ih C2		1.00000
57	Cs	Cs	C1	Cs	Cs	-	Cs	Cs	Cs	!	1.00000
58	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
59 60	C2v	C_{2v}	C2	C2v Ce	C2v	C2v	C2v Ce	C2v	C2v Ce	!	1.00000
61	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}		1.00000
62	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
63 64	Cs	Cs	CI	Cs	Cs	CI	CI	Cs	CI		1.00000
65	C2	C_2	C2	C_2	C2	C_2	$\tilde{C2}$	C2	C_2		1.00000
66 67	C1 Ce	C1 Cr	C1 Ce	C1 Ce	C1 Ce	C1 Ce	C1 Ce	C1 Ce	C1 Ce		0.00000
68	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
69	C5v	C5v	C5	C5	C5v	C5v	-	C5v	C5v	!	1.00000
70 71	C5v C5v	C_{5v}	C5v C5v	C5V C5	C5v C5v	C5v C5v	_	C5v C5v	C_{5v}	!	1.00000
72	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	-	Cs	\mathbf{Cs}		1.00000
73 74	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs	Cs	Cs Cs	Cs Cs	Cs Cs		1.00000
75	D5h	D5h	D5h	C_{5}	D5h	-	-	D5h	D5h	!	1.00000
75i	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
76 76i	C1	C1	C1 C1	C1	C1 C1	C1	C1	C1	C1		0.00000
77	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
77i 78	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs		0.00000
79	C2v	C_{2v}	C2v	C2v	C2v	C2v	Cs	C2v	C_{2v}	!	1.00000
80	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
82	C2V C1	C1	C2V C1	C2V C1	C1	C2V	C1	C1	C2V C1		0.00000
83	C2v	C2v	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
84 85	C1 C3v	C1 C3v	C1	C1	C1 C3v	C1 C3v	C1 C3v	C1 C3v	C1 C3v		0.00000
86	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
87	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
88 89	Cs C3v	Cs C3v	C1 -	Cs	Cs C3v	Cs C3v	Cs C3v	Cs C3v	Cs C3v	'	1.00000
90	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	Cs		1.00000
91	Cs	Cs	C1 C2:	\mathbf{Cs}	Cs	Cs	Cs	Cs	Cs	!	1.00000
92 93	C1	C1	C3V C1	 C1	C1 C1	C1	C1	C1	C1		0.00000
94	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
95 96	C1 C1	C1	C1 C1	C1	C1 C1	C1	C1 C1	C1 C1	C1 C1		0.00000
97	C1	C1	C1	Č1	C1	Č1	C1	C1	Č1		0.00000
98	Td C-	Td C-	Td C-	Td C-	Td C-	Td C-	Td C-	Td C-	Td C-		0.98711
991	C2v	C2v	C2v	C_{2v}	C2v	C_{2v}	Cs	C2v	C_{2v}	!	1.00000
100	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
101	C2v C2v	C_{2v}	C2v	C_{2v}	C2v C2v	C2v		C2v C2v	C_{2v}	, I	1.00000
102i	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	Cs	l .	1.00000
103	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
1031	C2v	C_{2v}	C2v	C_{2v}	C2v	C1 C2v	C1 C2v	C2v	C2v		1.00000

Table S39: Dataset: LJ, part 1.

1	SY	VA	Svm	Mol	I	libmsvm		so	FI	1	I
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
104i	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
105	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
106	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
107	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
108	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
109	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
110	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
111	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
112	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
113	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs	Cs		1.00000
114	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
115	C5v	C5v	C5v	C5v	C5v	-	-	C5v	C5v		1.00000
116	C5v	C5v	C5v	C5v	C5v	-	_	C5v	C5v		1.00000
117	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
118	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
119	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
120	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
121	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
122	C1	C1		C1		C1	C1		C1		0.00000
123	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
124	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
125	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
126	CI	CI	CI	CI		CI	CI	CI	CI		0.00000
127	C2V	C2V	C2V	C2V	C2V	C2V		C2V	C2V		1.00000
128	C1	C-	C1	C-		C1 C-	C1	C1	C-		1.00000
129	CI	CI	CI	CI	CI	CI	CI	CI	CI		1.00000
121	C2v	Car	C2rr	Car	Car	C2rr	CI	C2w	Car		1.00000
122	C2V	C1	C2V	C1	C1	C1	C1	C2V	C1		0.00000
122	Ca	Ca	Ca	Ca		Ca	Ca	Ca	Ca		1.00000
134	Cav	Cav	05		Cav	Cav	Cs_	Cav	Cav		1.00000
135	Th	TP	Ci	Ci	Th	Th	Ib	TP	TP	,	0.91300
136	C5v	C5v	C5v	C5	C5v	C5v	-	C5v	C5v		1 00000
137	C2v	C2v	C2v	C2v	C2v	C2v	_	C2v	C2v		1 00000
138	C3v	C3v			C3v		_	C3v	C3v		1.00000
139	C2v	C2v	C2v	C2v	C2v	C2v	_	C_{2v}	C2v		1.00000
140	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
141	C5v	C5v	C5v	C5v	C5v	_	_	C5v	C5v		1.00000
142	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
143	C2v	C2v	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
144	C3v	C3v	_	_	C3v	C3v	_	C3v	C3v		1.00000
145	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
146	C5v	C5v	C5v	C5	C5v	-	-	C5v	C5v	1	1.00000
147	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	1	0.99392
148	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
149	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
150	C3v	C3v	-	C3	C3v	-	-	C3v	C3v	!	1.00000

Table S40: Dataset: LJ, part 2.

	SY	VA	Sym	Mol		libmsym	·, ·	SO	FI	1.0	
5A	D3h	0.05 D3h	D3h	0.05 D3h	D3h	D3h	D3h	0.001 D3h	0.05 D3h	ап	1.00000
6A	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		1.00000
7A	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
8A 8B	D2d Ce	D2d Ce	D2d Ce	D2d Ce	D2d Ce	D2d Cs	D2d Ce	D2d Cs	D2d Ce		1.00000
9A	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
9B	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
10A 10B	D4d C2v	D4d C2w	D4d C2v	D4d C2w	D4d C2v	D4d C2v	D4d C2v	D4d C2u	D4d C2u		1.00000
10B 11A	D4d	D4d	S8	S8	D4d	D4d	D4d	D4d	D4d	!	1.00000
11B	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
11C	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}	C_{2v}		1.00000
11D 11E	Cs C2	C_{2v}	Cs C2	Cs	Cs C2	Cs C2	C_{2v}	Cs C2	C_{2v}	!M	0.99983
11E 11F	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
12A	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
12B	C5v	C5v	C5v	C5v	C5v	C5v	C5v C5v	C5v	C5v		1.00000
120 12D	D2d	D2d	D2d	D2d	D2d	D2d	D2d	D2d	D2d		1.00000
12E	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
13A	Ih	-	Ci	Ci	Ih	Ih	Ih	Ih	Ih	!	0.96634
13B	D5h C2v	D5h C2v	C5 C2v	C5 C2v	D5h C2v	D5h C2v	D5h C2y	C2v	D5h C2v	!	1.00000
14B	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
14C	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
15A	D6d	-	C6	C6	D6d C2	D6d	D6d C2	D6d	D6d	!	1.00000
15B 15C	C2v C2v	C2v C2v	C2v C2v	C_{2v}	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v		1.00000
16A	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
16B	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
16C	D3h	D2v D3b	D3h	C2v D3b	C2v D3b	C2v D3h	C2v D3h	D2v D2b	C2v D3b		1.00000
17B	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
17C	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs		1.00000
17D 17E		C2	C2 C2	C2	C2 C2	C2	C2	C2	C2		1.00000
18A	C2V	C_2^{2v}	C2V C2	C_2^{2v}	C2V C2	C2v C2	C_2^{\vee}	C_2^{2v}	C_2^{2v}		1.00000
18B	C5v	C5v	C5	C5	C5v	C5v	C5v	C5v	C5v	1	1.00000
18C	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
18D 19A	D5h D5h	D5h D5h	C5	C5	D5h D5h	D5h D5h	D5h D5h	D5h D5h	D5h D5h	!	1.00000
19B	C2v	C2v	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v		1.00000
20A	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
20B	C2v C2v	C2v C2v	C2v C2v	C_{2v}	C2v C2v	C2v C2v	C_{2v}	C2v C2v	C_{2v}		1.00000
21A 21B	C1	C2V C1	C1	C2V C1	C2V C1	C1	C1	C1	C2V C1		0.00000
21C	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
22A	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
22B 23A	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
23B	D3h	D3h	D3h	D3h	D3h	D3h	_	D3h	D3h		1.00000
23C	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
23D 24 A	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
24Aprime	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
24B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
24C 25A	C2v Ce	C2v Ce	C2v Ce	C2v	C2v	C2v	C2v Ce	C2v Ce	C2v		1.00000
25Aprime	C2v	C2v	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v		1.00000
25B	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
25C	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
26B	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
26C	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
27A	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
27B 27C	Cs	C2v Cs	Cs	Cs Cs	C2V Cs	C2V Cs	C2V Cs	C2v Cs	Cs Cs		1.00000
27D	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Čs	Cs		1.00000
27E	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
28A 28B	Cs	Cs	Cs	Cs	Cs	Cs	Cs _	Cs	Cs		1.00000
28C	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
28D	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
28E 29A	D3h	C2v D3b	C2v D3b	C2v D3b	C2v D3b	C2v D3h	C2v	C2v D3b	C2v D3b		1.00000
29B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
29C	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
29D	C2v D5b	C2v D5b	C2v C5	C2v C5	C2v D5b	C2v D5b	C2v D5b	C2v D5b	C2v D5b	,	1.00000
29E 29F	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
30A	C2v	C2v	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
30B	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
30C 30D	Cs	C2v Cs	Cs	Cs Cs	C2V Cs	C2V Cs	Cs	C2v Cs	Cs Cs	:	1.00000
30Dprime	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	\mathbf{Cs}	Cs	Cs		1.00000
30E	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
31A 31B	CI	CI	CI	Cs	Cs	Cs	Ci	Cs	Cs		1.00000
31C	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
31D	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
31E 31F	C2v Ce	C2v Ce	C2v Ce	C2v	C2v	C2v	C2v Ce	C2v Ce	C2v		1.00000
32A	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
32B	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C_{2v}	C_{2v}		1.00000
32C 32D	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		1.00000
32E	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
33A	Cs	Ĉs	Ĉs	Ĉs	Cs	Ĉs	Cs	Cs	Ċs		1.00000
33B 33C	C5v	C5v	C5	C5	C5v	C5v	C5v	C5v	C5v	!	1.00000
33D	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}	C_{2v}		1.00000
33E	C2v	C_{2v}	C2v	C_{2v}	C2v	C_{2v}	C_{2v}	C_{2v}	C_{2v}		1.00000
33F	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
34A 34B	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	D5h	C2v	C_{2v}	!	1.00000
34C	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
34D	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
34E 34F	C2v	C_{2v}	C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v		1.00000
			1							i	

Table S41: Dataset: morse, part 1.

name	SY 0.001	VA 0.05	Sym 0.001	Mol 0.05	'default'	libmsym 'medium'	'loose'	SC 0.001	FI 0.05	diff	dot product
35A	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
35B 35C	C3v C1	C3v C1	C3v C1	C3v C1	C3v C1	C3v C1	C3v C1	C3v C1	C3v C1		0.00000
35D	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	-	C2v	C_{2v}		1.00000
35E 35F	C2v C3v	C2v C3v	- C2v	C2v	C2v C3v	C2v C3v	C2v C3v	C2v C3v	C2v C3v		1.00000
36A	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
36C	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
36D	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
36F	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
36G	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
37B	C1	C1	C1 C1	C1	C1 C1	C1	C1	C1	C1		0.00000
37C	C2v C2v	C_{2v}	C2v C2v	C_{2v}	C2v C2v	C2v C2v	C_{2v}	C2v C2v	C_{2v}		1.00000
37E	C3v	C3v	-	-	C3v	-	C3v	C3v	C3v		1.00000
38A 38B	D2 C1	D2 C1	D2 C1	D2 C1	D2 C1	D2 C1	C2 C1	D2 C1	D2 C1	!	1.00000
38C	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
38D 38E	Oh C5v	Oh C5v	Oh C5	Oh C5	Oh C5v	Oh C5v	Oh	Oh C5v	Oh C5v	Ι,	0.98693
39A	C2v	C_{2v}	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C_{2v}		1.00000
39B 39C	C5v C4v	C5v C4v	C5 C4	C5 C4	C5v C4v	C5v C4v	_	C5v C4v	C5v C4v	!	1.00000
40A	Cs	Cs	Cs	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	· ·	1.00000
40B 40C	Cs D4h	Cs D4h	Cs D4h	Cs C4h	Cs D4h	Cs D4h	Cs D4h	Cs D4h	Cs D4h	, I	1.00000
41A	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C_{2v}	C2v	C_{2v}		1.00000
41B 41C	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	C2v	Cs C2v	Cs C2v		1.00000
41D	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
41E 41F	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C_{2v}		1.00000
42A	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
42B 42C	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs		1.00000
42D	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
42E 43A	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v		1.00000
43B	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
43C 43D	C2v C2v	C_{2v} C_{2v}	C2v C2v	C_{2v} C_{2v}	C2v C2v	C2v C2v	C2V Cs	C2v C2v	C2v C2v	!	1.00000
43E	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
44A 44B	C5V C1	C3V C1	C1 C1	C5 C1	C5V C1	C1 C1	C5V C1	C3V C1	C3V C1	·	0.00000
44C	Cs	Cs	Cs	Cs	Cs C=	Cs	Cs C=	Cs C=	Cs C-		1.00000
44D 44E	C1	C1 C1	C1 C1	C1	C1 C1	C1 C1	C1 C1	C1	C1		0.00000
45A 45B	Ih C1	Ih C1	Ci	Ci C1	Ih C1	Ih C1	Ih C1	Ih C1	Ih C1	!	0.98813
45B 45Bprime	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
45C 45D	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v	Cs C2v		1.00000
45E	C2v C2v	C_{2v}	C2v C2v	C_{2v}	C2v C2v	C2v C2v	C_{2v}	C2v C2v	C_{2v}		1.00000
45F 46 A	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs Cs		1.00000
46B	C2v	C_{2v}	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C_{2v}		1.00000
46C 46D	Cs Cs	Cs Cs	Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs		1.00000
46E	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
46Eprime 47A	Cs C3	Cs C3	Cs C3	Cs C3	Cs C3	Cs C3	Cs _	Cs C3	Cs C3		1.00000
47B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
47C 47D	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs		1.00000
48A	C2v	C_{2v}	C2v	C_{2v}	C2v	C_{2v}	-	C2v	C2v		1.00000
48B 48Bprime	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	C1	Cs C1	Cs C1		0.00000
48C	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	_	C2v	C_{2v}		1.00000
48D 49A	Cs	Cs	Cs	Cs	Cs			Cs	Cs		1.00000
49B	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
490 49D	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
50A 50B	C5v Cs	C5v Cs	C5v Cs	C5v Cs	C5v Cs	C5v Cs	C5v Cs	C5v Cs	C5v Cs		1.00000
50C	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
50D 51A	D3h C2	D3h C2	D3h C2	D3h C2	D3h C2	D3h C2	D3h _	D3h C2	D3h C2		1.00000
51B	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
51Bprime 51C	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs		0.00000
51D	Cs	Ċs	Cs	Ċs	Cs	Ċs	-	Cs	Cs		1.00000
51E 52A	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs		1.00000
52B	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
52C 52D	C2v C2v	C_{2v} C_{2v}	C2v C2v	C_{2v} C_{2v}	C2v C2v	C2v C2v	C2v	C2v C2v	C_{2v} C_{2v}		1.00000
52E	C2v	C2v	C2v	C_{2v}	C2v	C2v	-	C2v	C2v	.	1.00000
53A 53B	D6d C2v	C_{2v}	C6 C2v	C_{C2v}	C2v	D6d C2v	-C2v	C2v	C_{2v}	'	1.00000
53C	Cs C-	Cs C-	Cs C-	Cs C-	Cs	Cs		Cs C-	Cs C-		1.00000
54B	C5v	C_{5v}	C5	C5	C5v	C_{5v}	C_{5v}	C5v	C_{5v}	!	1.00000
54C 54D	C2v C2v	C_{2v}	C2v C2v	C_{2v}	C2v C2v	C_{2v}	C2v	C2v C2v	C_{2v}		1.00000
55A	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
55B 55C	Ih C2v	Ih C2v	Ci C2v	Ci C2v	Ih C2v	Ih C2v	Ih C2v	Ih C2v	Ih C2v	!	0.94555
55D	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
56A 56B	Cs C3v	Cs C3v	Cs -	Cs _	Cs C3v	_	Cs C3v	Cs C3v	Cs C3v		1.00000
56C	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
56D 56E	Cs D3h	Cs D3h	Cs D3h	Cs D3h	D3h	Cs D3h	Cs D3h	Cs D3h	Cs D3h		1.00000 1.00000
57A	D3h	D3h	D3h	C3h	D3h	D3h	D3h	D3h	D3h	!	1.00000
57B 57C	C2v	C_{2v}	C2v	C_{2v}	C2v	c_{2v}	C2v	C2v	C2v		1.00000

Table S42: Dataset: morse, part 2.

name	SY	VA 0.05	Sym	Mol	'default'	libmsym 'medium'	'loose'	SO	FI 0.05	diff	dot product
57D	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	dill	1.00000
58A 58B	Cs C3v	Cs C3v	Cs C3v	Cs C3v	Cs C3v	Cs C3v	Cs C3v	Cs C3v	Cs C3v		1.00000 1.00000
58C	D3h	D3h	D3h	D3h	D3h	D3h	_	D3h	D3h		1.00000
58D 58E	C1 C3v	C3v	-	-	C1 C3v	C1 C3v	C1 C3v	C1 C3v	C1 C3v		1.00000
59A	C3v	C3v	_	_	C3v	C3v	C3v	C3v	C3v		1.00000
59B 59C	C2V C1	C2V C1	C2V C1	C1	C1		C1	C2V C1	C1		0.00000
59D	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
60A	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs	Cs		1.00000
60B	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
60D	C2V Cs	Cs Cs	C ₂ V Cs	C2V Cs	Cs Cs	Cs	Cs	Cs	C ₂ V Cs		1.00000
60E 60F	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs		1.00000 1.00000
61A	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.80426
61B 61Bprime	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs		1.00000 1.00000
61C	C3v	C3v	C3v	C3v	C3v	C3v	-	C3v	C3v		1.00000
62A 62B	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs		1.00000 1.00000
62C	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
62D 62E	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1	C2v C1	C1	C2v C1	C2v C1		0.00000
62F	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
62G 62H	C1	C1	C1	C1	C1	C1	_	C1	C1		0.00000
63A	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		1.00000
63C	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
63D 64A	Cs D3d	Cs D3d	Cs S6	Cs S6	Cs D3d	Cs D3d	Cs _	Cs D3d	Cs D3d	!	1.00000 1.00000
64B	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
64C 64D	C2v Cs	C2v Cs	C2v Cs	C_{2v}	C2v Cs	C2v Cs	C1 Cs	C2v Cs	C_{2v}	!	1.00000 1.00000
65A	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
65C	C1 C2	C1 C2	C1 C2	C1 C2	C1 C2	C1 C2	C1 C2	C1 C2	C1 C2		1.00000
65D 65E	C1 C2	C1 C2::	C1 C2m	C1	C1	C1 C2rr	C1	C1	C1		0.00000
65F	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
65G 65H	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs		0.00000 1.00000
66A	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
66B 66C	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1		0.00000 0.00000
66D	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
66F	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
66G 67A	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
67B	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
67C 67D	C2 C2v	C2 C2v	C2 C2v	C2 C2v	C2 C2v	C2 C2v	C2	C2 C2v	C2 C2v		1.00000 1.00000
67E	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	Cs	C2v	C_{2v}	!	1.00000
67F 68A	C3v Cs	C3v Cs	Cs	Cs	C3v Cs	C3v Cs	C3v Cs	C3v Cs	C3v Cs		1.00000 1.00000
68B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
68C 68D	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		1.00000 0.00000
68Dprime	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
68F	C2V Cs	C2V Cs	C2V Cs	Cs	Cs	Cs	C2V C1	Cs	Cs	!	1.00000
68G 68H	C2v C3v	C_{2v}	C2v	C_{2v}	C2v C3v	C2v C3v	C2v C3v	C2v C3v	C2v C3v		1.00000 1.00000
69A	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
69B 69C	C1 C5v	C1 C5v	C1 C5	C1 C5	C1 C5v	C1 C5v	C1	C1 C5v	C1 C5v	!	0.00000 1.00000
69D	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
69F	C1	C1	C1 C1	C1	C1	C1	C1	C1	C1		0.00000
69G 70 A	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1 C2v	C1	C1 C2v	C1 C2v	C1 C2v		0.00000 1.00000
70B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
70C 70D	C5 C5v	C_{5v}	C5 C5v	C_{5v}	C5 C5v	C5v	_	C5 C5v	C_{5v}		1.00000 1.00000
70E	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
70F 70G	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
71A 71P	C1 C5	C1 C5	C1 C5	C1 C5	C1 C5	C1 C5	C1	C1 C5	C1 C5		0.00000
71C	C5v	C_{5v}	C5v	C5v	C5v	C5v	-	C5v	C5v		1.00000
71D 71E	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	C2v Cs	Cs	C2v Cs	C2v Cs		1.00000 1.00000
72A	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
72B 72C	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1	C1 Cs	C1 Cs		0.00000 1.00000
72D	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
72E 72F	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs	C1 Cs		0.00000 1.00000
73A	C3	C3	C3	C3	C3	C3	C3	C3	C3		1.00000
73C	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
73D 73E	Cs	Cs	Cs	Cs	Cs	Cs Cc	Cs Ca	Cs	Cs		1.00000
73F	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
74A 74B	C3v Cs	C3v Cs	C3v Cs	C3v Cs	C3v Cs	C3v Cs	C3v Cs	C3v Cs	C3v Cs		1.00000 1.00000
74C	C5v	C5v	C5	Č5	C5v	- 2		C5v	C5v	!	1.00000
74D 75A	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs Cs		1.00000 1.00000
75B 75C	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
75D	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
76A 76B	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1	Cs C1		1.00000
76C	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
76D	C1	C1	C1	C1	C1	C1	C1	C1	C1	I	0.00000

Table S43: Dataset: morse, part 3.

	SY	VA	Sym	Mol	I	libmsym		so	FI	I	
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
76E	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
76F	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
76G	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
77A	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
77B	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
77C	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
77D	C2v	C2v	C2v	C2v	C2v	C2v	Cs	C2v	C2v	!	1.00000
77E	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
78A	C3	C3	C3	C3	C3	C3	-	C3	C3		1.00000
78B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
78C	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
78D	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
78Dprime	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
78E	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
78F	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
78G	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
79A	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
79B	C2v	C2v	C2v	C2v	C2v	-	-	C2v	C2v		1.00000
79C	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
79D	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
79E	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
79F	D3h	D3h	D3h	-	D3h	D3h	D3h	D3h	D3h		1.00000
80A	C3	C3	C3	C3	C3	C3	C3	C3	C3		1.00000
80B	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
80C	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
80D	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
80E	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
80F	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
80G	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
147A	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
147B	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	!	0.97282
147C	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
147D	Cs	Cs	Cs	Cs	Cs	Cs	C1	Cs	Cs	!	1.00000
147E	C3v	C3v	-	C3	C3v	C3v	C3v	C3v	C3v	!	1.00000

Table S44: Dataset: morse, part 4.

	SY	VA	Sym	Mol		libmsym		SOFI			
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
11	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}		1.00000
12	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
13 14	Th C3v	Th C3v	Th C3v	Th C3v	C3v	Th C3v	Th C3v	Th C3v	Th C3v		1.00000
15	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
16 17	Cs C2	Cs C2	Cs C2	Cs C2	Cs C2	Cs C2	Cs C2	Cs C2	Cs C2		1.00000
18	C5v	C_{5v}	C5	C_{5}^{2}	C5v	C5v	C5v	C5v	C_{5v}	!	1.00000
19	D5h	D5h	C5	C5	D5h	D5h	D5h	D5h	D5h	!	1.00000
20 21	C2V C2	C2V C2	C2V C2	C2V C2	C2V C2	C2V C2	C2V C2	C2V C2	C2v C2		1.00000
22	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	\mathbf{Cs}		1.00000
23 24	D3h D3	D3h D3	D3h D3	D3h D3	D3h D3	D3h D3	D3h	D3h D3	D3h D3		1.00000
25	C3	C3	C3	C3	C3	C3	C3	C3	C3		1.00000
26	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.87031
27	Т	т	- T	т		T	Т	Т	т		0.00000
29	C3	C3	C3	C3	C3	C3	C3	C3	C3		1.00000
30	Cs C2	Cs C2	Cs C2	Cs C2	Cs C2	Cs	Cs C2	Cs C2	Cs C2		1.00000
32	D3	D3	D3	D3	D3	C3	-	D3	D3	!	1.00000
33	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
34 35	D3	D3	D3	D3	D3	D3	-	D3	D3		1.00000
36	C2	C2	C2	C2	C2	C_2	C2	C2	C2		1.00000
37 38	C2 C1	C2 C1	C2 C1	C2 C1	C2 C1	C2 C1	C2 C1	C2 C1	C2 C1		1.00000
39	C5	C5	C5	C5	C5	-	C5	C5	C5		1.00000
40	C1	Cs C1	C1	Cs	Cs	Cs		C1	Cs C1	!M	1.00000
41 42	D2	D2	D2	D2	D2	D2	D2	D2	D2		1.00000
43	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
44 45	Cs D3	Cs D3	Cs D3	Cs D3	Cs D3	Cs D3	Cs _	Cs D3	Cs D3		1.00000
46	C2	C_2	C2	C_2	C2	C2	C2	C2	C_2		1.00000
47	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
48 49	C1 C3v	C1 C3v	C1 C3v	C1 C3v	C3v	C1 C3v	C1 C3v	C1 C3v	C1 C3v		1.00000
50	Cs	Cs	Cs	Cs	Cs	Cs		Cs	Cs		1.00000
51 52	C2v C3v	C_{2v}	C2v	C_{2v}	C2v C3v	C2v C3v	C2v C3v	C2v C3v	C2v C3v		1.00000
53	C2v	C_{2v}	C2v	C2v	C2v	C2v	-	C2v	C_{2v}		1.00000
54	C5v	C5v	C5	C5	C5v	C5v	-	C5v	C5v	!	1.00000
56	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
57	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
58 59	C3v C3v	C3v C3v	C3v C3v	C3v C3v	C3v C3v	C3v C3v	C3v C3v	C3v C3v	C3v C3v		1.00000
60	D3	D3	D3	D3	D3	D3	-	D3	D3		1.00000
61	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
63	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
64	D3	D3	D3	D3	D3	C3	C1	D3	D3	!	1.00000
65 66	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1		0.00000
67	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
68	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
69 70	C5 C5	C5	C5 C5	C5	C5 C5	C5	-	C5	C5		1.00000
71	C5	C5	C5	C5	C1	-	-	C5	C5	!	1.00000
72 73	C2 Cs	C2 Cs	C2 Cs	C2 Cs	C2 Cs	C2 Cs	C2	C2 Cs	C2 Cs		1.00000
74	D3d	D3d	D3d	D3d	D3d	-	-	D3d	D3d		1.00000
75 76	C2	C2	C2	C2	C2	-	C2	C2	C2		1.00000
77	C2	C2	C2	C2	C2	C2	C1	C2	C2	!	1.00000
78	C1	C2	C1	C1	C1	C2	-	C1	C2	!M	1.00000
79 80	D3	D3	D3	D3	D3	D3	-	D3	D3		1.00000
81	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
82	C1 C1	C1 D3	C1 C1	C1 D3	C1 C1	C1 D3	C1	C1 C1	C1 D3	IM	0.00000
84	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
85 86	C1	C1	C1	C1	C1 C2	C1 C2	C1	C1	C1		0.00000
87	C2v	C_{2v}	C2v	C2v	C2v	C2v	-	C2v	C_{2v}		1.00000
88	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
89 90	C1 C1	C3 C1		C3 C1	C1 C1	C1 C1	C3 C1	C1 C1	C3 C1	!M	0.99991
91	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
92	C1	Т	C1	Т	C1	Т	Т	C1	Т	!M	0.98969
93 94	C1	C1	C1	C1		C1	C1	C1	C1		0.00000
95	C3	C3	C3	C3	C3	C3	C3	C3	C3		1.00000
96 97	C1 C1	C1 C2	C1 C1	C1	C1 C1	C1	C1	C1 C1	C1 C2	IM	0.00000
98	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
99 100	C1	C2	C1	C1	C2 C1		C1	C1	C2	!M	0.99994
101	D3	D3	D3	D3	D3	C3	-	D3	D3	!	1.00000
102	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
103 104	C2 C1	C2 C2	C2 C1	C2 C1	C2 C1	C2 C1	$\overline{C2}$	C2 C1	C2 C2	!M	0.99999
105	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
106	C1	C1 C2	C1	C1	C1 C2	C1 C2	C1	C1	C1	114	0.00000
107	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
109	C1	\mathbf{Cs}	C1	C1	C1	C1	C1	C1	C1	!	0.00000
110 111	C2 C1	C_{5}	C2 C1	C2 C5	C2 C5	C2 C5	C2	C2 C1	C2 C5	IM.	1.00000
112	C1	Cs	C1	C1	C1	Č1	C1	C1	C1	1	0.00000
113	C1	Cs	C1 C2	C1	C1 C2	C1 C2	C1	C1	C1	!	0.00000
114 115	C2 Cs	C2 Cs	Cs Cs	C2 Cs	Cs Cs	C2 Cs	-	Cs Cs	Cs Cs		1.00000
116	D5h	D5h	D5h	D5h	D5h	D5h	-	D5h	D5h	.	1.00000
117	C1	_	C1 C1	C1	C1	C1	C1	C1	C1	'	0.00000

Table S45: Dataset: murrel-mottram/Na, part 1.

1	SY	VA	Sym	Mol		libmsym		SOFI		1	l
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
119	C1			C1 C2		-	Cs C1		Cs C2	IM IM	0.99992
121	C1	_	C1	C1	C1	C1	C1	C1	C1		0.00000
122	C1	-	C1	C1	C1	C1	C1	C1	D2	!M	0.99998
123	C1	-	C1	C1	C1	C1	C1	C1 C1	C1		0.00000
124	C1	_				C1	C1		C1		0.00000
126	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
127	C2	-	C2	C2	C_2	C_2	-	C2	C2		1.00000
128	C1	-	C1	C1	C1	C1	C1	C1 C2	C1 C2		0.00000
130	C1	_	C1	C1	C1	C1	C1	C1	C1		0.00000
131	C2	-	C2	C_2	C2	C_2	_	C2	C_2		1.00000
132	C1	-	C1	Cs	Cs	Cs	Cs	C1	Cs	!M	1.00000
133	C1 Ib	- Th	C1 Th	C1 Th	C1 Ib	C1 Ib	C1 Ib	C1 Th	C1 Ib		0.00000
135	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih	Ih		0.91157
136	C5v	-	C5v	C5	C5v	C5v	-	C5v	C5v	!	1.00000
137	C_{2v}	-	C2v	C2v	C2v	C2v	_	C2v	C_{2v}		1.00000
138	C2v	_	C2v	C2v	C2v	C2v	C3v C2v	C2v	C2v		1.00000
140	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
141	C5v	-	C5v	C5v	C5v	C5v	-	C5v	C5v		1.00000
142	Cs C2v	_	C1 C2v	Cs C2v	Cs C2v	Cs C2v		Cs C2v	Cs C2v	!	1.00000
143	C3v	_	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
145	C2v	-	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
146	C5v	-	C5v	C5v	C5v	C5v	-	C5v	C5v		1.00000
147	Cs	_	Cs	Cs	Cs	Cs	- In	Cs	In Cs		1 00000
149	C1	-	C1	Cs	-	-	-	C1	Cs	M	1.00000
150	C3v	-	_	_	C3v	-	C3v	C3v	C3v		1.00000
151 152	C1 C1	_		C1 C=	C ¹	_	Cs Ce		Cs Ce	!M !M	0.99839
153	C1	_	C1	_	C3v	C3v	C3v	C1	C3v	!M	1.00000
154	C1	-	C1	\mathbf{Cs}	Cs	_	\mathbf{Cs}	C1	\mathbf{Cs}	!M	1.00000
155	Cs C1	-	Cs	Cs	Cs C1	Cs	Cs C-	Cs C1	Cs C-	114	1.00000
157	C1	_		C2	C2v	C1 C2v	Us –		C_{2v}	IM IM	1,00000
158	Č1	-	C1	Č1	Cs	C1	-	C1	Cs	!M	1.00000
159	C_{2v}	-	C2v	C_{2v}	C2v	C2v	C1	C2v	C_{2v}	!	1.00000
160	C1	_		C1	C1 C1	C1	C1		C1		0.00000
162	C1	_	C1	C1	C1	C1 C1	C1	C1	C1		0.00000
163	Cs	-	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}		1.00000
164	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
165	C1	_		C1		C1	C1		C1		0.00000
167	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
168	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
169	C1 C1	-	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1		0.00000
170	C5	_	C5	C5	C5	C5	-	C5	C5		1.00000
172	C5	-	C5	C5	C1	C5	-	C5	C5	!	1.00000
173	C5	-	C5	C5	C5	C5	_	C5	C5		1.00000
174	C1	_		C1		-	_		C1		0.00000
176	C5	-	C5	C_{5}	-	-	C1	C5	C_{5}	!	1.00000
177	C5	-	C5	C5	C5	-	_	C5	C5		1.00000
178	C5 C1	-	C5 C1	C5 C1	-		C1	C5 C1	C5 C1	! !	1.00000
180	C1 C1	_	C1	C2h	C1	Ci	_	C1	C2h	!M	1.00000
181	C1	-	C1	C1	C1	C1	-	C1	\mathbf{Cs}	!M	0.99999
182	C1	-	C1	C2	C2	C1	-	C1	C2	!M	1.00000
183	D3d	_	S6	S6	D3d		_	D3d	D3d	!M	1 00000
185	C1	-	C1	C1	C1	C1	C1	C1	C1	· ·	0.00000
186	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
187	C1 C1	-	C1 C1	C1 C1		C1 C1	C1 C1		C1 C1		0.00000
189	C1	_	C1	C1	C1	C1	C1	C1	C1		0.00000
190	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
191	C1	-	C1	C3	C1 C1		C1	C1 C1	C3	!M	0.99999
192	C1	_	C1	C1	C1	C1	C1	C1	C1		0.00000
194	D3	-	C1	D3	D3	-	-	D3	D3	!	1.00000
195	C1	-	C1 C1	C1	C1 C1	C1 C1	-	C1 C1	C1		0.00000
190	C1	_		C1	C1	C1	C1	C1	C1		0.00000
198	C1	-	C1	C1	C1	C1	C1	C1	C_2	!M	0.99997
199	C1	-	C1	C1	C1	C1	-	C1	C1	13.5	0.00000
200	C1	_		C1	C1 C1	C1	 C1		C2 C1	1 M	0.00000
202	C1	_	C1	C1	C1	Č1	C1	C1	C1		0.00000
203	C3	-	C1	C3	C3	C3	C3	C3	C3	!	1.00000
204	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
205	C3	_		C3		-	C3		C3		1.00000
207	C1	-	C1	C3	C3	C1	C3	C1	C3	!M	1.00000
208	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
209 210	C1	_		C1		C1	C1 C1		C1 C2	IM	0.00000
211	C1	_	C1	C1	C1	C1	Č1	C1	C1		0.00000
212	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
213	C3	-	C3	C3	C3	C3		C3	C3		1.00000
214 215	CI	_	CI	CI	C1	C1	C1	C1	C1		0.00000
216	Č1	-	C1	т	Т	т	т	C1	т	!M	0.95174
217	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
218	C1 C1	_		C1 C1	C1 _	C1 C1	C1 C1		C1 C3	114	0.00000
220	C1	_	C1	C1	C1	C1	Č1	C1	C1		0.00000
221	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
222	C1	-	C1	C3	C3	C3	-	C1	C3	!M	1.00000
223 224	C1	_	C1	C3 C1	C1	 C1	C1	C1	C1	'	0.00000
225	C1	-	C1	C1	C1	C1	-	C1	C1		0.00000
226	C2	-	C1	C2	C2	-	-	C2	C2	! !	1.00000
227 228	C2	_	C2	C1 C2	C1	_	-	C2	C2	!	1.00000
										1	1

Table S46: Dataset: murrel-mottram/Na, part 2.

	SY	VA	Syn	nMol		libmsym		SC	FI	I	
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
229	C1 C1	-	C1 C1	C1 C1		C1	C1	C1 C1	C1 C2	114	0.00000
231	C1	_	C1	C1	C1	C1	C1	C1	C1		0.00000
232	C1	-	C1	D3	D3	-	-	C1	D3	!M	1.00000
233	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
234	C1 C1	_	C1	C1		C1		C1	C1		0.00000
236	C_2	-	C_2	C2	C2	C1	C1	C_2	C_2	!	1.00000
237	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
238	C1 C1	-	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1		0.00000
239	C1	_	C1	C1	C1	C1	C1	C1	C1		0.00000
241	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
242	C1	-	C1	C2	C2	C1	_	C1	C2	!M	1.00000
243	C1	_	C1 C1	C1 C1		CI	-	C1	C1 C2	IM	1.00000
245	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
246	D5	-	C5	D5	-	-	-	D5	D5	!	1.00000
247	C5	-	C5	C5	C5	-	C5	C5	C5	1.14	1.00000
248 249	C5 C1	_	C5 C1	C5 C1		 C1	 C1	C5 C1	D5 C1	11/1	0.00000
250	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
251	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
252	_	_	C1 C5	C1 C5		-	-	C1 C5	C1 C5		1.00000
254	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
255	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
256	-	-	C1	C1 C1	C1 C1	C1 C1	C1	C1	C1		0.00000
258	_	_	C5	D5	C1	-	_	C5	D5	!M	1.00000
259	-	-	C1	C_2	C1	C1	C1	C1	C_2	!M	1.00000
260	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
261 262	_	_	C1	C1	C1 C1	C1	C1	C1	C1		0.00000
263	_	_	C1	C1	C1	Č1	C1	C1	C1		0.00000
264	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
265	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
267	_	_	C1	C1	C1	C1	C1	C1	C1		0.00000
268	-	-	C1	C1	C1	C1	C1	C1	Ci		0.00000
269	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
270 271	_	_	C1	C1	C1	C1	C1	C1	C1		0.00000
272	-	-	C_2	C_2	C2	C_2	_	C_2	C_2		1.00000
273	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
274	-	-	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1	C1 C1		0.00000
276	_	_	C1	C1	C1	C1	C1	C1	C1		0.00000
277	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
278	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
279	_	_	C1	C1		C1	C1	C1	C1		0.00000
281	_	-	C1	C1	C1	C1	C1	C1	C1		0.00000
282	-	-	Cs	\mathbf{Cs}	Cs	C1	Cs	Cs	\mathbf{Cs}	!	1.00000
283	-	-	C1	C1	C1 C2w	C1 C2	C1 C2w	C1 C2w	C1 C2w		0.00000
284	_	_	_	_	C3v C3v	C3v C3v	C3v	C3v C3v	C3v C3v		1.00000
286	-	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
287	-	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
288	_	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
290	-	-	C5v	C5v	C5v	C5v	-	C5v	C5v		1.00000
291	-	-	C5v	C5v	C5v	C5v	-	C5v	C5v		1.00000
292	-	-	C5v	C5v	C5v	C5v	-	C5v	C5v	Ι.	1.00000
293	_	_	C1	C1	C1	C1	 C1	C1	Cs	!M	0.98891
295	-	-	C1	Cs	Cs	Cs	Cs	Cs	Cs	1	1.00000
296	-	-	Ih	Ih	Ih	Ih	Ih	Ih	Ih		0.97463
297	_	_	Ih C5v	In C5	Ih C5v	1h _	Ih _	Ih C5v	Ih C5v	Ι,	0.97429
299	-	-	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
300	-	-	_	_	C3v	_	-	C3v	C3v		1.00000
301	_	_	C2v	C2v Ce	C_{2v}	C2v	_	C_{2v}	C2v		1.00000
303	-	-	$\tilde{C}2$	$\tilde{C2}$	C2	C2	C2	C_2	$\tilde{C}2$		1.00000
304	-	-	C1	C1	Cs	_	Cs	Cs	Cs	!	1.00000
305	_	_	C2v	C2v	C2v C3v	C3v	_	C2v C3v	C2v C3v		1.00000
307	_	_	C2v	C2v	C2v	_	-	C_{2v}	C_{2v}		1.00000
308	-	-	C5v	C_{5}	C5v	_	-	C5v	C5v	!	1.00000
309	_	_	Th Ce	Ih Cc	fh Ce	fh _	1h _	1h Cs	1h Cs		0.99314
311	_	_	Cs	Cs	Cs	_	_	Cs	Cs		1.00000
312	-	-	-	-	C3v	C3v	-	C3v	C3v		1.00000
313	-	-	C1	Cs	-	_	Cs	Cs	Cs	!	1.00000
314 315	_	_	Cs	Cs	C3v	Cs -	Cs C3v	Cs C3v	Cs C3v		1.00000
316	_	_	_	_	C3v	C3v	C3v	C3v	C3v		1.00000
317	-	-	\mathbf{Cs}	\mathbf{Cs}	Cs	_	\mathbf{Cs}	\mathbf{Cs}	\mathbf{Cs}		1.00000
318	-	-	C1	Cs	C1	Cs C-	Cs	C1 C7	Cs	!M	1.00000
319	_	_	C1	Cs	Cs	Cs	Cs	Cs	Cs	1	1.00000
321	_	_	Č1	Cs	Čs	Čs	Cs	C1	Cs	!M	1.00000
322	-	-	C_1	C_1	C1	-	C1	C1	C3v	!M	1.00000
323	-	-	Cs	Cs	Cs C1	Cs	Cs	Cs	Cs	13.5	1.00000
324 325	_	_	C1	C3v	C1	Cs	Cs	Cs	C3v	!M	1.00000
326	-	-	C1	C1	C1	Ċs	-	C1	Cs	!M	1.00000
327	-	-	C1	C_{2v}	C2v	C2v	-	Cs	C_{2v}	!M	1.00000
328	_	_	C1 C1	C1 C1	C1	C1	C1 C1	C1 C1	C1 C1		0.00000
330	_	_	C1	C1	C1	C1	C1	C1	C1		0.00000
331	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
332	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
334	_	_	C1	C1	C1	C1	C1	C1	C1		0.00000
335	-	-	C1	Č1	C1	Č1	C1	Č1	Č1		0.00000
336	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
337 338	_	_	C1	C1		C1	C1 C1	C1	C1		0.00000
						-	-				

Table S47: Dataset: murrel-mottram/Na, part 3.

	SY	VA	Sym	Mol	libmsym			SOFI			
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
339	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
340	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
341	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
342	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
343	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
344	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
345	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
346	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
347	-	_	C5	C5	C5	-	-	C5	C5		1.00000
348	-	_	C5	C5	-	-	-	C5	C5		1.00000
349	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
350	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
351	-	_	C1	C1	C1	C1	-	C1	C1		0.00000
352	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
353	-	_	C5	C5	C1	-	-	C5	C5	1	1.00000
354	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
355	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
356	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
357	-	_	S6	S6	D3d	D3	-	D3d	D3d	1	1.00000
358	-	_	C1	C1	C1	-	-	C1	Cs	!M	0.99998
359	-	_	C1	Cs	C1	-	-	C1	Cs	!M	1.00000
360	-	_	C1	C1	C1	-	-	C1	C1		0.00000
361	-	_	C1	C1	C1	-	C1	C1	C1		0.00000
362	-	-	C1	C1	C1	C1	-	C1	Cs	!M	0.99988
363	-	_	C1	C1	C1	C1	-	C1	C1		0.00000
364	-	-	C1	Cs	C1	-	C1	Cs	Cs	!	1.00000
365	-	_	C1	C2	C1	C1	-	C1	C2	!M	1.00000
366	-	-	C1	C1	C1	-	-	C1	Cs	!M	0.85440
367	-	-	C1	C1	C1	C1	-	C1	C1		0.00000
368	-	-	C1	Cs	C1	-	-	C1	Cs	!M	1.00000
369	-	-	C1	C3v	-	-	-	C1	C3v	M	1.00000
370	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
371	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
372	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
373	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
374	-	_	C1	C1	C1	C1	C1	C1	C1		0.00000
375	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
376	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
377	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
378	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
379	- 1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
380	-	-	C1	C1	C1	C1	C1	C1	C1		0.00000
								-			

Table S48: Dataset: murrel-mottram/Na, part 4.

	SY	VA	Sym	Mol	libmsym		SOFI				
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
3	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
4	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v		1.00000
5	C1	C1	C1	C1	C1	C1	-	C1	C1		0.00000
6	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
7	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
8	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v		1.00000
9	C3h	C3h	C3h	C3h	C3h	C3h	-	C3h	C3h		1.00000
10	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
11	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
12	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v		1.00000
13	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		0.94097
14	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
15	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
16	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
17	C4v	-	C4v	C4v	C4v	C4v	-	C4v	C4v		1.00000
18	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
19	C2	-	C2	C2	C2	C2	C2	C2	C2		1.00000
20	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
21	C4v	-	C4v	C4v	C4v	C4v	C4v	C4v	C4v		1.00000
22	D4h	-	C4h	C4h	D4h	D4h	-	D4h	D4h	1	1.00000
23	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
24	D3	-	D3	D3	D3	D3	D3	D3	D3		1.00000
25	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
26	C4v	-	C4	C4	C4v	C4v	-	C4v	C4v	1	1.00000
27	C2v	-	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
28	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
29	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
30	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
31	D4h	-	C4h	C4h	D4h	D4h	-	D4h	D4h	1	1.00000
32	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
33	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
34	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
35	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000

Table S49: Dataset: NaCl_N/welch, part 1.

	SY	VA	Sym	Mol	libmsym			SOFI			
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
3	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
4	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v		1.00000
5	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
6	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
7	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
8	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v		1.00000
9	C3h	C3h	C3h	C3h	C3h	C3h	-	C3h	C3h		1.00000
10	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
11	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
12	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v		1.00000
13	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		0.94424
14	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
15	C1	Cs	C1	C1	C1	C1	C1	C1	C1	1	0.00000
16	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
17	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v		1.00000
18	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
19	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
20	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
21	C4v	-	C4v	C4v	C4v	C4v	C4v	C4v	C4v		1.00000
22	D4h	_	C4h	C4h	D4h	D4h	D4h	D4h	D4h	!	1.00000
23	Cs	-	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
24	C1	_	C1	C1	C1	C1	C1	C1	C1		0.00000
25	Cs	_	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
26	C4v	-	C4	C4	C4v	C4v	-	C4v	C4v	1	1.00000
27	C2v	-	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
28	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
29	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
30	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
31	D4h	-	C4h	C4h	D4h	D4h	-	D4h	D4h	!	1.00000
32	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
33	C1	-	C1	C1	C1	C1	C1	C1	C1		0.00000
34	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
35	Cs	-	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000

Table S50: Dataset: NaCl_N/CBM, part 1.

	SY	VA	Sym	Mol	libmsym		SOFI				
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
17A	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
17B	Č.	Č.	Č.	Č.	Č.	Č.	Č.	Č.	Č.		1.00000
170	C3v	Cav	C3v	C3v	C3v	Cav	Cav	C3v	Cav		1 00000
27 4	Car	Car	Car	Car	Car	Car	Car	Car	Car		1.00000
27A	C2V	C2V	020	020	020	C2V	C2V	0.20	C2V		1.00000
278	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
28A	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
28B	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
30A	C_{2v}	C_{2v}	C_{2v}	C_{2v}	C_{2v}	C2v	C2v	C_{2v}	C_{2v}		1.00000
30B	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
31A	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
31B	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
31C	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
32A	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
32B	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
33A	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
33B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
34 A	C2v	C2v	C2v	C_{2v}	C2v	C2v	C_{2v}	C2v	C_{2v}		1.00000
34B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
354	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
25 D	Ca	Ca	Ca	Ca	Ca	Ca	Ca		Ca		1.00000
336	Cs Cr	Cs C-	Cs	Cs C-	Cs C-	Cs C-	Cs C-	Cs C-	Cs		1.00000
30A	Cs C-	Cs C-	Cs C-	Cs C-	Cs C-	Cs C-	Cs C-	Cs C-	Cs		1.00000
306	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
37A		CI		CI			CI		CI		0.00000
37B	CI	CI	CI	CI		CI	CI		CI		0.00000
38A	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		0.99980
38B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
44A	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
44B	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
57A	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs	Cs		1.00000
57B	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
66A	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
66B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
67A	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
67B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
72A	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
72B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
75 4	Ce	D5h	C1	C5	C5v	_	_	C1	D5h	IM	1 00000
75 P	C1	C1	C1	C1	C1	C1	C1		C1		0.00000
764	Ce	C		C	C	Ce	-	C	Ce		1 00000
768	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
760	CI	CI		CI	CI	C1	CI		CI		0.00000
7700	C2	Can	Can	Carr	C2	C2	C2	C2	Can		1.00000
774	C2V	020	020	C2V	C2V	C2V	C2V	C2V	C2V		1.00000
77B		CI		CI			CI		CI		0.00000
770	CI	CI	CI	CI		CI	CI	CI	CI		0.00000
78A	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
78B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
82A	C1	C1	C1	C1	C1	-	C1	C1	C1		0.00000
82B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
83A	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
83B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
84A	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
84B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
86A	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
86B	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
98A	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.82308
98B	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000

Table S51: Dataset: QLJ, part 1.

	SV.	VΔ	l Sym	Mol		libmeym		1 50	FI		
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
3	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	um	1 00000
4	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.99850
5	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
6	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		0.93406
7	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
8	D2d	D2d	D2d	D2d	D2d	D2d	D2d	D2d	D2d		1.00000
9	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
10	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
11	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
12	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v	C5v		1.00000
13	Ih	-	Ci	Ci	Ih	Ih	Ih	Ih	Ih	!	0.98001
14	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
15	D6d	-	C6	C6	D6d	D6d	D6d	D6d	D6d	!	1.00000
16	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
17	C2v	C2v	C2v	C2v	C2v	C2v	C2	C2v	C2v	!	1.00000
18	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
19	D5h	D5h	C5	C5	D5h	D5h	D5h	D5h	D5h	!	1.00000
20	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
21	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
22	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
23	C_2	C_2	C2	C_2	C2	C_2	C_2	C2	C_2		1.00000
24	C_2	C_2	C2	C_2	C2	C_2	C1	C2	C_2	!	1.00000
25	C3	C3	C3	C3	<u>C3</u>	C3	C3	C3	C3		1.00000
26	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
27	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
28	C1	C1		C1		C1	C1		C1		0.00000
29	C2	C2	C2	C2		C2	C2		C2		1.00000
30	Cs	Cs	Cs	Cs	Us CS	Us	Cs	Cs	Cs		1.00000
31	03	03	03	03	03	03	03	C3	03		1.00000
32	D2d	D2d	D2d	D2d	D2d	D2d	D2d	D2d	D2d		1.00000
33	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
34	C2	C2	C2 D2	C2	C2	C2	C_2	C2 D2	C2		1.00000
30	D3	D3 C2	D3 C2	D3 C2	D3 C2:	D3 C2	-	D3 C2	D3 C2		1.00000
30	C2v	C2v	020	020	C2V	020		C2V	C2v		1.00000
31	Ob	Ob	Oh	Oh	Oh	Oh	Ob	Ob	Ob		1.00000
20	C4w	C4w		C1	C4w	C4w	On	C4w	C4w		1.00000
40	C ₄ v	C*V	C4 C2	C4	C ₄ V	Ce Ce	C.	C ₄ v	C=		1.00000
41	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs	Cs		1 00000
42	Cs	Cs	Cs	Cs	Čs	Cs	Cs	Cs	Cs		1.00000
43	Cs	Cs	Cs	Cs	Čs	Čs	Cs	Cs	Cs		1.00000
44	C_2	C_2	C2	C_2	C2	C_2	C_2	C2	C_2		1.00000
45	Cs	Cs	Cs	Cs	Čs	Čs	Cs	Cs	Cs		1.00000
46	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
47	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
48	C2v	C2v	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
49	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
50	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
51	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
52	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
53	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
54	C5v	C5v	C5	C5	C5v	C5v	-	C5v	C5v	!	1.00000
55	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	!	0.98488
56	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
57	Cs	Cs	Cs	Cs	Cs	Cs	-	Cs	Cs		1.00000
58	D3h	D3h	D3h	D3h	D3h	D3h		D3h	D3h		1.00000
59	Td	Td	Td	Td	Td	Td	D'I'	Td	Td		0.86070
60	C2v	C_{2v}	C2v	C2v	C2v	C2v	-	C2v	C_{2v}		1.00000
61	C3v	C3v	C3v	C3v	C3v	C3v	-	C3v	C3v		1.00000
62	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
63	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
04	C2v	C2v	C2v C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
65	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
67	Cs	Cs	Cs	Cs	Cs	Cs Cs	Cs	Cs	Cs	l .	1.00000
67	C2v C2v	C_{2v}	C2v	C2v	C2v C2v	C2v	Cs	C2v	C2v	! !	1.00000
60	Cov	Cav			C3V	C3V C2	C3v	Car	Cav	.	1.00000
09 70	C2V	C2v	C2V	C2V		Ca	Ca		C2v	'	1.00000
70	C2v	C2v	C2v	C2v	Car	Cav	C:	C2v	C2v		1.00000
72	C1	C1	C1	C1	C1	C1	Ci	C1	C1	l :	0.00000
73	C	C.		C.		Ce	C		C.		1 00000
74	C5v	C5v	C5	C5	C5v		08	C5v	C5v		1.00000
75	D5h	D5h	D5h	C5	D5h		_	D5h	D5h		1.00000
76	C2v	C2v	C2v	Car	C2v	C2v	_	C2v	C2v	'	1 00000
77	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	Cs	C2v	C_{2v}	· ·	1 00000
78	Cs	Cs.	Cs	Cs.	Cs	Cs	Cs.	Cs	Cs.	l .	1.00000
79	D3h	D3h	D3h		D3h	D3h	D3h	D3h	D3h		1.00000
80	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000

Table S52: Dataset: sutton_9_6, part 1.

	SY	VA	Sym	Mol	1	libmsym		l so	FI	1	I
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
3	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
4	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.98731
6	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		0.88855
7	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
8	D2d	D2d	D2d	D2d	D2d	D2d	D2d	D2d	D2d		1.00000
9	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
10	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
11	C2v	C_{2v}	C2v	C_{2v}	C2v	C_{2v}	C_{2v}	C2v	C_{2v}		1.00000
12	- C2 Th	02	Ci	Ci	102 115	U2 1b	C2 Th		U2 1b	, I	0.99522
14	C6v	C6v	C6v	C6v	C6v	C6v	C6v	C6v	C6v	· ·	1.00000
15	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
16	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
17	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
18	Cs Cr	Cs C-	Cs C-	Cs C-	Cs C-	Cs C-	Cs	Cs C-	Cs C-		1.00000
20	C2v	C2v	C2v	C2v	C2v	Cav	Cav	C2v	C2v		1.00000
21	C6v	C6v	C6	C6	C6v	C6v	C6v	C6v	C6v	1	1.00000
22	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
23	C2	C2	C2	C2	C2	C2	C2	C2	C2		1.00000
24	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
25		C1 C		C1 C		C1	C1		C1 C		0.00000
26	Cs Cs	Cs Cs	Cs Cs	Cs Cs	Cs	Cs	Cs	Cs Cs	Cs		1.00000
28	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
29	C2	C_2	C2	C_2	C2	C2	C2	C2	C_2		1.00000
30	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
31	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
32	C3	C3	C3	C3	C3	C3	_	C3	C3		1.00000
33	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
34	C	C.		C.	C	Ca	C		C ^o		1.00000
36	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	-	C2v	C_{2v}		1.00000
37	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
38	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		1.00000
39	C4v	C4v	C4	C4	C4v	C4v	-	C4v	C4v	!	1.00000
40	D4h Ca	D4h C-	D4h C-	C4h	D4h C-	D4h C-	D4h Ca	D4h C-	D4h C-	! !	1.00000
41	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
43	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
44	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	\mathbf{Cs}		1.00000
45	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
46	C3	C3	C3	C3	C3	C3	_	C3	C3		1.00000
47	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
48	D5h	D5h	C5	C5	D5h	D5h	D5h	D5h	D5h	· ·	1 00000
50	D3h	D3h	D3h	D3h	D3h	D3h	_	D3h	D3h		1.00000
51	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
52	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	_	C2v	C_{2v}		1.00000
53	C3v C2w	C3v C2v	C3v C2w	C3v C2v	C3v C2v	C3v C2v	C3v C2v	C3v C2w	C3v C2w		1.00000
54 55	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
56	D2h	D2h	D2h	D2h	D2h	D2h	_	D2h	D2h		1.00000
57	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
58	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
59	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C2v	C2v	C_{2v}		1.00000
60	C2v C2v	C_{2v}	C2v C2v	C2v C2v	C2v C2v	C2v C2v	-	C2v C2v	C2v C2v		1.00000
62	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs		1.00000
63	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
64	C2v	C2v	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
65	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
66	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Ι.	1.00000
69	C2v C2v	C2v C2v	C2v	C2v	C2v C2v	C2v C2v	Car	C2v C2v	C2v C2v	'	1.00000
69	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
70	Cs	Čs	Čs	Čs	Čs	Čs	Čs	Čs	Čs		1.00000
71	C2v	C2v	C2v	C2v	C2v	C2v	Cs	C2v	C2v	!	1.00000
72	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
73	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	.	1.00000
(4 75	D5b	D5b	D5h	U5 D5h	D5b	_	_	D5b	D5b	'	1.00000
76	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	_	C2v	C_{2v}		1.00000
77	C2v	C_{2v}	C2v	C2v	C2v	C_{2v}	Cs	C2v	C2v	!	1.00000
78	Cs	Cs	Cs	Cs	Cs	Cs	C1	Cs	Cs	!	1.00000
79	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		0.98778
80	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v	C4v		1.00000

Table S53: Dataset: sutton_10_8, part 1.

	l ev	VA.	l Sum	Mol	I.	libmaum		1 80	FI		I.
name	0.001	0.05	0.001	0.05	'default'	'medium'	'loose'	0.001	0.05	diff	dot product
3	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
4	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.99681
5	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h	D3h		1.00000
6	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh	Oh		1.00000
7	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h	D5h		1.00000
8	D2d	D2d	D2d	D2d	D2d	D2d	D2d	D2d	D2d		1.00000
9	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	C_{2v}	C2v	C_{2v}		1.00000
10	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
11	C2v	C2v	C2v	C2v	C2v C5	C2v	C2v	C2v	C2v		1.00000
12	USV	Cov	Ci	Ci	USV	USV	Cov	USV	USV		0.04451
14	C3v	Cav	C3v	Cav	C3v	C3v	C3v	C3v	C3v		1 00000
15	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
16	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
17	C_2	C_2	C2	C2	C2	C_2	C2	C2	C2		1.00000
18	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
19	D5h	D5h	C5	C5	D5h	D5h	D5h	D5h	D5h	!	1.00000
20	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
21	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
22	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
23	D3h Ga	D3h	D3h	D3h Go	D3h Ga	D3h Ga	_	D3h	D3h Ga		1.00000
24	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v	C2v C2v		1.00000
20	Dab	Dap	Dab	Dap	Dap	Dap	Dap	Dab	Dap		1.00000
20	Ce	C	Ce	C	Ce	Ce	Ce	Ce	Ce		1.00000
28	C3v	C3v	_		C3v	C3v	C3v	C3v	C3v		1.00000
29	C2v	C_{2v}	C2v	C2v	C2v	C2v	C2v	C2v	C_{2v}		1.00000
30	C2v	C2v	C2v	C_{2v}	C2v	C2v	Cs	C2v	C2v	!	1.00000
31	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
32	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
33	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
34	C2v	C2v	C2v	C2v	C2v	C2v	-	C2v	C2v		1.00000
35	C2v	C_{2v}	C2v	C_{2v}	C2v	C_{2v}	C_{2v}	C2v	C_{2v}		1.00000
36	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
37	C3v	C3v		_	C3v	C3v	C3v	C3v	C3v		1.00000
38	C4m	Class	C1	On C4	C4m	C4.	On	C4m	C4m		1.00000
39	C24V	C4V	C4	C4		C4V Ce	 C=		C4V		1.00000
40	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
42	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
43	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
44	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
45	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	Cs	Cs	Cs		1.00000
46	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v	C2v		1.00000
47	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
48	C2v	C_{2v}	C2v	C_{2v}	C2v	C2v	_	C2v	C_{2v}		1.00000
49	C3v	C3v	C3v	C3v	C3v Dal	C3v	C3v	C3v	C3v		1.00000
50	D3n C2u	Can	C2m	D3n C2m	D3n C2w	Can	D3h	C2m	D3n C2		1.00000
52	C3v	C ₂ v	020	020	C3v	C3v	C3v	C3v	C2v C2v		1.00000
53	C2v	C_{2v}	C2v	C2v	C2v	C2v		C2v	C2v		1.00000
54	C5v	C5v	C5	C5	C5v	C5v	_	C5v	C5v	!	1.00000
55	Ih	Ih	Ci	Ci	Ih	Ih	Ih	Ih	Ih	!	0.97111
56	C3v	C3v	-	-	C3v	-	-	C3v	C3v		1.00000
57	Cs	\mathbf{Cs}	Cs	\mathbf{Cs}	Cs	Cs	\mathbf{Cs}	Cs	Cs		1.00000
58	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v	C3v		1.00000
59	Td	Td	Td	Td	Td	Td	Td	Td	Td		0.96339
60	Cs	Cs	Cs	Cs	Cs	Us C2	Cs	Ca	Ca		1.00000
63	C2v	C_{2v}	C2v	C2v C2v	C2v	C2v C2v	C2v C2v	C2v	C2v		1.00000
0⊿ 63	C2V	C2V		C2v		Czv	C2V		C2V		1.00000
64	C2v	C2v	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
65	C2v	C2v	C2v	C2v	C2v	C2v	_	C2v	C2v		1.00000
66	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
67	C2v	C2v	C2v	C2v	C2v	C2v	\mathbf{Cs}	C2v	C2v	!	1.00000
68	C3v	C3v	-	-	C3v	C3v	C3v	C3v	C3v		1.00000
69	C1	C1	C1	C1	C1	C1	C1	C1	C1		0.00000
70	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs	Cs		1.00000
71	C2v	C_{2v}	C2v	C2v	C2v	C2v	Cs	C2v	C2v	!	1.00000
72	C1	C1		C1		C1	C1		C1	,	0.00000
13	C5v	C5v	C5	C5	C5v	C2v	Cs	C5v	C5v		1.00000
75	D5b	D5b	D5h	C5	D5h	 D5h	_	D5b	D5b		1 00000
76	Cs	Cs	Cs	Cs	Cs	Cs	_	Cs	Cs	l ,	1.00000
77	C2v	C2v	C2v	C2v	C2v	C2v	\mathbf{Cs}	C2v	C2v		1.00000
78	C1	C1	C1	C1	C1	C1	C1	C1	C1	·	0.00000
79	D3h	D3h	D3h	_	D3h	D3h	D3h	D3h	D3h		1.00000
80	Cs	Cs	Cs	\mathbf{Cs}	Cs	Cs	-	Cs	Cs		1.00000

Table S54: Dataset: sutton_12_6, part 1.

References

- M. Gunde, N. Salles, L. Grisanti, L. MARTIN-SAMOS, and A. Hemeryck, "SOFI: Finding point group symmetries in atomic clusters as finding the set of degenerate solutions in a shape-matching problem," Jul. 2024. [Online]. Available: https://doi.org/10.5281/zenodo.12773914
- [2] L. Gyevi-Nagy and G. Tasi, "Syva: A program to analyze symmetry of molecules based on vector algebra," *Computer Physics Communications*, vol. 215, pp. 156–164, 2017. [Online]. Available: https://www.sciencedirect.com/science/article/pii/S0010465517300310
- [3] T. Pilati and A. Forni, "SYMMOL: a program to find the maximum symmetry group in an atom cluster, given a prefixed tolerance," Journal of Applied Crystallography, vol. 31, no. 3, pp. 503–504, Jun 1998. [Online]. Available: https://doi.org/10.1107/S0021889898002180
- [4] M. Johansson and V. Veryazov, "Automatic procedure for generating symmetry adapted wavefunctions," *Journal of Cheminformatics*, vol. 9, no. 1, p. 8, Feb 2017. [Online]. Available: https://doi.org/10.1186/s13321-017-0193-3
- [5] D. J. Wales, J. P. K. Doye, A. Dullweber, M. P. Hodges, F. Y. N. F. Calvo, J. Hernández-Rojas, and T. F. Middleton, "The cambridge cluster database." [Online]. Available: https://www-wales.ch.cam.ac.uk/CCD.html
- [6] D. J. Wales and J. P. K. Doye, "Global optimization by basin-hopping and the lowest energy structures of lennard-jones clusters containing up to 110 atoms," *The Journal of Physical Chemistry A*, vol. 101, no. 28, pp. 5111–5116, 1997. [Online]. Available: https://doi.org/10.1021/jp970984n
- [7] F. Calvo, J. P. K. Doye, and D. J. Wales, "Quantum partition functions from classical distributions: Application to rare-gas clusters," *Journal of Chemical Physics*, vol. 114, pp. 7312–7329, 2001. [Online]. Available: https://doi.org/10.1063/1.1359768
- [8] J. P. K. Doye and D. J. Wales, "Global minima for transition metal clusters described by suttonchen potentials," New J. Chem., vol. 22, pp. 733–744, 1998. [Online]. Available: http://dx.doi.org/10.1039/A709249K
- J. P. K. Doye, "A model metal potential exhibiting polytetrahedral clusters," The Journal of Chemical Physics, vol. 119, no. 2, pp. 1136–1147, 2003. [Online]. Available: https://doi.org/10.1063/1.1574797
- [10] J. P. K. Doye and S. C. Hendy, "On the structure of small lead clusters," The European Physical Journal D - Atomic, Molecular, Optical and Plasma Physics, vol. 22, no. 1, pp. 99–107, Jan 2003. [Online]. Available: https://doi.org/10.1140/epjd/e2002-00232-x
- [11] J. P. K. Doye, "Identifying structural patterns in disordered metal clusters," Phys. Rev. B, vol. 68, p. 195418, Nov 2003. [Online]. Available: https://link.aps.org/doi/10.1103/PhysRevB.68.195418
- [12] E. G. Noya, J. P. K. Doye, D. J. Wales, and A. Aguado, "Geometric magic numbers of sodium clusters: Interpretation of the melting behaviour," *The European Physical Journal D*, vol. 43, no. 1, pp. 57–60, Jul 2007. [Online]. Available: https://doi.org/10.1140/epjd/e2007-00092-x
- [13] J. P. Doye, "Lead clusters: Different potentials, different structures," Computational Materials Science, vol. 35, no. 3, pp. 227–231, 2006, proceedings of the 4th International Conference on the Theory of Atomic and Molecular Clusters (TAMC-IV). [Online]. Available: https://www.sciencedirect.com/science/article/pii/ S0927025605001278
- [14] J. Elliott, Y. Shibuta, and D. Wales, "Global minima of transition metal clusters described by finnissinclair potentials: A comparison with semi-empirical molecular orbital theory," *Philosophical Magazine*, vol. 89, no. 34-36, pp. 3311–3332, 2009. [Online]. Available: https://doi.org/10.1080/14786430903270668
- [15] J. P. Doye and D. J. Wales, "The structure of (c60)n clusters," *Chemical Physics Letters*, vol. 262, no. 1, pp. 167–174, 1996. [Online]. Available: https://www.sciencedirect.com/science/article/pii/0009261496010391
- [16] J. P. K. Doye, D. J. Wales, W. Branz, and F. Calvo, "Modeling the structure of clusters of c₆₀ molecules," *Phys. Rev. B*, vol. 64, p. 235409, Nov 2001. [Online]. Available: https: //link.aps.org/doi/10.1103/PhysRevB.64.235409
- [17] D. J. Wales and J. P. K. Doye, Theoretical Predictions of Structure and Thermodynamics in the Large Cluster Regime. Dordrecht: Springer Netherlands, 1996, pp. 241–279. [Online]. Available: https://doi.org/10.1007/978-94-009-0211-4_9

- [18] J. P. K. Doye and D. J. Wales, "The effect of the range of the potential on the structure and stability of simple liquids: from clusters to bulk, from sodium to," *Journal of Physics B: Atomic, Molecular and Optical Physics*, vol. 29, no. 21, p. 4859, nov 1996. [Online]. Available: https://dx.doi.org/10.1088/0953-4075/29/21/002
- [19] J. P. K. Doye and D. J. Wales, "Structural consequences of the range of the interatomic potential a menagerie of clusters," J. Chem. Soc., Faraday Trans., vol. 93, pp. 4233–4243, 1997. [Online]. Available: http://dx.doi.org/10.1039/A706221D
- [20] J. P. K. Doye, D. J. Wales, and S. I. Simdyankin, "Global optimization and the energy landscapes of dzugutov clusters," *Faraday Discuss.*, vol. 118, pp. 159–170, 2001. [Online]. Available: http://dx.doi.org/10.1039/B008881L
- [21] J. P. K. Doye and D. J. Wales, "Polytetrahedral clusters," *Phys. Rev. Lett.*, vol. 86, pp. 5719–5722, Jun 2001.
 [Online]. Available: https://link.aps.org/doi/10.1103/PhysRevLett.86.5719
- [22] J. P K Doye and D. J Wales, "Structural transitions and global minima of sodium chloride clusters," *Phys. Rev. B*, vol. 59, pp. 2292–2300, Jan 1999. [Online]. Available: https://link.aps.org/doi/10.1103/PhysRevB.59.2292
- [23] J. P. K. Doye and L. Meyer, "Mapping the magic numbers in binary lennard-jones clusters," *Phys. Rev. Lett.*, vol. 95, p. 063401, Aug 2005. [Online]. Available: https://link.aps.org/doi/10.1103/PhysRevLett.95.063401
- [24] M. D. Hanwell, D. E. Curtis, D. C. Lonie, T. Vandermeersch, E. Zurek, and G. R. Hutchison, "Avogadro: an advanced semantic chemical editor, visualization, and analysis platform," *Journal of Cheminformatics*, vol. 4, no. 1, p. 17, Aug 2012. [Online]. Available: https://doi.org/10.1186/1758-2946-4-17